The recent observation of the electron self-energy renormalization effect in the form of a “kink” in the dispersion has generated considerable interest because it reveals a coupling of the electrons with a collective boson mode of the cuprate superconductors[1]. However, the nature of the bosons involved remains controversial mainly because the previous experiments can only be used to determine an approximate energy of the mode and this energy is close to both the optical phonon[2, 3] and the spin resonance[4]. Determining the nature of the mode(s) that couple to the electrons is likely important in understanding the pairing mechanism of superconductivity.

In conventional superconductors, identification of the fine structure for the phonon anomalies in the tunnelling spectra has played a decisive role in reaching a consensus on the nature of the bosons involved[5]. The fine structure provides fingerprints for much more stringent comparison with known boson spectra. So far, such fine structure has not been detected in the angle-resolved photoemission spectroscopy (ARPES) data. In this Letter we present significantly improved high resolution ARPES data of (La$_{2-x}$Sr$_x$)$_2$CuO$_4$ (LSCO) that, for the first time, reveal fine structure in the electron self-energy, demonstrating the involvement of multiple boson modes. We identify four bosonic modes that couple to the electrons and the energies of the modes are near 27, 45, 61 and 75 meV. This fine structure is different from the spin excitation spectrum but corresponds to some known phonon features in this material.

The photoemission measurements were carried out on beamline 10.0.1.1 at the ALS, using a Scienta 2002 electron energy analyzer. As the real part of electron self-energy is already a small effect, high energy resolution and high data statistics are necessary to investigate its fine structure. The experimental conditions are set to compromise between these two conflicting requirements. The photon energy is 55 eV and the energy and angular resolutions are 18~20 meV and 0.3 degree, respectively(see [3] for details). An example of the high quality of the raw data is shown in Figs. 1a and 1b. Due to space charge problem, the Fermi level calibration has a ±2.5 meV uncertainty. We mainly present our data on the heavily underdoped LSCO x=0.03 (non-superconducting), LSCO x=0.07 (T$_c$=14 K) and LSCO x=0.063 (T$_c$=12 K) samples. The heavily underdoped LSCO samples are best candidates because they exhibit a stronger band renormalization effect[3]; a relatively large magnitude of the real self-energy makes the identification of the fine structure easier. The LSCO single crystals are grown by the travelling solvent floating zone method[7]. The samples were cleaved in situ in vacuum with a base pressure better than 4×10$^{-11}$ Torr. The measurement temperature was ∼20K so all samples were measured in the normal state.

We have used the MDC method to extract the energy-momentum dispersion relation (Fig. 1c). We chose to measure the dispersion along the nodal direction because this is technically the most reliable direction to get high quality dispersion data using the momentum distribution curves (MDC). It has been shown theoretically that this approach is reasonable in spite of the momentum-
The energy points were taken under the same condition, i.e., each energy point was averaged over the entire detector range along the energy direction. Therefore, all the energy points were taken under the same condition, independent of the detector inhomogeneity. The possibility of noise problem can also be ruled out because they are supposed to be random while for different samples, under different experimental conditions such as different experimental conditions and in the samples that exhibit the energy points were taken using the "swept mode" of the electron analyzer. While the fine structure is subtle and one may argue about individual curves, we have invariably observed them near similar energies in many independent measurements. The measurements of different dopings make the presence of the fine structure convincing and consistent.

A natural question is whether the fine structure can be due to instrumental artifact which may be related to detector inhomogeneity and/or system noise. The possibility of detector problem can be ruled out because the data were taken using the "swept mode" of the electron analyzer, i.e., each energy point was averaged over the entire detector range along the energy direction. Therefore, all the energy points were taken under the same condition, independent of the detector inhomogeneity. The possibility of noise problem can also be ruled out because they are supposed to be random while for different samples, under different experimental conditions such as different photon energies and different pass energies of the analyzer (Fig. 2a1 and 2a2), the multiple structures are all invariant in binding energy.

