Recent BaBar Studies of Bottomonium States

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We present studies in bottomonium spectroscopy carried out with samples of (98±1) million Υ(2S) and (121±1) million Υ(3S) events recorded with the BaBar detector at the PEP-II asymmetric-energy $e^+e^-$ collider at SLAC. Precise measurements of the branching fractions for $\chi_{b1,2}(1P, 2P) \rightarrow \gamma \Upsilon(1S)$ and $\chi_{b1,2}(2P) \rightarrow \gamma \Upsilon(2S)$ transitions, and searches for radiative decay to the $\eta_b(1S)$ and $\eta_b(2S)$ states are performed using photons that have converted into an $e^+e^-$ pair. In addition, we summarize the results of a search for the spin-singlet partner of the $\chi_{bJ}(1P)$ triplet, the $h_b(1P)$ state of bottomonium, in the transitions $\Upsilon(3S) \rightarrow \pi^0h_b$ and $\Upsilon(3S) \rightarrow \pi^+\pi^-h_b$.

1. Introduction

Bottomonia are the heaviest of the $q\bar{q}$ bound states. Decays within the bottomonium family of states occur via $\pi^0$, $\eta$, $\omega$ or di-pion emission, or by electric dipole transitions or magnetic dipole transitions. Electromagnetic transitions between the energy levels of the bottomonium spectrum can be calculated in the quark model and are an important tool in understanding the internal structure of $b\bar{b}$ bound states. In particular, the measurement of the hyperfine mass splittings between triplet and singlet states is paramount to understanding the role of spin-spin interactions in quarkonium models and in testing QCD calculations. In the non-relativistic approximation, the hyperfine splitting is proportional to the square of the wave function at the origin, which is expected to be non-zero only for $L = 0$, where $L$ is the orbital angular momentum quantum number of the $q\bar{q}$ system.

In particular, the mass splitting between the $\Upsilon(1S)$ and the $\eta_b(1S)$ is a key ingredient in many theoretical calculations. The value measured by BaBar, $m(\Upsilon(1S)) - m(\eta_b(1S)) = 69.3\pm2.8$ MeV/$c^2$ [1,2] and subsequently by CLEO [3] is larger than most predictions based on potential models [4], but in reasonable agreement with predictions from lattice calculations [2]. According to ref. [6], the shift in measured $\eta_b(1S)$ compared to QCD predictions might be explained by the mixing of the $\eta_b$ with a CP-odd Higgs scalar. To test this model, a measurement of the $\eta_b$ width is essential, and this was one of the BaBar motivations for searching for the $\eta_b$ using photon conversions as described in Sec. 2.

For $L = 1$, the splitting between the spin-singlet ($^1P_1$) and the spin-averaged triplet state ($^3P_J$) is expected to be $\Delta M_{HF} = M(^3P_J) - M(^1P_1) \sim 0$. The $^1P_1$ state of bottomonium, the $h_b(1P)$, is the axial vector partner of the $P$-wave $\chi_{bJ}(1P)$ states. Its expected mass, computed as the spin-weighted center of gravity of the $\chi_{bJ}(1P)$ states [4], is 9899.87±0.27 MeV/$c^2$. Higher-order corrections might cause a small deviation from this value, but a hyperfine splitting larger than 1 MeV/$c^2$ might be indicative of a vector component in the confinement potential [8]. The hyperfine splitting for the charmonium $^1P_1$ state $h_c$ is measured by the BES and CLEO experiments [4,11] to be $\sim0.1$ MeV/$c^2$. An even smaller splitting is expected for the much heavier bottomonium system [8].

The BaBar [12] experiment collected data at the narrow $\Upsilon(nS)$ resonances in order to carry out detailed studies in bottomonium spectroscopy [1].

We summarize the results of a study of radiative bottomonium transitions using $\gamma \rightarrow e^+e^-$ conversions, and of searches for the $h_b(1P)$ state in $\Upsilon(3S) \rightarrow \pi^0h_b(1P)$ decay [13] and $\Upsilon(3S) \rightarrow \pi^-h_b(1P)$ decay [14].

2. Study of radiative bottomonium transitions using $\gamma \rightarrow e^+e^-$ conversions

The rate of $\gamma \rightarrow e^+e^-$ conversion in the detector material, and of the reconstruction of the $e^+e^-$ pairs is much lower than that for photons reconstructed using the BaBar electromagnetic calorimeter. However, the substantial improvement in energy resolution for photon conversions results in better separation of photon energy lines.

