

SUSY Simplified Models at 14, 33, and 100 TeV Proton Colliders

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Abstract

Results are presented for a variety of SUSY Simplified Models at the 14 TeV LHC as well as a 33 and 100 TeV proton collider. Our focus is on models whose signals are driven by colored production. We present projections of the upper limit and discovery reach in the gluino-neutralino (for both light and heavy flavor decays), squark-neutralino, and gluino-squark Simplified Model planes. Depending on the model a jets + E_T^{miss} , mono-jet, or same-sign di-lepton search is applied. The impact of pileup is explored. This study utilizes the Snowmass backgrounds and combined detector. Assuming 3000 fb^{-1} of integrated luminosity, a gluino that decays to light flavor quarks can be discovered below 2.3 TeV at the 14 TeV LHC and below 11 TeV at a 100 TeV machine.

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1 Introduction

The Large Hadron Collider (LHC) has completed its 8 TeV run. Searches for a wide variety of beyond the Standard Model (SM) states, both in the context of Supersymmetry (SUSY) and otherwise, have been (and are being) performed. The absence so far for any signatures of new particles lurking in the 8 TeV data does not deter the expectation that new physics will be accessible at colliders. The next stage of the energy frontier collider effort will begin once the LHC has completed its upgrade to a center-of-mass energy approaching 14 TeV. In addition, discussions of collider physics beyond the LHC have begun; of particular relevance here are plans for a proton collider with $\sqrt{s} \sim 100$ TeV. In light of all this activity, it is interesting to develop a quantitative picture for the physics potential of the next phase of the LHC and beyond.

This work provides a study of the reach of the LHC upgrade and future proton colliders in the context of SUSY Simplified Models [1–3]. Supersymmetry is one of the best-motivated possibilities for new physics within the reach of future machines. Supersymmetric models provide a framework for constructing collider searches that generically cover additional motivated extensions of the SM; most importantly signals that involve missing energy and/or heavy flavor production. Furthermore, there is a cornucopia of results on SUSY extensions to the SM using 8 TeV LHC data that provide a useful reference point for comparing the reach of future colliders. Clearly, assessing the ability to search for new physics in the context of SUSY is a convenient benchmark for understanding the general physics potential of future proton colliders.

Given the vast possibilities for signatures that can be realized within the SUSY framework, we choose to work with the signature driven approach of Simplified Models. The philosophy underlying Simplified Models is simple: isolate the minimal field content required to produce a specific SUSY signature — it then becomes tractable to optimize a search such that it provides the maximal reach in both mass and $\sigma \times \text{BR}$. In practice, Simplified Models are IR-defined Lagrangian based theories that consist of a minimal number of particles and couplings; by keeping the number of free parameters to $\mathcal{O}(\text{a few})$, it is possible to understand the consequences of a given experiment for the entire parameter space.

Note that Simplified Models do not capture certain features of “complete” SUSY models; this approach remains agnostic about complimentary phenomenology, *e.g.* dark matter. For contrast consider the UV-motivated simplified parameter space of the CMSSM; many of these models do contain multiple collider accessible particles, but it is only possible to explore the full parameter space with a non-trivial combination of experiments including proton colliders and dark matter detection [4]. Another fruitful approach for understanding complementarity between experiments is the reduced IR parameter space of the pMSSM [5]. However, it can be challenging to interpret and generalize the results of CMSSM or pMSSM specific collider searches to more generic settings.

The parameter space of SUSY Simplified Models has been explored in great detail at the 8 TeV LHC by both the ATLAS and CMS collaborations (for a recent overview of the experimental

exclusions and the implications for SUSY models, see [6]). In this work we focus on minimal SUSY extensions of the SM with colored initial states. These models are expected to provide the greatest sparticle mass reach at hadron colliders.

In particular, motivated by expectations for the “first signatures” of SUSY, we study the following Simplified Models:

Section	Simplified Model	Decay Channel
3 and 4	Gluino-neutralino with light flavor decays	$\tilde{g} \rightarrow q \bar{q} \tilde{\chi}_1^0$
5 and 6	Squark-neutralino	$\tilde{q} \rightarrow q \tilde{\chi}_1^0$
7	Gluino-squark with a massless neutralino	$\tilde{g} \rightarrow (q \bar{q} \tilde{\chi}_1^0 / q \tilde{q}^*); \tilde{q} \rightarrow (q \tilde{\chi}_1^0 / q \tilde{g})$
8	Gluino-neutralino with heavy flavor decays	$\tilde{g} \rightarrow t \bar{t} \tilde{\chi}_1^0$

Our analyses loosely follow existing public 8 TeV search strategies from the ATLAS and CMS collaborations with optimizations performed to account for the higher luminosity and energy. We study the impact of pileup conditions to estimate how our conclusions could be altered by the harsh environments of running proton colliders at high instantaneous luminosity. Additional studies on the impact of systematic uncertainties are provided for a few models.

Discovery reach and exclusions limits are given for the following collider scenarios:

Machine	\sqrt{s}	Final Integrated Luminosity
LHC Phase I	14 TeV	300 fb ⁻¹
HL-LHC or LHC Phase II	14 TeV	3000 fb ⁻¹
HE-LHC	33 TeV	3000 fb ⁻¹
VLHC	100 TeV	3000 fb ⁻¹

The results presented in this work use the common Snowmass backgrounds [7], which were generated using the Open Science Grid [8]. The Snowmass detector framework [9] was used for signal and background event reconstruction. QCD backgrounds were not simulated as the preselection cuts have been demonstrated to effectively eliminate any QCD contamination. Note that all results presented here are based on existing Monte Carlo and detector simulation tools extended to 33 TeV and 100 TeV. We do not investigate the uncertainties related to the extrapolation of parton distribution functions or the modeling of electroweak contributions to the parton shower at high collision energies (for some discussion of these issues, see the Snowmass report from the energy frontier QCD working group [10]).

While studies assuming center-of mass energies beyond 14 TeV do exist, for example the famous EHLQ paper on SSC collider physics [11], the results presented here represent some of the first

computations that have been done using modern Monte Carlo and detector simulation tools. This work is a broad first step in the realistic assessment of the capabilities of future proton colliders for new particle searches. This work, along with other Snowmass 2013 studies of new physics searches at 33 TeV [12–15] and 100 TeV [16–21] colliders, provides a useful reference for evaluating future experimental options and a launching point for further detailed investigation.

The rest of the paper is organized as follows. Section 2 compares our results with an official 14 TeV ATLAS study. The remaining sections are divided by the particular choice of Simplified Model, with separate sections for the searches targeted in the compressed regions of parameter space. Sections 3–7 describe the searches and results for Simplified Models with hadronic final states, with the details of the common analyses and the impact of pile-up and systematics discussed in the context of the gluino-neutralino model in Sec. 3 and for compressed spectra in Sec. 4. Section 8 presents the analysis and sensitivity of a leptonic search for the gluino-neutralino model with heavy flavor decays. An appendix provides the details of the Monte Carlo framework employed for this study.

A companion paper [22] provides a summary of the results and lessons learned. Its purpose is to emphasize the compelling case for future proton colliders.

2 Validation

In order to validate our event generation and weighting procedures, we have made a comparison with an ATLAS study on the capabilities of the high luminosity 14 TeV LHC [23]. Specifically, ATLAS provides distributions for benchmark points in the gluino-squark plane with

- $m_{\tilde{g}} = 3200 \text{ GeV}; m_{\tilde{q}} = 3200 \text{ GeV}$
- $m_{\tilde{g}} = 2800 \text{ GeV}; m_{\tilde{q}} = 2400 \text{ GeV}$

where the following requirements are enforced: $E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$, no leptons, and four jets with $p_T > 60 \text{ GeV}$.

In the left panel of Fig. 1 we show the m_{eff} distribution for signal and backgrounds from [23] and on the right we show our analogous distribution. The signal distributions are the same within the tolerance of the systematic uncertainty assumed below. We find that the parts of the distributions within the cut regions for our analyses appear to be consistent to within 10%. The $E_T^{\text{miss}}/\sqrt{H_T}$ distribution, also provided in [23], is also consistent with our results. Finally, we note that while we use slightly different search strategies (and have used different detector simulations) we obtain similar results for the gluino-squark plane presented below in Sec. 7.

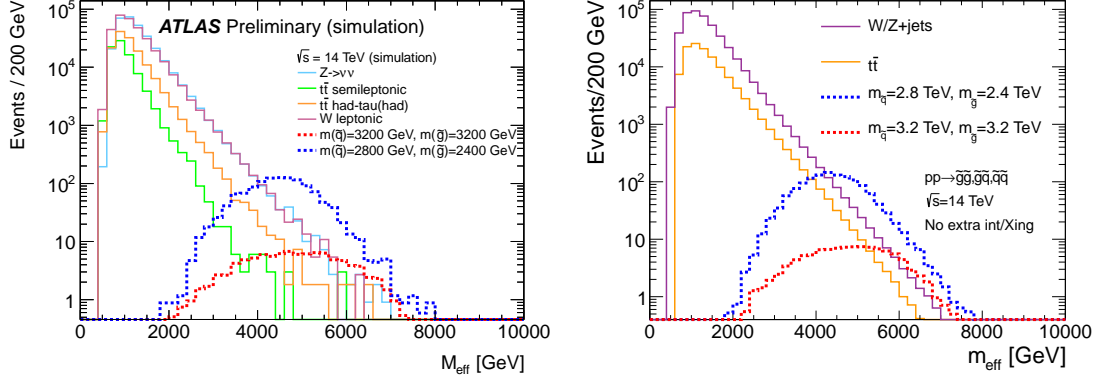


Figure 1: Plotted on the left [right] is the histogram of m_{eff} for the validation model as determined by ATLAS [this study]. Note that an exact comparison between the background not possible since we use the Snowmass particle containers, *i.e.* $W + \text{jets}$ and $Z + \text{jets}$ are plotted together. The background histograms are not stacked.

3 The Gluino-Neutralino Model with Light Flavor Decays

In the “gluino-neutralino model with light flavor decays”, the gluino \tilde{g} is the only kinematically accessible colored particle. The squarks are completely decoupled and do not contribute to gluino production diagrams. The gluino undergoes a prompt three-body decay through off-shell squarks, $\tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$, where $q = u, d, c, s$ are the first and second generation quarks and $\tilde{\chi}_1^0$ is a neutralino LSP. The branching ratios to all four flavors of light quark are taken to be equal. The only two relevant parameters are the gluino mass $m_{\tilde{g}}$ and the neutralino mass $m_{\tilde{\chi}_1^0}$. This model can be summarized by:

BSM particles	production	decays
$\tilde{g}, \tilde{\chi}_1^0$	$pp \rightarrow \tilde{g}\tilde{g}$	$\tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$

This model is motivated by (mini-)split supersymmetry scenarios, where the scalar superpartners are heavier than the gauginos [24–28]. The final state is four (or more) hard jets and missing energy. Therefore, this signature provides a good proxy with which to investigate the power of a traditional jets plus E_T^{miss} style hadron collider search strategy to discriminate against background.

We simulated matched MadGraph samples for $\tilde{g}\tilde{g}$ with up to 2 additional generator level jets for the following points in parameter space:¹

¹We include 1 GeV for an example where the neutralino is effectively massless; the second line of neutralino masses is chosen to cover the bulk of the gluino-neutralino plane; the final line is chosen to ensure coverage in the “compressed” region.

BSM particles	masses
$m_{\tilde{g}}$ [14 TeV]	(315, 397, 500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989, 3489) GeV
$m_{\tilde{g}}$ [33 TeV]	(500, 629, 792, 997, 1255, 1580, 1989, 2504, 3152, 3968, 4968, 5968, 6968) GeV
$m_{\tilde{g}}$ [100 TeV]	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 5012, 6310, 7944, 9944, 11944, 13944, 15944) GeV
$m_{\tilde{\chi}_1^0}$	1 GeV (0.2, 0.4, 0.6, 0.7, 0.8, 0.9) $\times m_{\tilde{g}}$ $m_{\tilde{g}} - (100 \text{ GeV}, 50 \text{ GeV}, 15 \text{ GeV}, 5 \text{ GeV})$

We find that including pileup does not significantly change the results of this study and present results below for only the no-pileup case. We discuss the effect of pile-up in more detail in Sec. 3.12.

3.1 Dominant Backgrounds

The background is dominated by $W/Z + \text{jets}$, with subdominant contributions from $t\bar{t}$ production. Single top events and W/Z events from vector boson fusion processes are also illustrated in several figures, and are negligible. In all cases, there are decay modes which lead to multi-jet signatures. The E_T^{miss} can come from a variety of sources, such as neutrinos, jets/leptons which are lost down the beam pipe, and energy smearing effects.

3.2 Analysis Strategy

The gluino-neutralino model with light flavor decays can be probed with an analysis inspired by the ATLAS analysis in [23]. After an event preselection, rectangular cuts on one or more variables are optimized at each point in parameter space to yield maximum signal significance. Specifically, we simultaneously scan a two-dimensional set of cuts on E_T^{miss} and H_T , where E_T^{miss} is the magnitude of the missing transverse momentum and H_T is defined as the scalar sum of jet p_T . In contrast, the discriminating variable used by ATLAS is m_{eff} , the scalar sum of H_T and E_T^{miss} . We require jets to have $p_T > 30$ GeV and $|\eta| < 3.5$. Electrons and muons are selected by requiring $p_T > 10$ GeV and $|\eta| < 2.6$.