The existence of fine structure indicates the involvement of several collective modes in the coupling, with each structure representing a "subkink" in the dispersion and defining the energy scale of the mode. We quantify the characteristic energies by fitting a smooth curve through the ReΣ data and then performing second-order derivative to the fitted curve. Given the noise level in the data, a spline through the data is difficult and somewhat subjective. To this end, we first use the MEM procedure which has been exploited to extract the spectral features of the electron-phonon coupling from ARPES data for the two-dimensional surface state of Be[9]. Since a priori we do not know whether the method developed for conventional metal can be extended to cuprate superconductors, we use it only as the first step a procedure for systematic curve fitting. The MEM is more objective in getting the fine structure because the number of peaks and their positions are insensitive to the fitting details[9].

The fitted curves are shown in Fig. 2a together with the measured ReΣ . In Fig 2b, we show the second-order derivative of the fitted curves whose peaks reveal

FIG. 1: (a) Typical raw data of a two-dimensional image showing the photoelectron intensity as a function of the momentum and energy for the LSCO x=0.063 sample. The intensity is expressed by the false-color. The measurement was taken along the (0,0)-(π,π) nodal direction and at a temperature of 20 K. (b) The photoemission spectra (energy distribution curves, EDCs) for the LSCO x=0.063 sample corresponding to Fig. 1a. The spectrum at the Fermi momentum k_F=(0.44π/a, 0.44π/a) (red curve) shows a sharp peak. (c) The energy-momentum dispersion for LSCO x=0.03(c1), x=0.063 (c2) and x=0.07 (c3) samples, as determined from fitting the MDCs. The green dashed lines connecting the two points at the Fermi energy and -0.2 eV are examples of a simple selection of the bare band.

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The energies of the collective modes. As expected, the peaks correspond to anomalies in the raw data. Three main features near 27, 45 and 61 meV can be resolved for different samples with different doping levels, consistent with the fine structure visible to a naked eye in the electron self-energy (Fig. 2a). Again, the consistency and the robustness of the energy scales in all the data sets give credence to these three energy scales revealed. In addition, the MEM procedure has resulted in one more possible feature between 70 and 80 meV which appears stronger with increasing doping[10].

The existence of fine structure in the electron self-energy indicates that there must be fine structure present in the underlying bosonic spectral function. The identified multiple sharp features (Fig. 2b) are very different from the magnetic excitation spectra measured in LSCO and (La,Ba)$_2$CuO$_4$ from neutron scattering[11]. On the other hand, the first three features (Fig. 2b) show close correspondence to the three low-energy features in the phonon density-of-states (DOS), measured also from neutron scattering on LSCO (Fig. 2c)[12]. We do not see the strong phonon feature near 85~90 meV but we observe a feature near 75 meV which appears to get more pronounced at higher doping. This is consistent with the known result that the full-breathing phonon mode near 85~90 meV shows much weaker doping-induced change, indicating a weaker coupling, than the anomalous doping-induced softening of the half-breathing mode from 80 meV to 70 meV, indicating a much stronger coupling[12]. This phonon softening leads to a new peak in the phonon DOS near 75 meV as observed in the x=0.08 sample (Fig. 2b)[12]. The good correspondence between the extracted fine structure and the measured phonon features provides further evidence that the bosons involved in the coupling are phonons. In addition to the half-breathing mode at 70~80 meV that we previously considered strongly coupled to electrons[2], the present results reveal that several lower energy optical phonons of oxygens are also actively involved. This means that the observed renormalization has several contributions so that the quantitative value of the coupling strength should not be attributed to the highest energy of the breathing mode alone.