1These samples correspond to 14 fb$^{-1}$ and 30 fb$^{-1}$ of $\Upsilon(2S)$ and $\Upsilon(3S)$ data, respectively.

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Photon conversions are reconstructed with a dedicated fitting algorithm that pairs oppositely charged particle tracks to form secondary vertices away from the interaction point. To remove internal conversions and Dalitz decays, and to improve signal purity, the conversion vertex radius is restricted to the beampipe, SVT, support tube, and inner wall of the DCH (see Fig. 1).

The data are divided into four energy ranges (see Fig. 2) corresponding to bottomonium transitions, in Υ(3S) data,

- $180 \leq E^*(\gamma) \leq 300$ MeV: $\chi_{bJ}(2P) \rightarrow \gamma \Upsilon(2S)$
- $300 \leq E^*(\gamma) \leq 600$ MeV: $\Upsilon(3S) \rightarrow \gamma \chi_{bJ}(1P)$ and $\Upsilon(3S) \rightarrow \gamma \eta_b(2S)$
- $600 \leq E^*(\gamma) \leq 1100$ MeV: $\chi_{bJ}(2P) \rightarrow \gamma \Upsilon(1S)$ and $\Upsilon(3S) \rightarrow \gamma \eta_b(1S)$

and in Υ(2S) data,

- $300 \leq E^*(\gamma) \leq 800$ MeV: $\chi_{bJ}(1P) \rightarrow \gamma \Upsilon(1S)$ and $\Upsilon(2S) \rightarrow \gamma \eta_b(1S)$.

The photon energy ($E^*(\gamma)$) is analysed in the center-of-mass (CM) frame of the initial $\Upsilon(2S,3S)$ system. The photon spectra from subsequent boosted decays (e.g. $\chi_{bJ}(nP) \rightarrow \gamma \Upsilon(1S)$) are consequently affected by Doppler broadening due to the motion of the parent state in the CM frame. This broadening of the lineshapes of the various photon lines is incorporated into the fits used to extract the yields for the branching fractions obtained.
The number of signal events for a given bottomonium transition is extracted from the data by performing a \( \chi^2 \) fit to the \( E^*(\gamma) \) distribution in 1 MeV intervals. The functional form and parameterization for each photon signal are determined from simulation. In general, the lineshape is related to a Crystal Ball function \( CBF \), i.e. a Gaussian function with a power-law tail. This functional form is used to account for bremsstrahlung losses of the \( e^+e^- \) pair. The underlying smooth inclusive photon background is described by the product of a polynomial and an exponential function. This functional form adequately describes the background in each separate energy range.

The decays \( \Upsilon(3S) \to \gamma \chi_{b0,2}(1P) \) are observed, and precise measurements of the branching fractions for \( \chi_{b1,2}(1P,2P) \to \gamma \Upsilon(1S) \) and \( \chi_{b1,2}(2P) \to \gamma \Upsilon(2S) \) decays obtained. The background-subtracted fit results are shown in Fig. 2. The product of branching fractions \( B(\Upsilon(nS) \to \gamma \chi_{b/J}) \times B(\chi_{bJ} \to \Upsilon(1S)) \) obtained from the fit of Fig. 2 are consistent with, and improve upon, the current values \cite{1}.

The searches for \( \eta_b(1S) \) and \( \eta_b(2S) \) states using the converted photon energy spectrum are largely inconclusive.

Table 1: Summary of Branching Fraction Measurements. The first uncertainty is statistical and the second systematic. Upper limits are given at the 90% confidence level.
Over a range of approximately $9974 < m_{b}(2S) < 10015$ MeV/c², we find $\mathcal{B}(\Upsilon(3S) \rightarrow \gamma \eta_b(2S)) < 1.9 \times 10^{-3}$ (at 90% C.L.). This value is consistent with, but does not improve upon, the upper limit obtained by CLEO [15]. Due to low efficiency and high background levels, no evidence for $\Upsilon(2S) \rightarrow \gamma \eta_b(1S)$ is found. The most significant peaking structure seen in the $E^*(\gamma)$ energy region expected for the $\Upsilon(3S) \rightarrow \gamma \eta_b(1S)$ transition, if interpreted as a $\eta_b$ signal, trends toward recent potential model [16] and lattice [17] predictions. However, the small (< 3σ) significance of the result is insufficient to measure the $\eta_b$ mass from the present analysis. Taking advantage of the improved resolution from a converted photon technique to make a definitive measurement of the $\eta_b$ mass and width will require much more data from future experiments.