In detail, our analysis strategy proceeds as follows:

PRESELECTION

- zero selected electrons or muons
- $E_T^{\text{miss}} > 100$ GeV

- at least 4 jets with $p_T > 60$ GeV

After preselection, a requirement is placed on $E_T^{\text{miss}}/\sqrt{H_T}$ to further reduce the QCD background, where the dominant source of E_T^{miss} is from jet mismeasurement. A cut on the leading jet p_T is applied to reduce backgrounds from hard ISR jets. Finally, a two dimensional scan over cuts on H_T and E_T^{miss} is performed to determine the maximum significance.

SEARCH STRATEGY: Simultaneous optimization over H_T and E_T^{miss}

- $E_T^{\text{miss}}/\sqrt{H_T} > 15$ GeV^{1/2}
- The leading jet p_T must satisfy $p_T^{\text{leading}} < 0.4 H_T$
- $E_T^{\text{miss}} > (E_T^{\text{miss}})_{\text{optimal}}$
- $H_T > (H_T)_{\text{optimal}}$

The 14, 33, and 100 TeV analyses all use the same set of fixed cuts, differing only in the optimization over $(E_T^{\text{miss}})_{\text{optimal}}$ and $(H_T)_{\text{optimal}}$. In practice, scaling the $E_T^{\text{miss}}/\sqrt{H_T}$ cut with CM energy may be desirable to reduce QCD background, and we have verified that this has no effect on the efficiencies for the signal and dominant backgrounds for the models under study.

Note that this search yields some power to discover these models in the difficult region of parameter space where the neutralino is degenerate with the gluino. Section 4 will provide the results of a search that is specifically targeted for this region of parameter space.

3.3 Analysis: 14 TeV

In Fig. 2 we show histograms of E_T^{miss} [left] and H_T [right] for signal and background at $\sqrt{s} = 14$ TeV after applying the preselection cuts listed in Sec. 3.2. Because the tails of the signal and background distributions have a similar slope, the optimization procedure generally leads to cuts near the bulk of the signal distribution. We find that the searches are systematics limited when the optimal cuts are applied (see Sec. 3.11 below for a detailed discussion).

Using the search strategy discussed above in Sec. 3.2, it is possible to explore the potential reach for the gluino-neutralino model at the 14 TeV LHC. Table 1 gives a few example of the number of events that result from this cut flow for background and three example signal points: $m_{\tilde{g}} = 500, 1255, \text{ and } 2489$ GeV with $m_{\tilde{\chi}_1^0} = 1$ GeV. Each choice of the E_T^{miss} and H_T cuts given in Table 1 corresponds to the optimal cut for one of the given signal points. The hardness of the cut increases with the mass of the gluino. Note that for 14 TeV proton collisions, the V +jets background dominates over the events from $t\bar{t}$. From this table, it is possible to infer that 500 GeV and 1255 GeV gluinos could be easily discovered while the 2489 GeV would only yield a few σ hint using the full power of the high luminosity LHC.

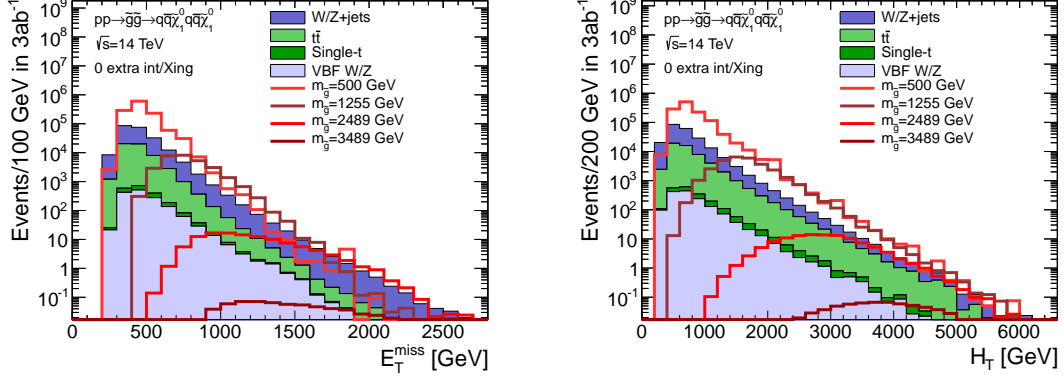


Figure 2: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of guino-neutralino models with light flavor decays at the 14 TeV LHC. The neutralino mass is 1 GeV for all signal models.

Cut				$m_{\tilde{g}}$ [GeV]		
	V+jets	$t\bar{t}$	Total BG	500	1255	2489
Preselection	2.07×10^7	2.47×10^7	4.54×10^7	3.08×10^7	1.03×10^5	173
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.45×10^5	1.20×10^5	5.65×10^5	1.34×10^6	3.14×10^4	95
$p_T^{\text{leading}} < 0.4 \times H_T$	1.69×10^5	5.16×10^4	2.21×10^5	7.62×10^5	1.68×10^4	52.9
$E_T^{\text{miss}} > 450 \text{ GeV}$ $H_T > 800 \text{ GeV}$	4.73×10^4	1.84×10^4	6.57×10^4	5.57×10^5	2.98×10^4	115
$E_T^{\text{miss}} > 800 \text{ GeV}$ $H_T > 1650 \text{ GeV}$	1.22×10^3	554	1.78×10^3	1.14×10^4	9.36×10^3	110
$E_T^{\text{miss}} > 1050 \text{ GeV}$ $H_T > 2600 \text{ GeV}$	55.5	30.1	85.6	297	288	57.2

Table 1: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected guino masses for the guino-neutralino model with light flavor decays. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each guino mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

3.4 Results: 14 TeV

The 5σ discovery [top] and 95% CL limits [bottom] for the guino-neutralino model are shown in Fig. 3. The left [right] panel assumes 300 fb^{-1} [3000 fb^{-1}] of integrated luminosity. The signal and background yields after optimized cuts are provided as inputs to a RooStats routine to calculate 95% CL exclusion intervals using the CL_s method along with the expected signal p_0 values. A 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematics are outlined in the appendix.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of gluino mass which would yield 10 events at 300 fb^{-1} (3000 fb^{-1}) is 2.8 (3.3) TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 14 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here, the 14 TeV 300 fb^{-1} limit with massless neutralinos is projected to be at a gluino mass of 2.3 TeV (corresponding to 110 events), while the 14 TeV 3000 fb^{-1} limit is projected to be at 2.7 TeV (corresponding to 175 events). Furthermore, the 14 TeV LHC with 3000 fb^{-1} could discover a gluino as heavy as 2.3 TeV if the neutralino is massless, while for $m_{\tilde{\chi}_1^0} \gtrsim 500 \text{ GeV}$ the gluino mass reach rapidly diminishes.

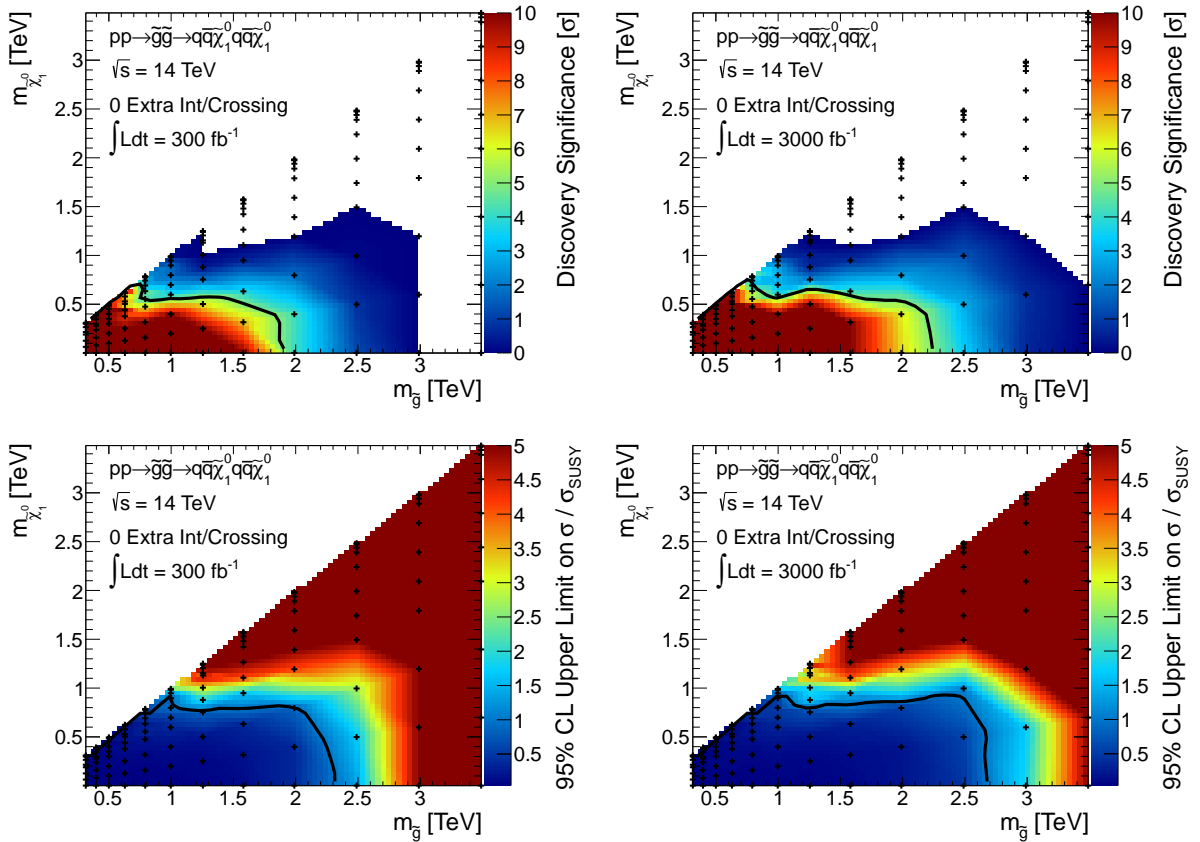


Figure 3: Results at 14 TeV for the gluino-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The top [bottom] row shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 300 fb^{-1} [left] and 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed and pileup is not included. The black crosses mark the simulated models.

3.5 Analysis: 33 TeV

In Fig. 4 we show histograms of E_T^{miss} [left] and H_T [right] for signal and background at $\sqrt{s} = 33$ TeV after applying the preselection cuts listed in Sec. 3.2. Because the tails of the signal and background distributions have a similar slope, the optimization procedure generally leads to cuts near the bulk of the signal distribution. Moving to a higher center-of-mass energy allows for harder cuts to be placed, which in turn implies fewer background events survive the requirements. At 33 TeV, we find that the searches are systematics limited when the optimal cuts are applied (see Sec. 3.11 below for a detailed discussion).

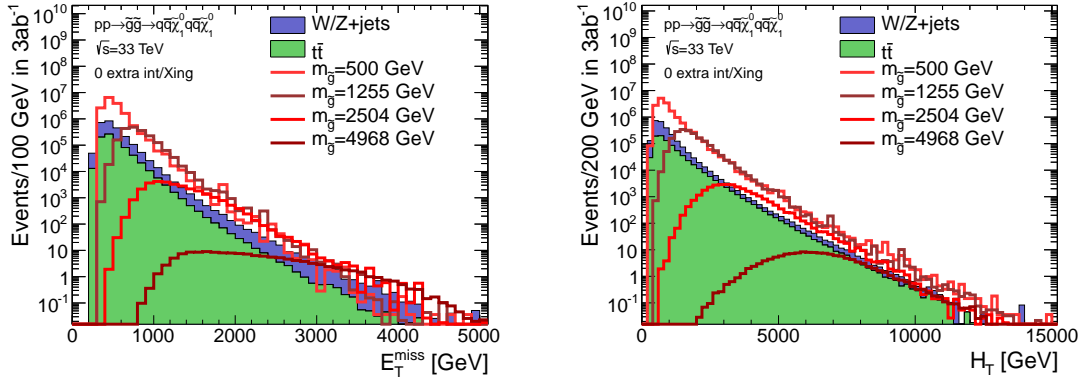


Figure 4: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of gluino-neutralino models with light flavor decays at a 33 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Using the search strategy discussed above in Sec. 3.2, it is possible to explore the potential reach for the gluino-neutralino model at a 33 TeV proton collider. Table 2 gives a few example of the number of events that result from this cut flow for background and three example signal points: $m_{\tilde{g}} = 1255, 3152, \text{ and } 4968$ GeV with $m_{\tilde{\chi}_1^0} = 1$ GeV. Each choice of the E_T^{miss} and H_T cuts given in Table 2 corresponds to the optimal cuts for one of the given signal points. The hardness of the cut increases with the mass of the gluino. It is clear that the ratio of $t\bar{t}$ to V +jets background is growing with regards to the 14 TeV search; this is due to the higher probability for gluon scattering as \sqrt{s} increases. It would likely be advantageous to veto b -tagged jets to further reduce the background from top quarks, and similarly to veto τ -tagged jets to further reduce W/Z +jets. From this table, it is possible to infer that gluinos as heavy as ~ 5 TeV could be discovered at a 33 TeV collider. H_T cuts as hard as 5 TeV are required to extract the most information from this data set.