For conventional metals, the MEM procedure can be used to extract the Eliashberg function which gives spectral features of the electron-phonon coupling[9]. For strongly correlated cuprate superconductors, a priori it is unclear whether the Eliashberg formalism is applicable or not. However, we note that the nodal excitation of LSCO in the normal state may provide a closest case for the procedure to be applicable. Recent transport measurements reveal that a quasiparticle picture may be still reasonable for electrons near the nodal direction, even for very low doping[13]. This is consistent with the ARPES data which show a well-defined peak in the nodal spectrum in the lightly doped samples[3]. The nodal dispersion does not have pronounced structure in its bare band, unlike the strong curvature near the saddle point of the antinodal region. The selection of the nodal direction in the normal state also minimizes complications due to the existence of a superconducting gap or pseudogap in the extraction process.

Given these considerations and the fact that there is no better alternative available, we have applied the Eliashberg formalism and the MEM procedure to extract the effective bosonic function from the real part of the electron self-energy (Fig. 3a). It is clear that the multiple features are rather robust against the choice of the bare band by varying $a_1$ and $a_2$. All other tests as detailed in [9] have been carried out. The fine structure as obtained from
bosonic functions obtained by using different bare bands as represented by the different sets of \( a_1 \) and \( a_2 \) values. (b) The MDC width of LSCO \( x=0.03 \) (open circles). The contribution from the electron-phonon coupling (blue line) is calculated from the effective bosonic function in Fig. 3a with \( a_1=-4.25 \) and \( a_2=0 \). The “impurity” contribution is assumed to be a constant (dotted black line). The momentum resolution here is 0.019 °A\(^{-1}\). After subtracting all the electron-phonon and “impurity” contributions, the residual part is proportional to \( \omega^\alpha (\alpha \sim 1.5) \) (green line).

LSCO \( x=0.03 \) is in agreement with that in the second-order derivative shown in Fig. 2b. The calculated real part of the electron self-energy is plotted in Fig. 3a to-gether with the measured data. Fig. 3b shows the MDC width which is directly related to \( \text{Im}\Sigma=(\Gamma/2)v_0 \), with \( \Gamma \) being the MDC width (Full-Width-at-Half-Maximum, FWHM) and \( v_0 \) the bare velocity. While there is a drop near 75 meV, there is an overall increase of the MDC width with increasing binding energy (Fig. 3b), which is different from simple electron-phonon coupling systems such as Be[8]. The MEM analysis allows us to calculate the abrupt drop in \( \text{Im}\Sigma \) which is due to electron-phonon coupling. After subtracting the contributions from the electron-phonon coupling, “impurity” scattering, and angular resolution, the residual part is found to be proportional to \( \omega^\alpha (\alpha \sim 1.5) \) (Fig. 3b). This term most likely represents the contribution of the electron-electron interaction. The corresponding electron-electron contribution in the real part of the self-energy is a smooth function and may be absorbed into the “bare dispersion” because we focus only on abrupt structure in Re\( \Sigma \) in extracting the bosonic spectral function. Here we also note that while the imaginary part of the electron self-energy is consistent with the existence of electron-phonon coupling, it is difficult to identify the fine structure as has been done for the real part because of the larger experimental uncertainty in determining the peak width over the peak position. This analysis also shows that there is an internal consistency in the MEM procedure that connects the real and imaginary parts of the self-energy.

In summary, by taking high resolution data on heavily underdoped LSCO samples with high statistics, we have detected fine structure from multiple bosonic coupling in the electron self-energy near 27, 45, 61 and 75 meV.

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[10] For the \( x=0.07 \) sample, the peak at 74 meV in the second-order derivative (Fig. 2b) is not due to the two abnormal data points near 73 meV (Fig. 2a). By removing those two points, the effective bosonic spectral function extracted is similar to that obtained from the original data.
[11] S. M. Hayden et al., Phys. Rev. Lett. 76, 1344 (1996); J. Tranquada et al., cond-mat/0401621. From both measurement and associated calculations, the magnetic spectra are smooth except for a broad peak at a lower energy (~20 meV). Although the data points were not as dense as in phonon DOS measurement[12], there was no indication of fine structure similar to the fine structure shown in Fig. 2b.