The measured branching fractions obtained from the fits of Fig. 2 are listed in Table 1.

3. The BaBar search for the $h_b(1P)$ in $\Upsilon(3S)$ data

The $h_b(1P)$ state is expected to be produced in $\Upsilon(3S)$ decay via $\pi^0$ or di-pion emission, and to undergo a subsequent $E1$ transition to the $\eta_b(1S)$, with branching fraction (BF) $\mathcal{B}(h_b(1P) \rightarrow \gamma \eta_b(1S)) \sim (40 - 50)%$ [8]. The isospin-violating decay $\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(2S)$ (hereafter denoted $\Upsilon^{3-2}$) produce a peak centered at the $\Upsilon(2S)$ mass $(m[\Upsilon(2S)] = 10.20326 \pm 0.00031$ GeV/c² [8]). The cascade process $\Upsilon(3S) \rightarrow \Upsilon(2S)X$, $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$ ($\Upsilon^{2-1}$) results in a peak centered at 9.791 GeV/c². The peak is offset from the $\Upsilon(1S)$ mass by approximately the $\Upsilon(3S)$ to $\Upsilon(2S)$ mass difference. Doppler shift and broadening further affect the position and width of this peak. When the $\Upsilon(2S)$ parent in $\Upsilon^{2-1}$ decays is produced through the $\Upsilon^{3-2}$ channel, a pion from the $\Upsilon(3S)$ decay can be combined with an oppositely-charged track from the $\Upsilon(2S)$ decay to produce a broad distribution centered around 9.9 GeV/c². The $\Upsilon(2S)$ is also produced through the initial-state radiation (ISR) process $e^+e^- \rightarrow \gamma_{ISR} \Upsilon(2S)$ ($\Upsilon^{2+1}$). Of the nine possible $\Upsilon(3S) \rightarrow \chi_{bJ}(2P)\gamma_{ISR} \Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$ decay chains (\(\chi_{bJ}^{J,J'}\)), only those for \(J' = J\) = 1, 2 have been reported [7]; these should generate two slightly separated peaks near 9.993 GeV/c², while the contributions with \(J' \neq J\) or with \(J = 0\) are expected to be negligible.

No $h_b(1P)$ signal is seen in the $\Upsilon(3S) \rightarrow \pi^+\pi^- h_b$ production channel. Assuming the $h_b$ mass to be 9.900 GeV/c², we set a 90% C.L. upper limit $\mathcal{B}[\Upsilon(3S) \rightarrow \pi^+\pi^- h_b] < 1.2 \times 10^{-4}$, which excludes, at 90% CL, values of $\mathcal{B}[\Upsilon(3S) \rightarrow \pi^+\pi^- h_b] < 1.8 \times 10^{-4}$ for a wide range of assumed $h_b$ mass values. These results disfavor the calculations of Refs. [21, 22]. Similarly, a recent measurement of the $\Upsilon(1S)[D_J] \rightarrow \Upsilon(1S)\pi^+\pi^-$ branching fraction [23] disfavors the calculations of Ref. [24]. The predictions of Ref. [24] are at least one order of magnitude smaller and are not contradicted by our result.

Figure 3 shows the distribution of $m_{R}$ after subtraction of the non-peaking background. An expanded view of the $\chi_{bJ}^{J,J'}$ region is shown on the right.

A branching fraction measurement $\mathcal{B}(\Upsilon(3S) \rightarrow \pi^+\pi^- \Upsilon(2S)) = (3.00 \pm 0.02$ (stat.) $\pm 0.14$ (syst.))% improves over the current world average (2.45 ± 0.23)% [8]. Product branching fractions $\mathcal{B}(\Upsilon(3S) \rightarrow X_{\chi_{b1}}(2P)) \times \mathcal{B}(X_{\chi_{b1}}(2P) \rightarrow \pi^+\pi^- \chi_{b1}) = (1.16 \pm 0.07 \pm 0.12) \times 10^{-3}$, $\mathcal{B}(\Upsilon(3S) \rightarrow X_{\chi_{b2}}(2P)) \times \mathcal{B}(X_{\chi_{b2}}(2P) \rightarrow \pi^+\pi^- \chi_{b2}) = (0.64 \pm 0.05 \pm 0.08) \times 10^{-3}$, and $\mathcal{B}(\Upsilon(3S) \rightarrow \chi_{bJ}(2P)) \times \mathcal{B}(\chi_{bJ}(2P) \rightarrow \pi^+\pi^- \Upsilon(2S)) = (1.78 \pm 0.02 \pm 0.11)%$ are also obtained from this analysis. In addition, we obtain a measurement of 331.50 ± 0.02 (stat.) ± 0.13 (syst.) MeV/c² for the $\Upsilon(3S)$-$\Upsilon(2S)$ mass difference.