Cut	V+jets	$t\bar{t}$	Total BG	$m_{\tilde{g}}$ [GeV]		
				1255	3152	4968
Preselection	1.55×10^8	2.86×10^8	4.42×10^8	1.22×10^7	1.89×10^4	316
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.50×10^6	1.93×10^6	6.44×10^6	3.50×10^6	1.13×10^4	229
$p_T^{\text{leading}} < 0.4 \times H_T$	1.70×10^6	8.02×10^5	2.50×10^6	1.94×10^6	6.94×10^3	139
$E_T^{\text{miss}} > 900 \text{ GeV}$ $H_T > 1900 \text{ GeV}$	4.06×10^4	5.65×10^4	9.71×10^4	8.36×10^5	6.93×10^3	139
$E_T^{\text{miss}} > 2100 \text{ GeV}$ $H_T > 3800 \text{ GeV}$	127	103	230	1.44×10^3	1.10×10^3	78.5
$E_T^{\text{miss}} > 2750 \text{ GeV}$ $H_T > 5150 \text{ GeV}$	10	7.8	17.8	53.1	91.2	33.6

Table 2: Number of expected events for $\sqrt{s} = 33 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected gluino masses for the gluino-neutralino model with light flavor decays. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each gluino mass column the entry in the row corresponding to the ‘‘optimal’’ cuts is marked in red.

3.6 Results: 33 TeV

The 5σ discovery [left] and 95% C.L. limits [right] for the gluino-neutralino model are shown in Fig. 5, assuming 3000 fb^{-1} of integrated luminosity. 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematic are outlined in the appendix. Pileup is not included; a demonstration that pileup will not significantly change these results is given in Sec. 3.12 below.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of gluino mass which would yield 10 events at 3000 fb^{-1} is 6.7 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 33 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 33 TeV 3000 fb^{-1} limit with massless neutralinos is projected to be 5.8 TeV (corresponding to 61 events). Furthermore, the 33 TeV proton collider with 3000 fb^{-1} could discover a gluino as heavy as 4.8 TeV if the neutralino is massless, while for $m_{\tilde{\chi}_1^0} \gtrsim 1 \text{ TeV}$ the gluino mass reach rapidly diminishes.

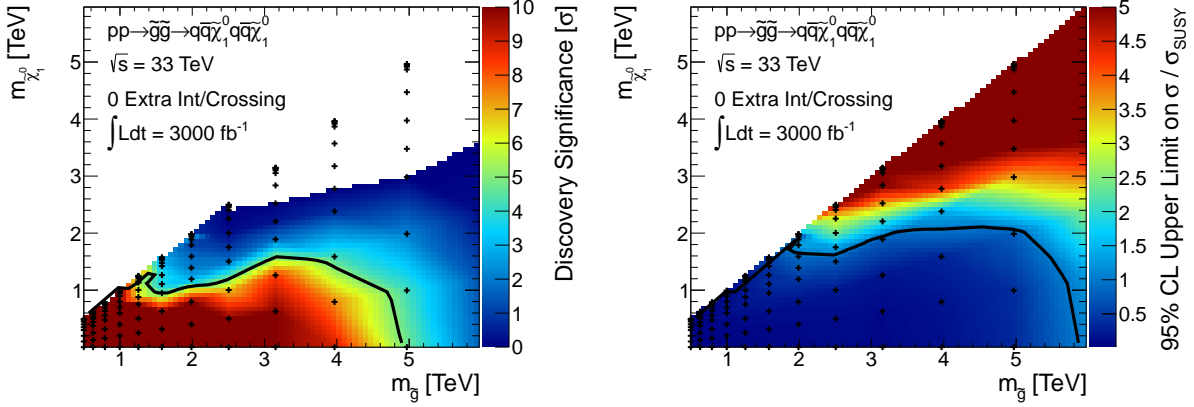


Figure 5: Results at 33 TeV for the gluino-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} . A 20% systematic uncertainty is assumed and pileup is not included. The black crosses mark the simulated models.

3.7 Analysis: 100 TeV

In Fig. 6 we show histograms of E_T^{miss} [left] and H_T [right] for signal and background at $\sqrt{s} = 100 \text{ TeV}$ after applying the preselection cuts listed in Sec. 3.2. Because the tails of the signal and background distributions have a similar slope, the optimization procedure generally leads to cuts near the bulk of the signal distribution. Moving to a higher center-of-mass energy allows for harder cuts to be placed, which in turn implies fewer background events survive the requirements. For example, we find that the signal efficiencies at the high gluino mass edge of our limits are several times larger at 100 TeV than at 14 TeV. We find that the searches are only barely systematic limited when the optimal cuts are applied (see Sec. 3.11 below for a detailed discussion).

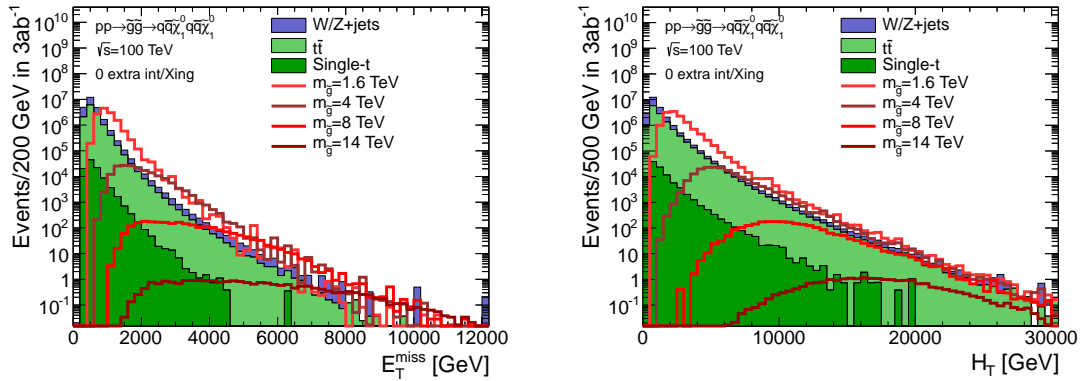


Figure 6: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of gluino-neutralino models with light flavor decays at a 100 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut	V+jets	$t\bar{t}$	Total BG	$m_{\tilde{g}}$ [GeV]		
				5012	9944	13944
Preselection	1.64×10^9	3.33×10^9	4.97×10^9	1.12×10^5	876	43.4
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	3.59×10^7	3.31×10^7	6.90×10^7	7.99×10^4	740	38.8
$p_T^{\text{leading}} < 0.4 \times H_T$	1.19×10^7	1.25×10^7	2.44×10^7	4.87×10^4	443	22.7
$E_T^{\text{miss}} > 5150 \text{ GeV}$ $H_T > 9550 \text{ GeV}$	21.6	33.1	54.8	216	91.6	10.7
$E_T^{\text{miss}} > 5530 \text{ GeV}$ $H_T > 9750 \text{ GeV}$	12	18.9	30.9	136	67.4	9.2
$E_T^{\text{miss}} > 6150 \text{ GeV}$ $H_T > 11700 \text{ GeV}$	4.1	6.3	10.4	33.6	29.6	6.8

Table 3: Number of expected events for $\sqrt{s} = 100 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected gluino masses for the gluino-neutralino model with light flavor decays. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each gluino mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

Using the search strategy discussed above in Sec. 3.2, it is possible to explore the potential reach for the gluino-neutralino model at a 100 TeV proton collider. Table 3 gives a few example of the number of events that result from this cut flow for background and three example signal points: $m_{\tilde{g}} = 5012, 9944,$ and 13944 GeV with $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$. Each choice of the E_T^{miss} and H_T cuts given in Table 3 corresponds to the optimal cuts for one of the given signal points. The hardness of the cut increases with the mass of the gluino. It is clear that the ratio of $t\bar{t}$ to V+jets background is growing with regards to the 14 and 33 TeV searches; this is due to the higher probability for gluon scattering as \sqrt{s} increases. In this analysis it would certainly be advantageous to veto b -tagged jets to further reduce the background from top quarks. From this table, it is possible to infer that gluinos as heavy as $\sim 10 \text{ TeV}$ could be discovered at a 100 TeV collider. H_T cuts as hard as 12 TeV are required to extract the most information from this data set.

3.8 Results: 100 TeV

The 5σ discovery [left] and 95% CL limits [right] for the gluino-neutralino model are shown in Fig. 7, assuming 3000 fb^{-1} of integrated luminosity. 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematic are outlined in the appendix. Pileup is not included; a demonstration that pileup will not significantly change these results is given in Sec. 3.12 below.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of gluino mass which would yield 10 events at 3000 fb^{-1} is 16.1 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 100 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 100 TeV 3000 fb^{-1} limit with massless neutralinos is projected to be 13.5 TeV (corresponding to 60 events). Furthermore, the 100 TeV proton collider with 3000 fb^{-1} could discover a gluino as heavy as 11 TeV if the neutralino is massless, while for $m_{\tilde{\chi}_1^0} \gtrsim 1 \text{ TeV}$ the gluino mass reach rapidly diminishes.

The next section provides a comparison of the impact that the four Snowmass collider scenarios can have on the parameter space of this model.

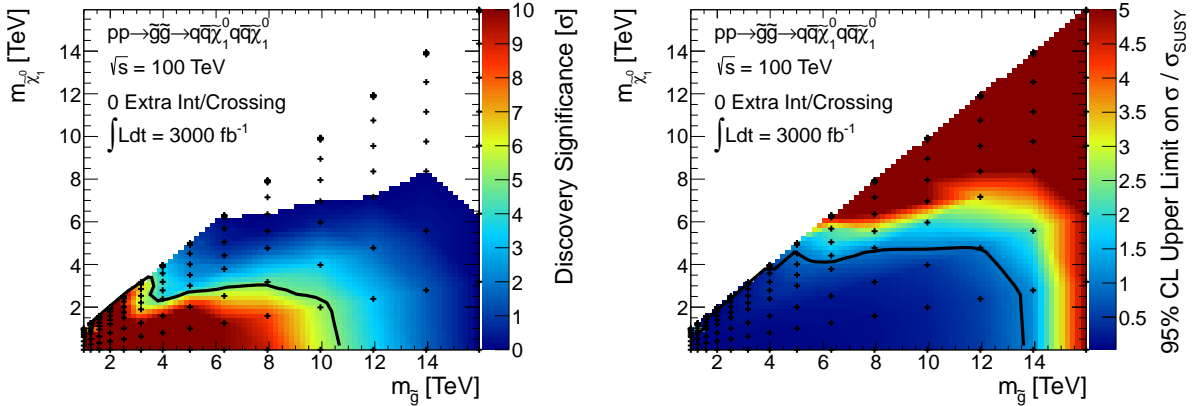


Figure 7: Results at 100 TeV for the gluino-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} . A 20% systematic uncertainty is assumed and pileup is not included. The black crosses mark the simulated models.

3.9 Comparing Colliders

The multi-jet plus E_T^{miss} signature of the gluino-neutralino model with light flavor decays provides a useful study with which to compare the potential impact of different proton colliders. Figure 8 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the full data set assumed for 33 and 100 TeV. At 14 TeV, the factor of 10 increase in luminosity leads to a modest increase by 350 GeV in the gluino limits. The smallness of this increase is due to the rapidly falling cross section. Furthermore, because the signal regions are not background-free, the improvement in cross section-limit does not match the factor of 10 increase in luminosity; the shift in mass reach corresponds to only roughly a factor of five in the gluino production cross-section. For lighter gluinos, there is no improvement to the range of accessible neutralino masses. This is because the systematic uncertainty dominates in the signal regions for these models except in the high gluino mass tail.

In contrast, increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space, since now much heavier gluinos can be produced without relying on the tails of parton distributions to supply the necessary energy. Figure 8 makes a compelling case for investing in future proton colliders which can operate at these high energies.

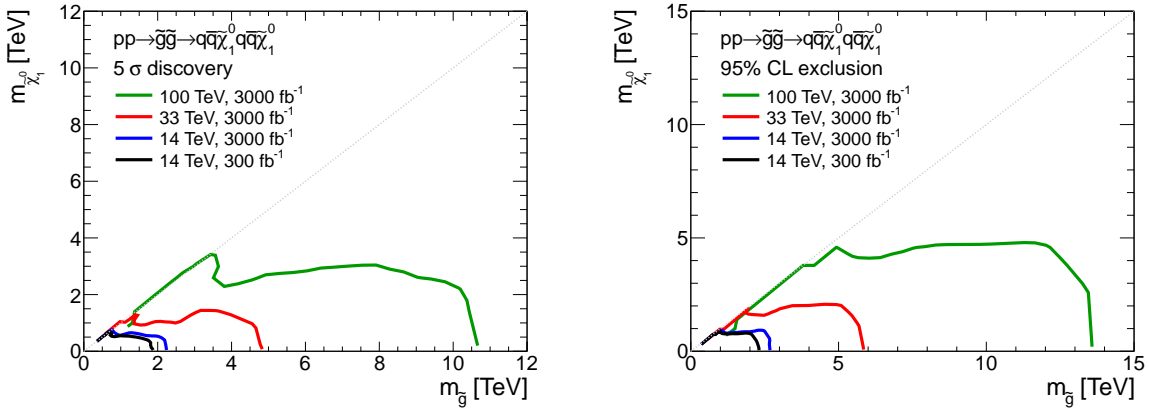


Figure 8: Results for the gluino-neutralino model with light flavor decays. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is not included.

Figure 9 provides a comparison of the optimal cut at the different colliders that results from applying the analysis discussed in Sec. 3.2 as a function of gluino mass (assuming a 1 GeV neutralino). It is interesting to note that the slope of the H_T cut is larger than that for the E_T^{miss} cut. The search is taking advantage of the tremendous energy that is imparted to jets when these heavy gluinos decay. Furthermore, it is also interesting that the H_T cuts track very closely between machines (until mass of the gluino becomes so heavy that a given collider can no longer produce them in appreciable quantities), while the E_T^{miss} cuts begin to flatten out for very high mass gluinos. This can be understood by inspecting the histograms provided in Figs. 2, 4, and 6. The signal and

background distributions have different shapes for E_T^{miss} , while the H_T of signal and background tend to fall off with a similar slope in the tails. The cut on H_T therefore simply scales with the gluino mass, while the optimization for E_T^{miss} is more subtle. Finally, it is worth noting that due to the increase of the ratio of $t\bar{t}$ to V +jets events as \sqrt{s} increases, it is likely worth exploring the addition of a veto on b -tagged jets for the higher energy colliders.

It is clear from these results that all four collider scenarios can have tremendous impact on our understanding of the gluino-neutralino parameter space. The next sections are devoted to exploring various details related to these conclusions.

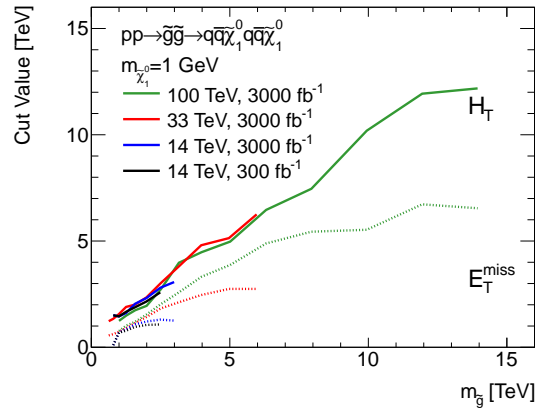


Figure 9: The optimal H_T [solid] and E_T^{miss} [dashed] cuts for the gluino-neutralino model with light flavor decays as a function of gluino mass (assuming a 1 GeV neutralino) for the four collider scenarios studied here.

3.10 Comparing Optimization Strategies

A two-dimensional optimization over cuts on E_T^{miss} and H_T is employed here. This is the most significant difference between our strategy and the cuts used in the ATLAS analysis [23], which only optimizes over $m_{\text{eff}} \equiv H_T + E_T^{\text{miss}}$. The purpose of this section is to quantify the gain in significance from performing the two-dimensional optimization. In Fig. 10, we plot the results of our mockup of the ATLAS one-dimensional scan along with the contours derived in this study by optimizing cuts over both E_T^{miss} and H_T . The two-dimensional strategy improves the reach for several regions of the signal grid. Therefore, we also use the two-dimensional strategy to study the squark-neutralino and gluino-squark signal models in the following sections.

It is interesting to compare the scaling of the optimal cut as a function of the gluino mass for the two optimization strategies. The optimal cuts which result for the m_{eff} only [black, dotted] strategy along with the E_T^{miss} [blue, solid] and H_T [red, solid] are plotted in Fig. 11. Also shown is $E_T^{\text{miss}} + H_T$ [grey, solid], which allows a direct comparison between the one-dimensional and two-dimensional optimizations. Above ~ 1 TeV, the cuts all increase monotonically as a function of $m_{\tilde{g}}$. The single cut on m_{eff} tends to be harder than the sum of E_T^{miss} and H_T . The two-dimensional optimization can cover a wider parameter space of cuts, which allows it to take advantage of more complete information about the shape of the distribution. This allows it to perform as well or better with a slightly softer effective m_{eff} cut.

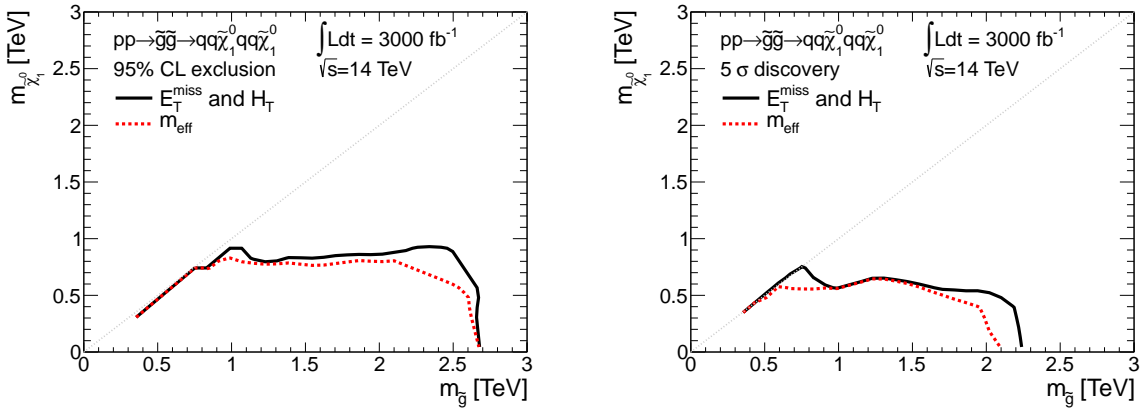


Figure 10: The 5σ discovery contours [right] and expected 95% CL exclusion limits [left] for the one-dimensional m_{eff} [red, dotted], and two-dimensional E_T^{miss} and H_T [black, solid] optimization strategies.

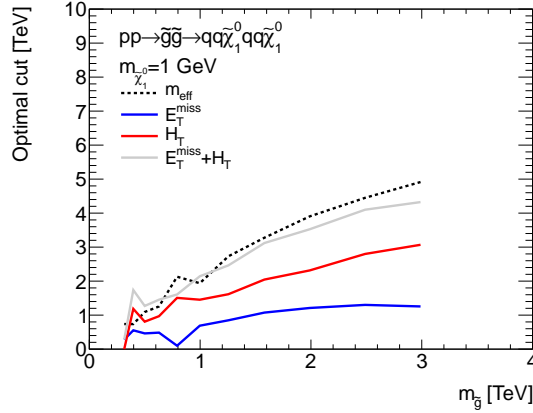


Figure 11: Optimal cuts on m_{eff} [black, dotted], E_T^{miss} [blue, solid], and H_T [red, solid] for the 14 TeV LHC with 3000 fb^{-1} . The mass of the neutralino is 1 GeV. Also plotted is $E_T^{\text{miss}} + H_T$ [grey, solid] for the two-dimensional optimization, which allows direct comparison with m_{eff} from the one-dimensional strategy.

3.11 Impact of Systematic Uncertainties

A systematic uncertainty of 20% was assumed for the background normalization in the results we have presented. It is likely that the experiments will significantly reduce these uncertainties with larger datasets and an improved understanding of their detectors; it is also possible that this value is aggressive given our current knowledge (or lack thereof) of physics at higher \sqrt{s} . It is therefore interesting to understand the impact of different systematic uncertainties on the discovery reach.

Figure 12 shows the impact from a change in the systematic uncertainty for gluino discovery at 14 TeV with 3000 fb^{-1} . Varying the systematic background uncertainty from 30% to 5%, the discovery reach increases by roughly 600 GeV in $m_{\tilde{g}}$ and the coverage in $m_{\tilde{\chi}_1^0}$ direction is roughly doubled. The impact of systematic uncertainties on the 95% exclusion limits is less dramatic. Note that in this analysis we reoptimized the E_T^{miss} and H_T cuts for each choice of systematic uncertainty. As the LHC continues to run, the improvements in our understanding of the relevant backgrounds will be useful in extending the physics potential of the machine.

3.12 Impact of Pileup

In order to reach an integrated luminosity of 3000 fb^{-1} , the instantaneous luminosity at the LHC will need to increase significantly with respect to previous runs. There will be a corresponding increase in the number of pile-up events per bunch crossing. It is crucial to understand the impact this environment will have on the expected reach using this data set.

To study this in detail, we repeated the full analysis with signal and background samples that include 140 additional minimum-bias interactions. The Delphes based Snowmass simulation includes a pileup suppression algorithm that primarily impacts the E_T^{miss} resolution [9]. Figure 13 shows the E_T^{miss} [left] and H_T [right] distributions with and without pileup. The samples with pileup follow the distributions without pileup closely, especially in the search regions. We also

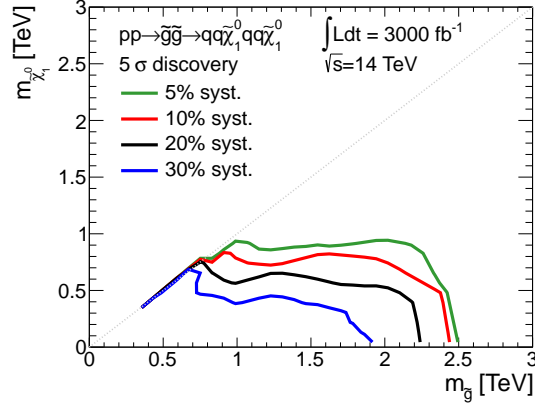


Figure 12: Expected 5σ discovery contours for the $\sqrt{s} = 14$ TeV LHC with 3000 fb^{-1} . The different curves correspond to various assumptions for the systematic uncertainty on the background: 5% [green], 10% [red], 20% [black], and 30% [blue].

observe that the the largest effects of pileup is at at low values of E_T^{miss} -significance, and are therefore suppressed by the requirement that $E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$.

The impact of pileup on the discovery significance [left] and limits [right] are shown in Fig. 14. Given that the H_T and E_T^{miss} distributions are effectively unchanged, it is not surprising that the results are very similar with and without pileup. The contours with and without pileup each lie within the other's 1σ confidence interval, and we find no evidence that this reflects anything other than statistical fluctuations for a few signal points. We can safely assume that pileup has a small impact on this analysis.

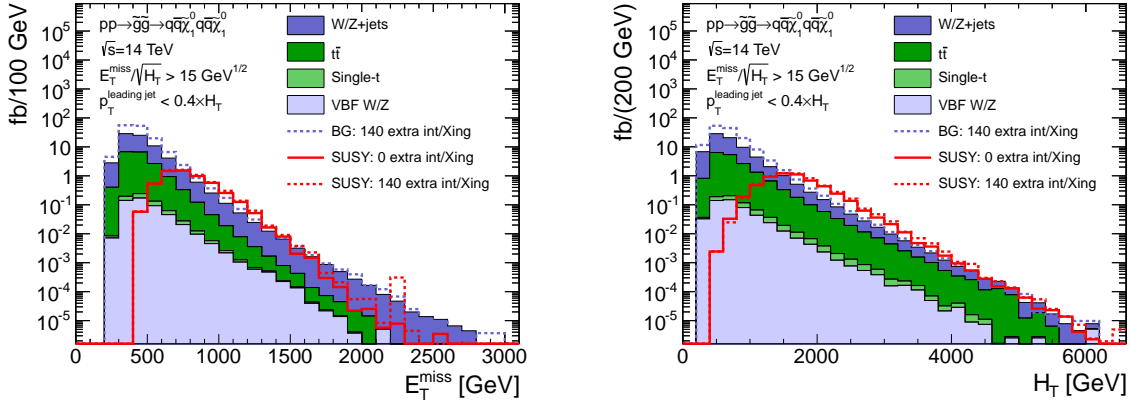


Figure 13: Signal and background E_T^{miss} [left] and H_T [right] distributions at the 14 TeV LHC for events with no pileup [solid] and the sum of backgrounds for events with 140 additional pp interactions per bunch crossing [dashed]. Additional interactions increase the background rates at low E_T^{miss} , but have little impact on the final analysis due to the tight E_T^{miss} cuts.