3.2. Evidence for the $h_b(1P)$ in the decay $\Upsilon(3S) \rightarrow \pi^0 h_b$

Evidence for the $h_b(1P)$ state is obtained in the decay $\Upsilon(3S) \rightarrow \pi^0 h_b(1P)$, by requiring a photon with an energy consistent with that for the $h_b(1P) \rightarrow \gamma \eta_b(1S)$ transition. The number of $\pi^0$ events in $m_{\text{recoil}}(\pi^0)$ is
A π⁰ candidate is reconstructed as a photon pair with invariant mass m(γγ) in the range 55–200 MeV/c² (see Fig. 4). In the calculation of m_{recoil}(π⁰), the γ-pair invariant mass is constrained to the nominal π⁰ value [7] in order to improve the momentum resolution of the π⁰. We employ a simple set of criteria based on kinematic and event-shape variables to suppress backgrounds. Photons from π⁰ decays are a primary source of background in the region of the signal photon line from h_b → γγ_b transitions. Similarly, many misreconstructed π⁰ candidates result from the pairing of photons from different h_b's. We impose the π⁰ veto² condition on all photon candidates to improve the purity of the π⁰ and photon candidate sample.

We obtain the m_{recoil}(π⁰) distribution in 90 intervals of 3 MeV/c² from 9.73 to 10 GeV/c². For each m_{recoil}(π⁰) interval, the m(γγ) spectrum consists of a π⁰ signal above combinatorial background (see Fig. 4). We construct the m_{recoil}(π⁰) spectrum by extracting the π⁰ signal yield in each interval of m_{recoil}(π⁰) from a fit to the m(γγ) distribution in that interval. The m_{recoil}(π⁰) distribution is thus obtained as the fitted π⁰ yield and its uncertainty for each interval of m_{recoil}(π⁰).

We use the MC background and MC π⁰-signal distributions directly in fitting the m(γγ) distributions in data. For each m_{recoil}(π⁰) interval in MC, we obtain histograms in 0.1 MeV/c² intervals of m(γγ) corresponding to the π⁰-signal and background distributions. The π⁰-signal distribution is obtained by requiring matching of the reconstructed to the generated π⁰'s on a candidate-by-candidate basis (termed “truth-matching” in the following discussion). The histogram representing background is obtained by subtraction of the π⁰ signal from the total distribution.

For both signal and background the qualitative changes in shape over the full range of m_{recoil}(π⁰) are quite well reproduced by the MC. However, the π⁰ signal distribution in data is slightly broader than in MC, and is peaked at a slightly higher mass value. The m(γγ) background shape also differs between data and MC. To address these differences, the MC π⁰ signal is displaced in mass and smeared by a double Gaussian function with different mean and width values; the MC background distribution is weighted according to a polynomial in m(γγ). The signal-shape and background-weighting parameter values are obtained from a fit to the m(γγ) distribution in data for the full range of m_{recoil}(π⁰). At each step in the fitting procedure, the π⁰ signal and background distributions are normalized to unit area, and a χ² between a linear combination of these MC

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²A signal photon candidate is rejected if, when combined with another photon in the event (γ₂), the resulting γγ₂ invariant mass is within 15 MeV/c² of the nominal π⁰ mass; this is called a π⁰ veto.
Figure 4: The result of the fit to the $m(\gamma\gamma)$ distribution in data (data points) for the full range of $m_{\text{recoil}}(\pi^0)$. The solid histogram shows the fit result, and is essentially indistinguishable from the data; the shaded histogram corresponds to the background distribution.

histograms and the $m(\gamma\gamma)$ distribution in data is computed. The fit function provides an excellent description of the data ($\chi^2/NDF=1446/1433$; $NDF=$Number of Degrees of Freedom) and the fit result is essentially indistinguishable from the data histogram. The background distribution exhibits a small peak at the $\pi^0$ mass, due to interactions in the detector material of the type $n\pi^+ \to p\pi^0$ or $p\pi^− \to n\pi^0$ that cannot be truth-matched. The normalization of this background to the non-peaking background is obtained from the MC simulation, which incorporates the results of detailed studies of interactions in the detector material performed using data [25]. This peak is displaced and smeared as for the primary $\pi^0$ signal.