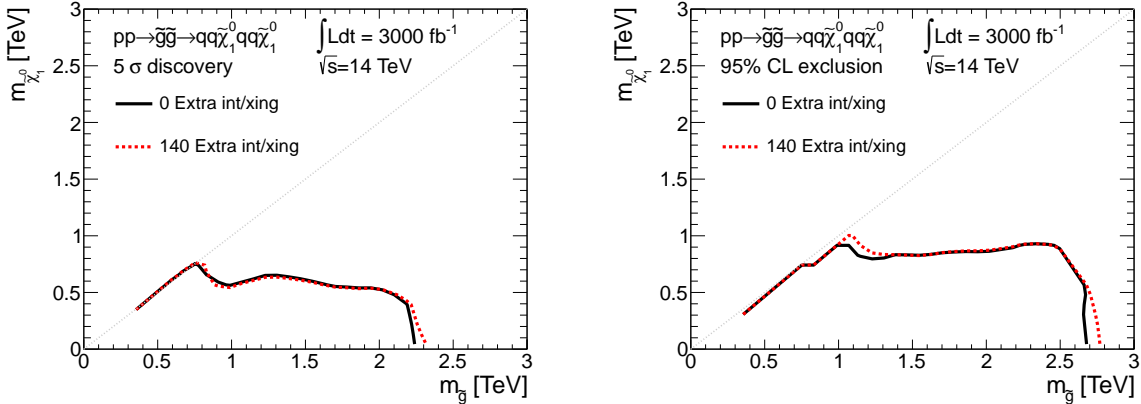


Figure 14: Discovery contours [right] and expected limits [left] for the analyses performed with [red, dotted] and without [black, solid] pileup at the 14 TeV LHC with 3000 fb^{-1} integrated luminosity.

4 The Compressed Gluino-Neutralino Model with Light Flavor Decays

This section is devoted to analyses which target the compressed region of parameter space for the gluino-neutralino with light-flavor decays Simplified Model discussed in Sec. 3, where

$$m_{\tilde{g}} - m_{\tilde{\chi}_1^0} \equiv \Delta m \ll m_{\tilde{g}}. \quad (1)$$

For models with this spectrum, the search strategy of Sec. 3 does not provide the optimal reach. With compressed spectra the gluino decays only generate soft partons, thereby suppressing the H_T signals and reducing the efficiency for passing the 4 jet requirement. A more effective strategy for compressed spectra searches relies instead on events with hard initial state radiation (ISR) jets to discriminate signal from background.

In this study, we will apply two different search strategies that are optimized for this kinematic configuration and will choose the one which leads to the most stringent bound on the production cross section for each point in parameter space. Some of the cuts chosen below are inspired by recent public results from ATLAS [29] and CMS [30] on monojet searches. For recent work on the compressed region of parameter space see [31], and for a discussion of the theoretical uncertainties see [32].

4.1 Dominant Backgrounds

The dominant background is the production of a Z boson in association with jets, where the Z boson decays into a pair of neutrinos ($Z \rightarrow \nu\nu$), leading to events with jets and a significant amount of missing transverse energy. Subleading backgrounds are the production of a W boson which decays leptonically ($W \rightarrow \ell\nu$) in association with jets, where the charged lepton is not reconstructed properly. Finally, when considering events with a significant number of jets, $t\bar{t}$ production in the fully hadronic decay channel ($t \rightarrow bqq'$) can be relevant.

4.2 Two Analysis Strategies: 14 TeV

This section is devoted to a description of the two analysis strategies employed to search for the compressed regions of the gluino-neutralino parameter space. Applications to the 14 TeV LHC will be presented for illustration; 33 and 100 TeV will be discussed below. The following preselections are common to both approaches.

PRESELECTION

- lepton veto: any event with an electron or muon with $p_T > 10$ GeV and $|\eta| < 2.5$ is discarded
- jets are required to have $p_T > 30$ GeV and $|\eta| < 4.5$
- the leading jet must be reconstructed within $|\eta| < 2.5$
- $E_T^{\text{miss}} > 100$ GeV

The first set of cuts implemented in this analysis is based on the public monojet search from the ATLAS collaboration [29].

SEARCH STRATEGY 1: Leading jet based selection

- at most 2 jets
- leading jet must have $p_T > (\text{leading jet } p_T)_{\text{optimal}}$ and $|\eta| < 2.0$
- second jet is allowed if $\Delta\varphi(j_2, E_T^{\text{miss}}) > 0.5$
- $E_T^{\text{miss}} > (E_T^{\text{miss}})_{\text{optimal}}$

where both $(E_T^{\text{miss}})_{\text{optimal}}$ and $(\text{leading jet } p_T)_{\text{optimal}}$ are determined simultaneously by taking the values in the range 1 – 10 TeV that yields the strongest exclusion. Figure 15 shows the distribution of the leading jet p_T and illustrates the ability to distinguish signal from background using this variable.

Table 4 shows the expected signal and background yields for the signal region with cuts on the leading jet $p_T > (500 \text{ GeV}, 1 \text{ TeV}, 2 \text{ TeV})$ and $E_T^{\text{miss}} > (500 \text{ GeV}, 1 \text{ TeV}, 2 \text{ TeV})$. This analysis is expected to be especially powerful for very small mass differences, when no jets except for a hard ISR jet can be reconstructed.

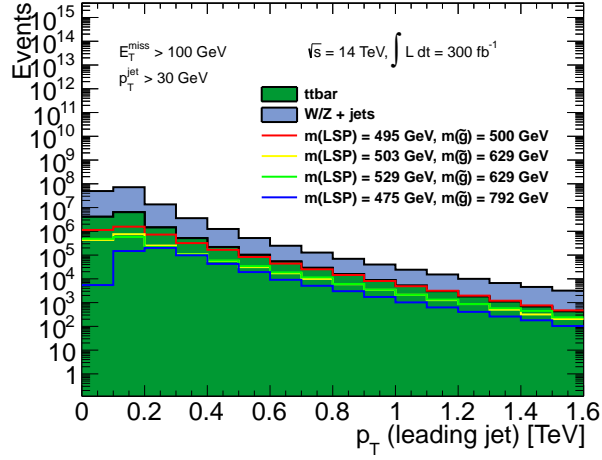


Figure 15: Histogram of the leading jet p_T for signal and background at the 14 TeV LHC with 300 fb^{-1} after the preselection for a range of gluino and neutralino masses in the compressed region.

Cut	V+jets	$t\bar{t}$	Total BG	$(m_{\tilde{g}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(500, 495)	(792, 787)	(997, 992)
Preselection	1.3×10^9	1.2×10^8	1.4×10^9	4.0×10^7	2.6×10^6	6.0×10^5
$E_T^{\text{miss}} > 120 \text{ GeV}, \leq 2 \text{ jets}$	6.0×10^8	7.0×10^6	6.1×10^8	1.9×10^7	1.4×10^6	2.8×10^5
$p_T(j_1) > 120 \text{ GeV}, \eta(j_1) < 2.0$	3.2×10^8	3.2×10^6	3.6×10^8	1.2×10^7	9.2×10^5	1.9×10^5
$\Delta\varphi(j_2, E_T^{\text{miss}}) > 0.5$	2.4×10^8	1.6×10^6	2.4×10^8	8.0×10^6	6.4×10^5	1.3×10^5
$E_T^{\text{miss}} > 500 \text{ GeV}$ $p_T(j_1) > 500 \text{ GeV}$	4.5×10^5	1.7×10^3	4.5×10^5	4.5×10^5	5.9×10^4	1.6×10^4
$E_T^{\text{miss}} > 1 \text{ TeV}$ $p_T(j_1) > 1 \text{ TeV}$	9.4×10^3	13	9.4×10^3	1.9×10^4	4.4×10^3	1.6×10^3
$E_T^{\text{miss}} > 2 \text{ TeV}$ $p_T(j_1) > 2 \text{ TeV}$	49	0	49	87	38	18

Table 4: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ and 3000 fb^{-1} for the background processes and three gluino-neutralino models in the compressed region. The leading jet p_T based selection with various cuts is applied. Three choices of cuts are provided for illustration.

SEARCH STRATEGY 2: E_T^{miss} based selection without jet veto

- leading jet with $p_T > 110 \text{ GeV}$ and $|\eta| < 2.4$
- $E_T^{\text{miss}} > (E_T^{\text{miss}})_{\text{optimal}}$

with E_T^{miss} varied in the range (1, 10) TeV. No requirement is placed on a maximum number of jets. Figure 16 shows that already for signal scenarios with small mass differences it is likely to reconstruct more than one jet in the event. Note that for higher jet multiplicities the production of top quark pairs in the fully hadronic decay mode starts to dominate over $W/Z + \text{jets}$ production.

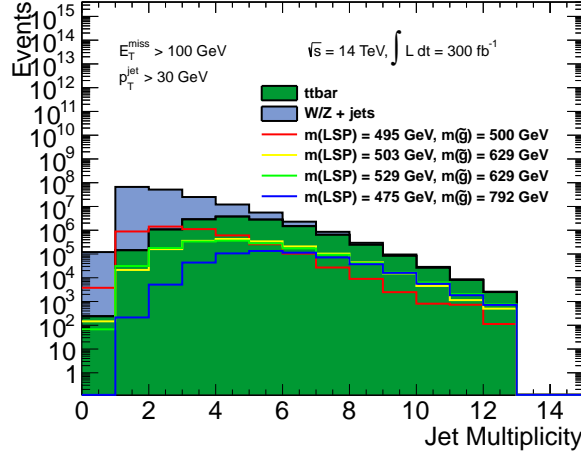


Figure 16: Histogram of jet multiplicities for signal and background at the 14 TeV LHC with 300 fb^{-1} after the preselection for a range of gluino and neutralino masses in the compressed region.

Table 5 shows the expected number of signal and background for three choices of the E_T^{miss} cut. Compared to the previous selection one can see that a significantly larger number of events are selected, especially for the larger mass differences. In addition, for this selection top pair production can make a non-negligible contribution to the total number of background events.

Cut	$V+\text{jets}$	$t\bar{t}$	Total BG	$(m_{\tilde{g}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(500, 495)	(792, 787)	(997, 992)
Preselection	1.3×10^9	1.2×10^8	1.4×10^9	4.0×10^7	2.6×10^6	6.0×10^5
$p_T(j_1) > 110 \text{ GeV}, \eta(j_1) < 2.4$	7.9×10^8	8.1×10^7	8.7×10^8	3.0×10^7	2.1×10^6	4.8×10^5
$E_T^{\text{miss}} > 500 \text{ GeV}$	2.1×10^6	1.5×10^5	2.3×10^6	2.4×10^6	2.9×10^5	7.5×10^4
$E_T^{\text{miss}} > 1 \text{ TeV}$	4.9×10^4	2.1×10^3	5.2×10^4	1.3×10^5	2.5×10^4	8.1×10^3
$E_T^{\text{miss}} > 2 \text{ TeV}$	278	3	282	900	328	133

Table 5: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ and 3000 fb^{-1} for the background processes and selected signal processes. The selection without a veto on additional jets with cuts on E_T^{miss} is applied. Three choices of cuts are provided for illustration.

4.3 Results: 14 TeV

We now apply the compressed analysis to the gluino-neutralino model. Figure 17 shows which of the two selection strategies lead to the best discovery reach in the $m_{\tilde{\chi}_1^0} - m_{\tilde{g}}$ plane. For lighter gluinos and very small values of Δm the leading jet based search dominates, while for higher masses and less compression the more inclusive E_T^{miss} based search leads to the strongest exclusion. Note that for the points with $m_{\tilde{g}} \gtrsim 2$ TeV neither analysis can exclude the model so that the choice is not particularly relevant.

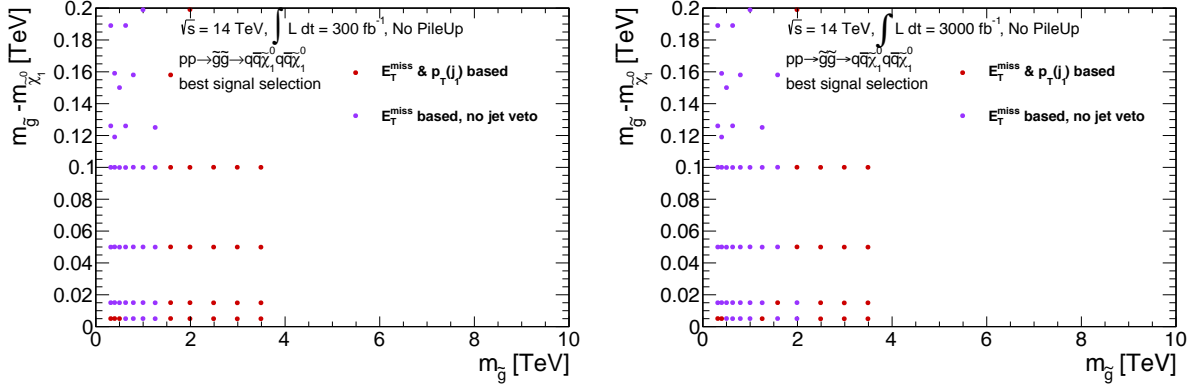


Figure 17: The choice of analysis that lead to the best discovery reach for a given point in parameter space for an integrated luminosity of 300 fb^{-1} [left] and 3000 fb^{-1} [right] at the 14 TeV LHC for the compressed region of the gluino-neutralino Simplified Model with light flavor decays. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based. For very high gluino masses, neither analysis can exclude the signal process.

The results for integrated luminosities of 300 fb^{-1} and 3000 fb^{-1} at the 14 TeV LHC are shown in Fig. 18. A 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematic are outlined in the appendix. Pile-up is neglected for these results; its impact is explored in Sec. 4.10 below.

With 300 fb^{-1} of data this search can exclude gluino masses of up to approximately 900 GeV for a mass difference of 5 GeV, with reduced reach for larger mass differences. The limits increase to around 1 TeV with a factor of 10 more data. This improves the reach near the degenerate limit by roughly 200 GeV compared to the H_T -based analysis described in Sec. 3; the H_T -based searches do not begin to set stronger limits until $\Delta \gtrsim 50$ GeV. The combined discovery reach is shown in the bottom row of Fig. 18. The discovery reach of this search is gluino masses up to 800 GeV near the degenerate limit. Unlike the exclusion reach, the discovery reach for this search is not a substantial improvement over the H_T -based analysis, even in the degenerate limit. This occurs because the signal efficiency using these searches is such that there are not enough events to reach 5σ confidence. Overall, it is clear that the 14 TeV LHC can have profound implications for models with compressed spectra.

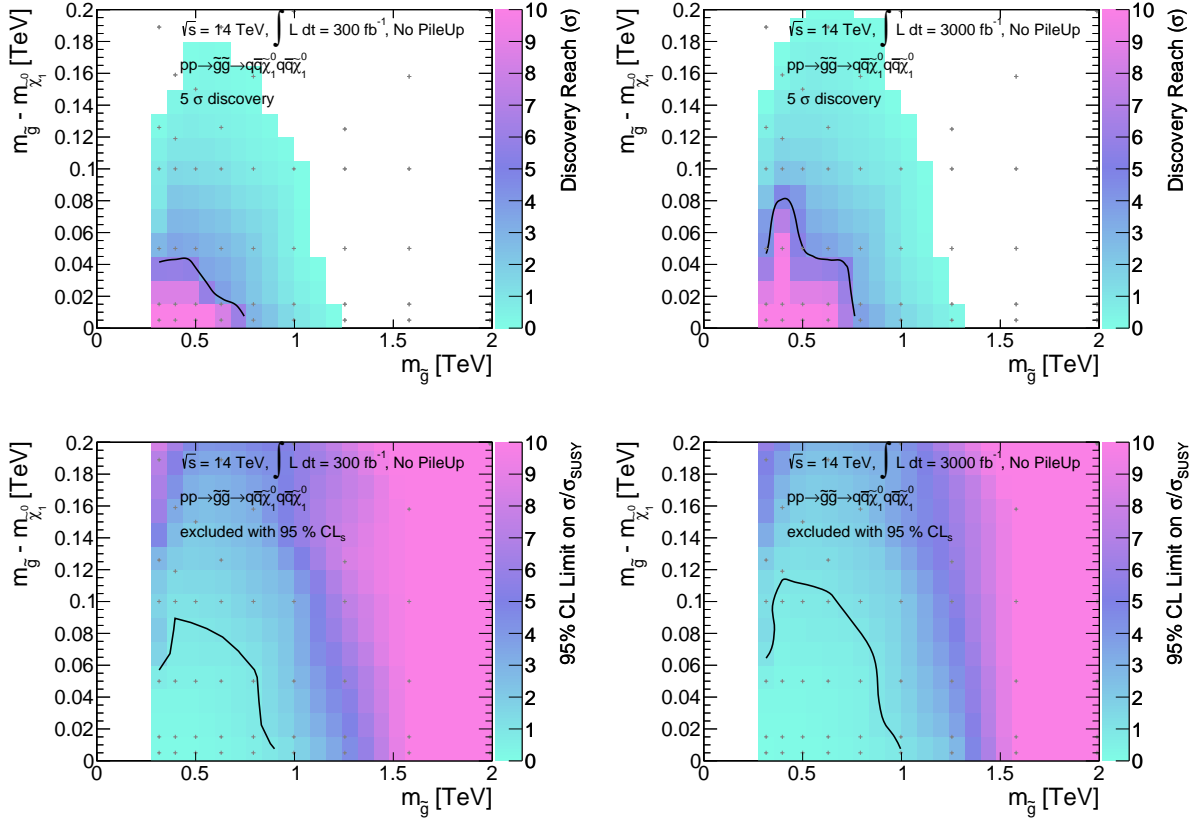


Figure 18: Results for the compressed gluino-neutralino model with light flavor decays at the 14 TeV LHC are given in the $m_{\tilde{g}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The top [bottom] row shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 300 fb^{-1} [left] and 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed for the background and pileup is not included.

4.4 Analysis: 33 TeV

This section is devoted to the details of the 33 TeV analysis in the compressed region of the gluino-neutralino model with light flavor decays. As the center-of-mass energy increases, the average p_T of an ISR jet would also increase. This implies that the probability for more than one ISR jets to pass the preselection cuts will be correspondingly higher, causing the E_T^{miss} -based search without additional jet veto to have the best acceptance of our search strategies. From Fig. 19, it is clear that this intuition holds; the E_T^{miss} based search gives the optimal significance for most of the parameter space studied here.

Figure 20 gives histograms of E_T^{miss} distribution for background and a variety of signal models. It is clear that a cut on E_T^{miss} can be used to distinguish signal from background. This can be seen quantitatively using Table 6, where the cut flows are given for background and three signal models.

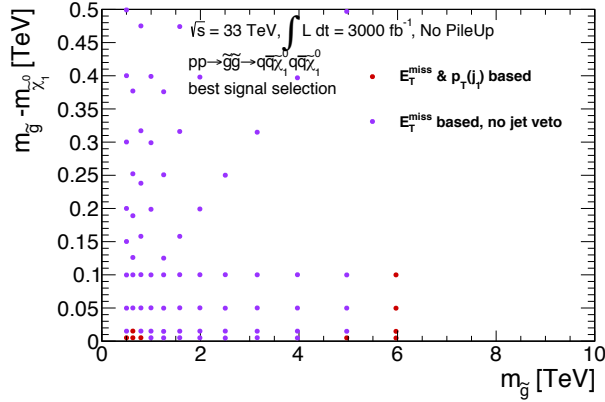


Figure 19: The choice of analysis that lead to the best discovery reach for a given point in parameter space for an integrated luminosity of 3000 fb^{-1} at a 33 TeV proton collider for the compressed region of the gluino-neutralino Simplified Model with light flavor decays. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based. For very high gluino masses, neither analyses can exclude the signal process.

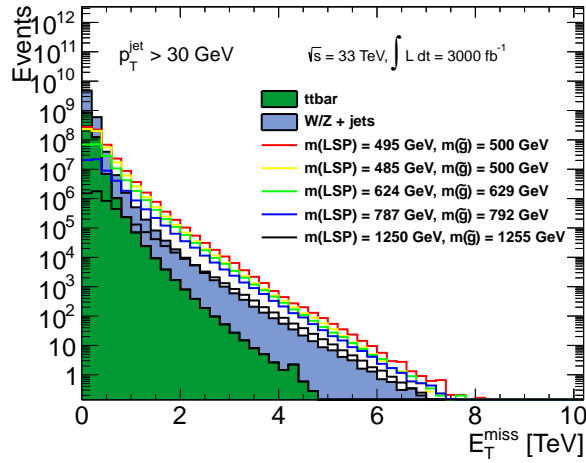


Figure 20: Histogram of E_T^{miss} for signal and background at a 33 TeV proton collider with 3000 fb^{-1} after the preselection for a range of gluino and neutralino masses in the compressed region.

Cut	V+jets	$t\bar{t}$	Total BG	$(m_{\tilde{g}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(797, 792)	(997, 992)	(1580, 1575)
Preselection	4.2×10^9	8.6×10^8	5.1×10^9	5.5×10^7	1.7×10^7	1.2×10^6
$p_T^{\text{leadjet}} > 110 \text{ GeV}, \eta^{\text{leadjet}} < 2.4$	2.6×10^9	6.5×10^8	3.3×10^9	4.8×10^7	1.5×10^7	1.1×10^6
$E_T^{\text{miss}} > 1 \text{ TeV}$	7.5×10^5	1.1×10^5	8.6×10^5	1.8×10^6	8.0×10^5	1.0×10^5
$E_T^{\text{miss}} > 3 \text{ TeV}$	1.5×10^3	62	1.5×10^3	6.1×10^3	4.0×10^3	1.1×10^3
$E_T^{\text{miss}} > 5 \text{ TeV}$	19	0	19	62	50	19

Table 6: Number of expected events for $\sqrt{s} = 33 \text{ TeV}$ and 3000 fb^{-1} for the background processes and selected signal processes. The selection without a veto on additional jets with cuts on E_T^{miss} is applied. Three choices of cuts are provided for illustration.

4.5 Results: 33 TeV

The 5σ discovery [left] and 95% C.L. limits [right] for the gluino-neutralino model are shown in Fig. 21, assuming 3000 fb^{-1} of integrated luminosity. 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematic are outlined in the appendix. Pileup is not included; a demonstration that pileup will not significantly change these results is given in Sec. 4.10 below.

For a 33 TeV proton collider with 3000 fb^{-1} of data, the exclusion reach for a mass difference of 5 GeV covers gluino masses of up to approximately 1.8 TeV, with reduced reach for larger mass differences. For very small mass differences in the range of 5 to 50 GeV discoveries could be made for gluino masses up to 1.4 TeV. This search improves the exclusion (discovery) reach near the degenerate limit by roughly 800 GeV (400 GeV) compared to the H_T -based analysis described in Sec. 3; the H_T -based searches do not begin to set stronger limits until $\Delta \gtrsim 50 \text{ GeV}$. Overall, it is clear that a 33 TeV proton collider can have profound implications for models with compressed spectra.

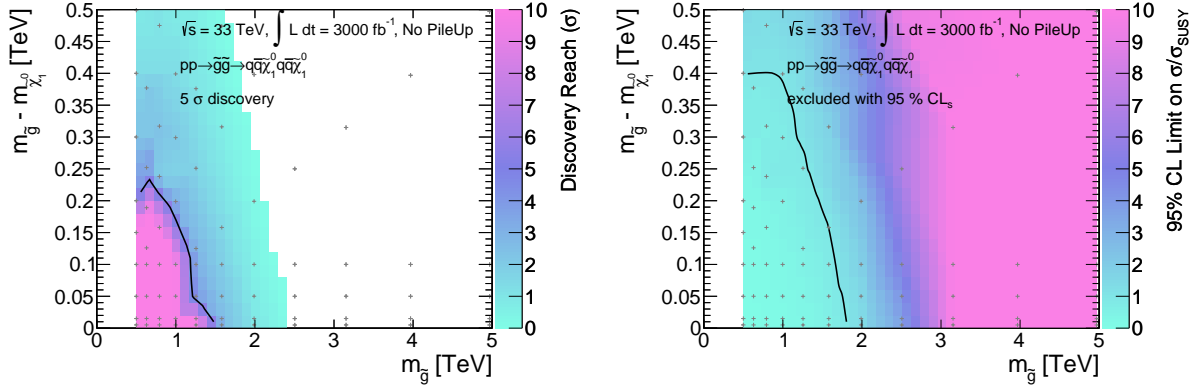


Figure 21: Results for the compressed gluino-neutralino model with light flavor decays at a 33 TeV proton collider with 3000 fb^{-1} are given in the $m_{\tilde{g}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed for the background and pileup is not included.

4.6 Analysis: 100 TeV

This section is devoted to the details of the 100 TeV analysis in the compressed region of the gluino-neutralino model with light flavor decays. As the center-of-mass energy increases, the average p_T of an ISR jet would also increase. This implies that the probability for more than one ISR jets to pass the preselection cuts will be correspondingly higher, causing the E_T^{miss} -based search to have the best acceptance of our search strategies. From Fig. 22, it is clear that this intuition holds; the E_T^{miss} based search gives the optimal significance for all of the probable parameter space. Figure 23 gives histograms of E_T^{miss} for background and a variety of signal models. It is clear that a cut on E_T^{miss} can be used to distinguish signal from background. This can be seen in Table 7 where the cut flows are given for background and three signal models.

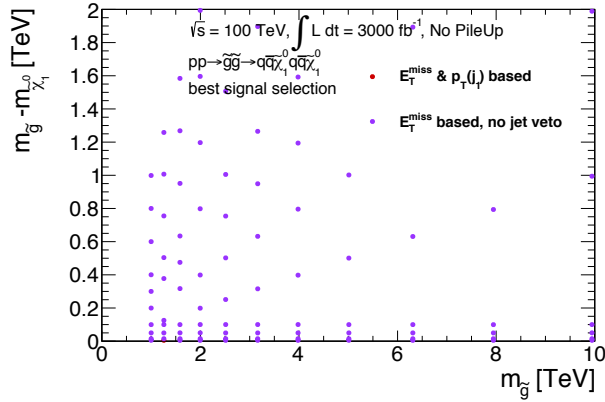


Figure 22: The choice of analysis that lead to the best discovery reach for a given point in parameter space for an integrated luminosity of 3000 fb^{-1} at a 100 TeV proton collider for the compressed region of the gluino-neutralino Simplified Model with light flavor decays. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based.