The fits to the individual $m(\gamma\gamma)$ distributions are performed with the smearing and weighting parameters fixed to the values obtained from the fit shown in Fig. 4. In this process, the MC signal and background distributions for each $m_{\text{recoil}}(\pi^0)$ interval are shifted, smeared, and weighted using the fixed parameter values, and then normalized to unit area. Thus, only the signal and background yields are free parameters in each fit. The $\chi^2$ fit to the data then gives the value and the uncertainty of the number of $\pi^0$ events in each $m_{\text{recoil}}$ interval.

To search for an $h_b$ signal, we perform a binned $\chi^2$ fit to the $m_{\text{recoil}}(\pi^0)$ distribution obtained in data. The $h_b$ signal function is represented by the sum of two Crystal Ball functions [26] with parameter values, other than the $h_b$ mass, $m$, and the normalization, determined from simulated signal $\Upsilon(3S) \to \pi^0 h_b$ events. The background function is a fifth order polynomial, where parameter values are obtained from a fit which excludes the signal region (see Fig. 5(a)).

We then perform a fit over the signal region to search for an $h_b$ signal of the expected shape, taking account of the correlated uncertainties related to the polynomial interpolation procedure, but with the fitted values of the polynomial coefficient fixed.

In Fig. 5(b) we plot the difference between the distribution of $m_{\text{recoil}}(\pi^0)$ and the fitted histogram of Fig. 5(a) over the entire region from 9.73 GeV/$c^2$ to 10.00 GeV/$c^2$; we have combined pairs of 3 MeV/$c^2$ intervals from Fig. 5(a) for clarity.

The width of the observed signal is consistent with experimental resolution, and its significance is 3.3 $\sigma$, including systematic uncertainties. The measured mass value, $m = 9902 \pm 4(\text{stat.}) \pm 2(\text{syst.})$ MeV/$c^2$, is consistent with the expectation for the $h_b(1P)$ bottomonium state, the axial vector partner of the $\chi_{bJ}(1P)$ triplet of states. We obtain the value $(4.3 \pm 1.1(\text{stat.}) \pm 0.9(\text{syst.})) \times 10^{-4}$ for the product branching fraction $B(\Upsilon(3S) \to \pi^0 h_b) \times B(h_b \to \gamma\eta_b)$.

This measurement combined with the expected rate for the $h_b(1P) \to \gamma\eta_b(1S)$ transition [8] would indicate that the $\Upsilon(3S) \to \pi^+\pi^- h_b(1P)$ is suppressed by a factor greater than 3 w.r.t. $\Upsilon(3S) \to \pi^0 h_b(1P)$.
4. Conclusions

A study of radiative transitions between bottomonium states using photons that have been converted to $e^+e^-$ pairs in the detector material led to the observation of $\Upsilon(3S) \rightarrow \gamma \chi_{b0,2}(1P)$ decays, and to precise measurements of the branching fractions for $\chi_{b1,2}(1P,2P) \rightarrow \gamma \Upsilon(1S)$ and $\chi_{b1,2}(2P) \rightarrow \gamma \Upsilon(2S)$ decays.

Studies of inclusive di-pion and $\pi^0$ transitions was carried out using $\Upsilon(3S)$ events. While we find no evidence for the bottomonium spin-singlet state $h_b(1P)$ in the invariant mass distribution recoiling against the $\pi^+\pi^-$ system, we obtain evidence at the 3.3$\sigma$ level for the $h_b(1P)$ in $\Upsilon(3S) \rightarrow \pi^0 h_b(1P)$ decay. Shortly after the BaBar $h_b$ search results were obtained, preliminary results of a search for the $h_b$ in the reaction $e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$ ($n = 1, 2$) in data collected near the $\Upsilon(5S)$ resonance were announced by the Belle Collaboration [27]. The $h_b(1P)$ mass measured therein agrees very well with the value reported in this paper. It is interesting to note that the $e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$ cross sections measured in the Belle analysis relative to the $e^+e^- \rightarrow \Upsilon(2S)\pi^+\pi^-$ cross section are large, indicating an anomalous production rate for the $h_b(1P)$ and $h_b(2P)$, and suggesting that these states are maybe produced via an exotic process that violates the suppression of heavy quark spin-flip.

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