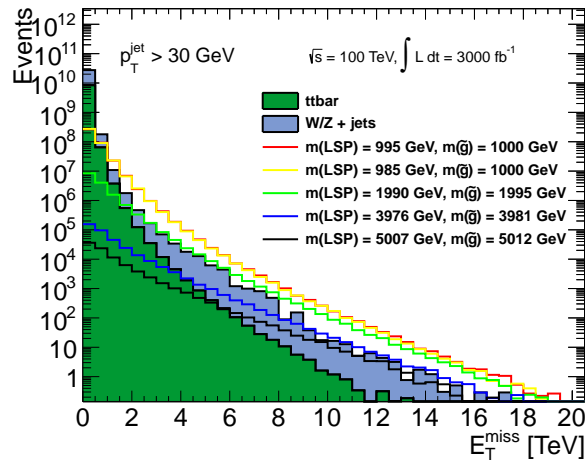


Figure 23: Histogram of E_T^{miss} for signal and background at a 100 TeV proton collider with 3000 fb^{-1} after the preselection for a range of gluino and neutralino masses in the compressed region.

Cut	V+jets	$t\bar{t}$	Total BG	$(m_{\tilde{g}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(1995, 1990)	(2512, 2507)	(5012, 5007)
Preselection	1.7×10^{10}	7.0×10^9	2.4×10^{10}	1.3×10^7	4.1×10^6	7.9×10^4
$p_T^{\text{leadjet}} > 110 \text{ GeV}, \eta^{\text{leadjet}} < 2.4$	1.2×10^{10}	6.1×10^9	1.9×10^{10}	1.3×10^7	4.1×10^6	7.9×10^4
$E_T^{\text{miss}} > 3 \text{ TeV}$	1.3×10^5	2.0×10^4	1.5×10^5	1.9×10^5	9.4×10^4	4.8×10^3
$E_T^{\text{miss}} > 6 \text{ TeV}$	3.6×10^3	229	3.8×10^3	8.0×10^3	5.1×10^3	509
$E_T^{\text{miss}} > 9 \text{ TeV}$	100	9	109	612	410	67

Table 7: Number of expected events for $\sqrt{s} = 100 \text{ TeV}$ and 3000 fb^{-1} for the background processes and selected signal processes. The selection without a veto on additional jets with cuts on E_T^{miss} is applied. Three choices of cuts are provided for illustration.

4.7 Results: 100 TeV

The 5σ discovery [left] and 95% C.L. limits [right] for the gluino-neutralino model are shown in Fig. 24, assuming 3000 fb^{-1} of integrated luminosity. 20% systematic uncertainty is applied to the backgrounds. The assumed signal systematic are outlined in the appendix. Pileup is not included; a demonstration that pileup will not significantly change these results is given in Sec. 4.10 below.

For a 100 TeV proton collider with 3000 fb^{-1} of data, the exclusion reach for a mass difference of 5 GeV covers gluino masses of up to approximately 5.7 TeV, with reduced reach for larger mass differences. For very small mass differences discoveries could be made for gluino masses up to 4.8 TeV. This search improves the exclusion (discovery) reach near the degenerate limit by roughly 1.7 TeV (1.3 TeV) compared to the H_T -based analysis described in Sec. 3; the H_T -based searches do not begin to set stronger limits until $\Delta \gtrsim 500 \text{ GeV}$. Overall, it is clear that a 100 TeV proton collider can have profound implications for models with compressed spectra.

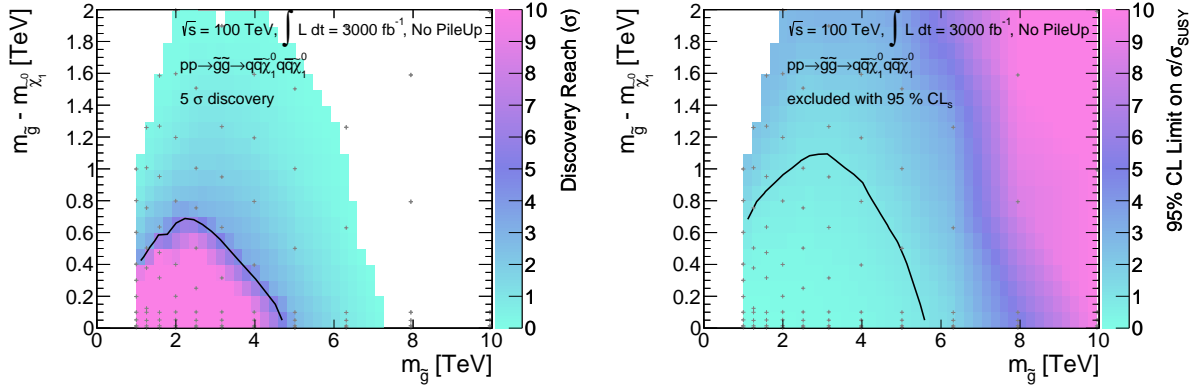


Figure 24: Results for the compressed gluino-neutralino model with light flavor decays at a 100 TeV proton collider are given in the $m_{\tilde{g}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed for the background and pileup is not included.

4.8 Comparing Colliders

The search for the gluino-neutralino model with light flavor decays in the compressed region provides an interesting case study with which to compare the potential impact of different proton colliders. Figure 25 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the full data set assumed for 33 and 100 TeV. At 14 TeV, the factor of 10 increase in luminosity leads to a modest increase from 900 GeV to 1000 GeV in the gluino limits. These limits have a strong dependence on the assumed systematic uncertainties. Therefore, the increase in luminosity does not have a tremendous impact on the ability to probe higher mass gluinos.

In contrast, increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space. For these machines, significantly heavier gluinos can be produced and more hard ISR jets are expected. For higher center-of-mass-energy, these searches specially targeted at the compressed region also become more and more important to fill in the gap in the reach of the untargeted search described in Sec. 3. Figure 25 makes a compelling case for investing in future proton colliders which can operate at these high energies.

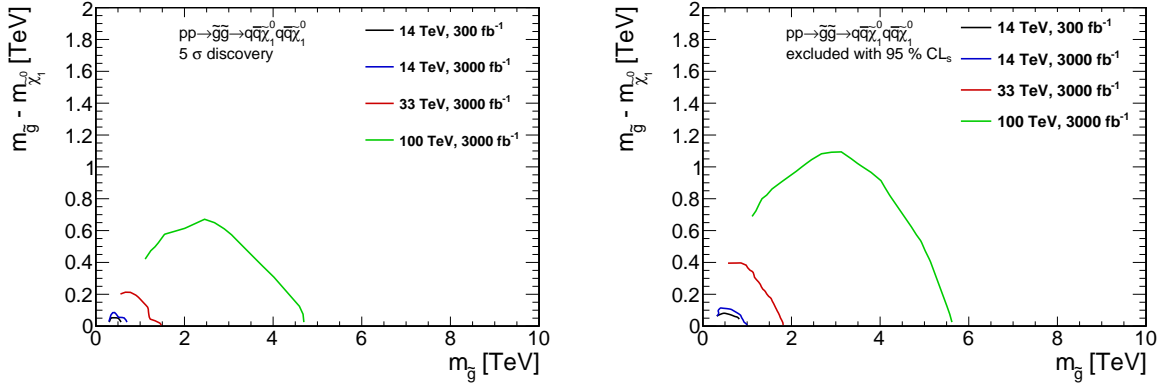


Figure 25: Results for the gluino-neutralino model with light flavor decays for the analyses that target the compressed region of parameter space. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is not included.

4.9 Impact of Systematic Uncertainties

In the previous studies the systematic uncertainties on background are assumed to account for 20% on the overall background normalization. In the event of a discovery, it is likely that this error will be reduced dramatically as tremendous effort will be devoted to understanding these backgrounds in detail. It is therefore interesting to study the impact of this assumption.

Since the E_T^{miss} -based search is most relevant in the region where the 5σ contour lies (see Figs. 17 and 18), we demonstrate the impact of varying the systematic uncertainty for this search strategy for fixed cuts. The results for 3000 fb^{-1} of integrated luminosity at 14 TeV are shown in Fig. 26, where we fix $E_T^{\text{miss}} > 2 \text{ TeV}$ and plot the 5σ discovery reach for 30% [green], 20% [red], 10% [blue], and 5% [black]. We see that a model with a degenerate gluino and neutralino could be discovered up to $\sim 600 \text{ GeV}$ ($\sim 1.1 \text{ TeV}$) for 30% (5%) systematic uncertainty. The leading jet based search also has a comparable sensitivity to systematic uncertainties. Improving our understanding of the background, which could be in principle achieved by studying this large data set carefully, could improve the gluino reach by more than 400 GeV.

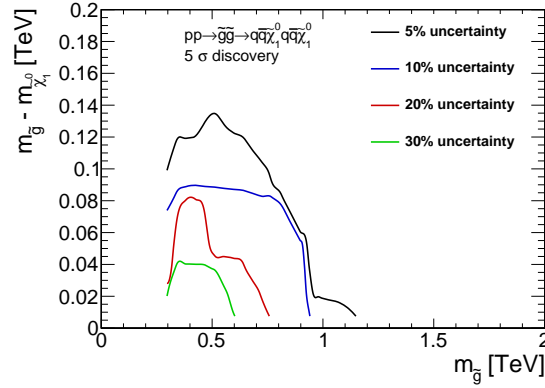


Figure 26: Expected 5σ discovery contours for the $\sqrt{s} = 14$ TeV LHC with 3000 fb^{-1} using the E_T^{miss} search strategy using a fixed cut of $E_T^{\text{miss}} > 2$ TeV. The different curves correspond to various assumptions for the systematic uncertainty on the background: 30% [green], 20% [red], 10% [blue], and 5% [black].

4.10 Impact of Pileup

This section is devoted to an investigation of how the results for compressed spectra presented above would be affected by the presence of pileup. As discussed in Sec. 4.9, the strategy which yields the highest significance in the region where the 5σ contour lies is the E_T^{miss} -based search. Therefore, we use this search to demonstrate the impact of different pileup conditions.

Figure 27 gives the 5σ discovery contour [95% CL exclusion] on the left [right] for no pileup [black], 50 average events per bunch crossing [blue], and 140 average events per bunch crossing [red]. Surprisingly, we see that including pileup appears to increase the reach of this search. One possibility the search is picking up more otherwise “invisible” final states with soft ISR that become visible because there are pileup jets to push these events above the cut thresholds. In other words, this apparent improvement is due to the fact that we have a fixed grid of cuts for our optimization scans. Note that the limits for $m_{\tilde{g}} \simeq m_{\tilde{\chi}_1^0}$ remain unchanged; the presence of pileup only impacts somewhat larger mass differences.

Note that all the curves in Fig. 27 are computed for a fixed set of cuts, instead of reoptimizing for each pileup scenario which would obscure the comparison of the different limits. It is clear that including pileup only makes the reach stronger. The fact that we neglected pileup for the main results using these search strategies will imply that the limits we present are conservative.

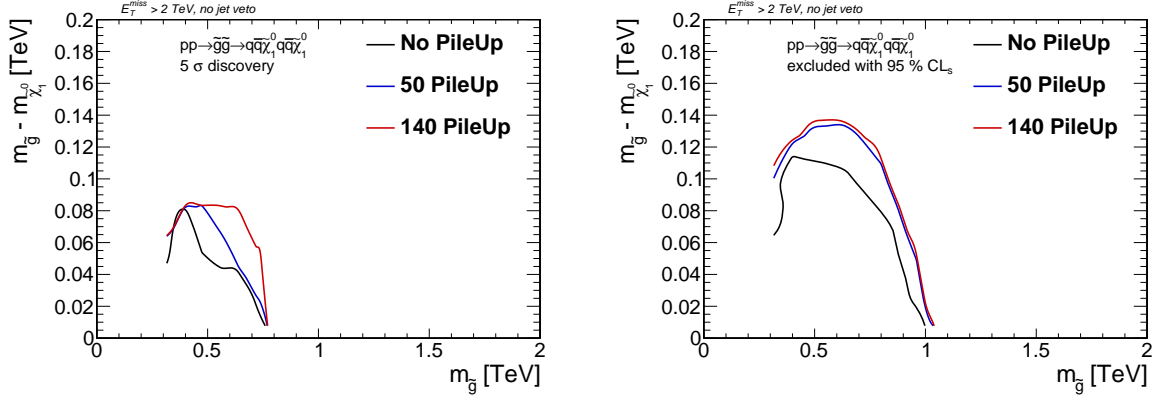


Figure 27: Expected 5σ discovery contours [left] and 95% CL limits [right] for the $\sqrt{s} = 14$ TeV LHC with 3000 fb^{-1} using the E_T^{miss} search strategy for a fixed cut of $E_T^{\text{miss}} > 2$ TeV. The different curves correspond to the following average pileup: 0 [black], 50 [blue], 140 [red].

5 The Squark-Neutralino Model

In the “squark-neutralino model”, the first and second generation squarks $\tilde{q} = \tilde{u}_L, \tilde{u}_R, \tilde{d}_L, \tilde{d}_R, \tilde{c}_L, \tilde{c}_R, \tilde{s}_L, \tilde{s}_R$ are the only kinematically accessible colored states. The gluino is completely decoupled from the squark production diagrams — the squark production cross section is significantly reduced compared to models where the gluino is just above the kinematic limit. The squarks decay directly to the LSP and the corresponding quark, $\tilde{q}_i \rightarrow q_i \tilde{\chi}_1^0$. The only two relevant parameters are the squark mass $m_{\tilde{q}}$, which is taken to be universal for the first two generations, and the neutralino mass $m_{\tilde{\chi}_1^0}$. The model is summarized as:

BSM particles	production	decays
$\tilde{q}, \tilde{\chi}_1^0$	$pp \rightarrow \tilde{q}\tilde{q}^*$	$\tilde{q} \rightarrow q \tilde{\chi}_1^0$

Due to the structure of the renormalization group equations in the Minimal SUSY SM, a heavy gluino would tend to raise the squark masses; some tuning is required to achieve light squarks. However, a class of theories with Dirac gluinos can be well approximated by this Simplified Model [33].

Since the final state is two (or more) hard jets and missing energy, this model also serves to test the power of jets+ E_T^{miss} style analyses. The mass reach is not be nearly as high as in the gluino-neutralino light flavor decay model for two reasons: neglecting ISR and FSR, the final state has only two hard jets from the squark decays as opposed to four hard jets from the gluino decays, and cross section for producing squark pairs with the gluino completely decoupled is substantially lower than that for producing gluino pairs of the same mass. Note that we checked that the 4 jet requirement included in the jets+ E_T^{miss} preselection does not have a detrimental impact on the squark results presented below.

We simulated matched MadGraph samples for $\tilde{q}\tilde{q}^*$ with up to 2 additional generator level jets for the following points in parameter space:²

BSM particles	masses
$m_{\tilde{q}}$ [14 TeV]	(315, 397, 500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989) GeV
$m_{\tilde{q}}$ [33 TeV]	(500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989, 3489, 3989, 4489, 4989, 5489, 5989) GeV
$m_{\tilde{q}}$ [100 TeV]	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 5012, 6310, 7944, 9944, 11944, 13944, 15944, 17944, 19944) GeV
$m_{\tilde{\chi}_1^0}$	1 GeV (0.2, 0.4, 0.6, 0.7, 0.8, 0.9) $\times m_{\tilde{q}}$ $m_{\tilde{q}} - (100 \text{ GeV}, 50 \text{ GeV}, 15 \text{ GeV}, 5 \text{ GeV})$

The signature of this model is multi-jets and E_T^{miss} . Therefore, the dominant backgrounds are identical to the ones relevant for the gluino-neutralino model with light flavor decays and are discussed in Sec 3.1. We use the same analysis strategy as for the gluino-neutralino model, described in Sec. 3.2, to project discovery reach and limits for this model. Given that pileup had no impact on the results using this search strategy as demonstrated in Sec. 3.12 above, we present here results only for the no pile-up scenario and expect little change when pileup is included.

Note that this search yields some power to discover these models in the difficult region of parameter space where the squark is degenerate with the neutralino, but Sec. 6 will provide the results of a search which is specifically targeted for this region of parameter space.

The next two sections give the details of the 14 TeV LHC analysis and results.

5.1 Analysis: 14 TeV

Figure 28 shows the background and three signal distributions for the 14 TeV LHC in the two kinematic variables which are scanned in this analysis: E_T^{miss} [left] and H_T [right]. In Table 8 we give the number of events after each stage of cuts for the dominant backgrounds and two signal models. From this table, it is clear that the 14 TeV LHC with 3000 fb^{-1} would be able to exclude (but not discover) squarks with mass of 1255 GeV.

²We include 1 GeV for an example where the neutralino is effectively massless; the second line of neutralino masses is chosen to cover the bulk of the squark-neutralino plane; the final line is chosen to ensure coverage in the “compressed” region.

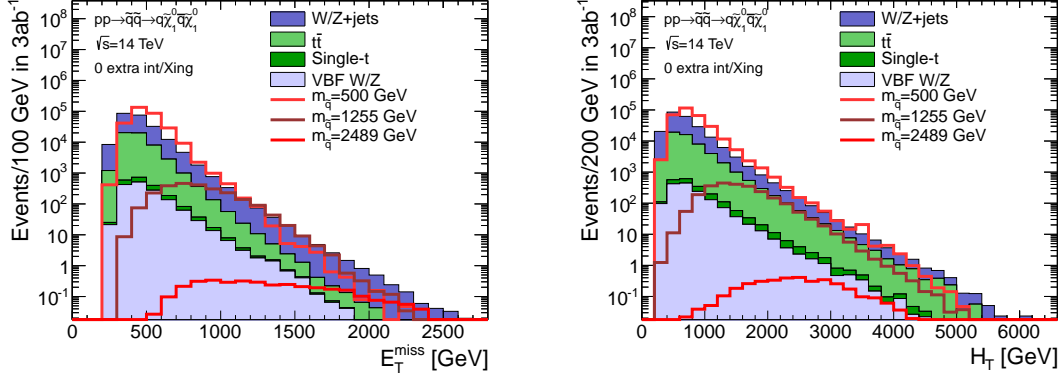


Figure 28: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of squark-neutralino models at the 14 TeV LHC. The neutralino mass is 1 GeV for all signal models.

Cut	V+jets		Total BG	$m_{\tilde{q}}$ [GeV]	
	$t\bar{t}$			500	1255
Preselection	2.07×10^7	2.47×10^7	4.54×10^7	2.94×10^6	1.41×10^4
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.45×10^5	1.20×10^5	5.65×10^5	6.31×10^5	8.48×10^3
$p_T^{\text{leading}} < 0.4 \times H_T$	1.69×10^5	5.16×10^4	2.21×10^5	3.05×10^5	2.42×10^3
$E_T^{\text{miss}} > 550 \text{ GeV}$ $H_T > 600 \text{ GeV}$	3.98×10^4	1.16×10^4	5.15×10^4	1.27×10^5	2.33×10^3
$E_T^{\text{miss}} > 1200 \text{ GeV}$ $H_T > 1400 \text{ GeV}$	174	23	197	185	222

Table 8: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected squark masses for the squark-neutralino model. The neutralino mass is 1 GeV. Two choices of cuts on E_T^{miss} and H_T are provided, and for each squark mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

5.2 Results: 14 TeV

The results for the squark-neutralino model are shown in Fig. 29 for the 14 TeV LHC. The left [right] panels give discovery significance [95% CL exclusion] contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The top [bottom], results assume 300 fb^{-1} [3000 fb^{-1}] of data. As expected, the reach is significantly smaller than for the gluino-neutralino model with light flavor decays.

Using the NLO squark pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of squark mass which would yield 10 events at 300 fb^{-1} (3000 fb^{-1}) is 2.4 (2.9) TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 14 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 14 TeV

300 fb⁻¹ limit with massless neutralinos is projected to be 1.5 TeV (corresponding to 1022 events), while the 14 TeV 3000 fb⁻¹ limit is projected to be 1.7 TeV (corresponding to 3482 events). Given these huge numbers of events, it is possible that a different (or more sophisticated) search strategy would allow for greater sensitivity to these models — this is outside the purview of the current study. Finally, we note that the 14 TeV LHC with 3000 fb⁻¹ could discover a squark as heavy as 800 GeV if the neutralino is massless. Unlike in the gluino-neutralino model, the squark mass discovery reach immediately begins to weaken significantly as soon as the neutralino mass is increased from the massless limit.

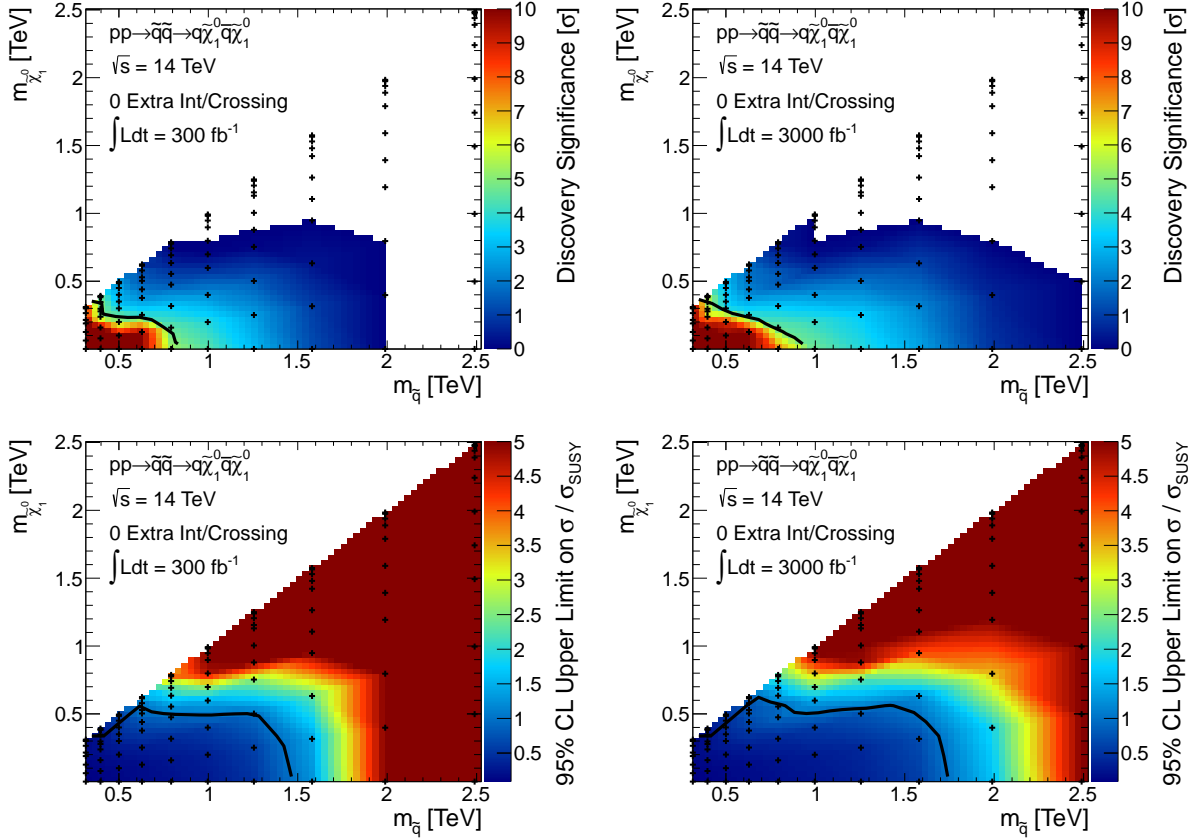


Figure 29: Results for the squark-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The top [bottom] row shows the expected 5 σ discovery reach [95% confidence level upper limits] for squark-anti-squark production at the 14 TeV LHC. Mass points to the left/below the contours are expected to be probed with 300 fb⁻¹ [left] and 3000 fb⁻¹ [right] of data. A 20% systematic uncertainty is assumed for the backgrounds. Pileup is not included.

5.3 Analysis: 33 TeV

Figure 30 shows the background and three signal distributions for a 33 TeV proton collider in the two kinematic variables which are scanned in this analysis: E_T^{miss} [left] and H_T [right]. In Table 9 we give the number of events after each stage of cuts for the dominant backgrounds and three signal models. From this table, it is clear that a 33 TeV proton collider with 3000 fb^{-1} would be able to exclude (but not discover) squarks with mass of 3152 GeV.

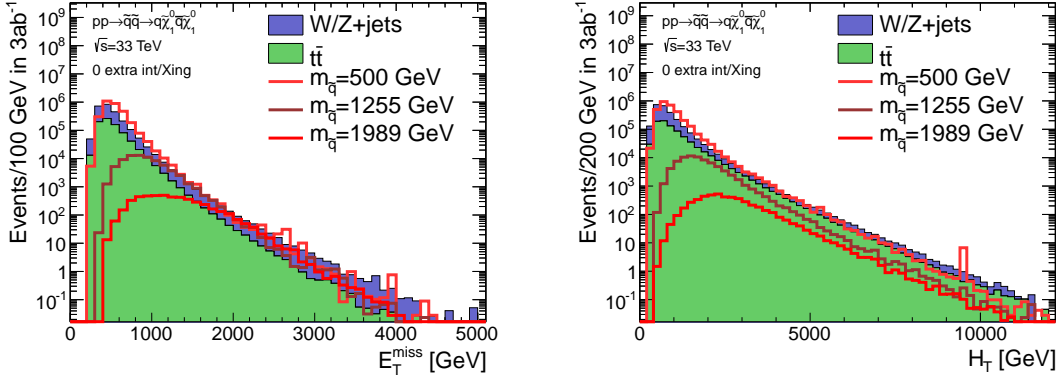


Figure 30: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of squark-neutralino models at a 33 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut	V+jets	$t\bar{t}$	Total BG	$m_{\tilde{q}}$ [GeV]		
				629	1255	3152
Preselection	1.55×10^8	2.86×10^8	4.42×10^8	1.20×10^7	3.99×10^5	926
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.50×10^6	1.93×10^6	6.44×10^6	3.66×10^6	2.34×10^5	762
$p_T^{\text{leading}} < 0.4 \times H_T$	1.70×10^6	8.02×10^5	2.50×10^6	1.61×10^6	7.67×10^4	150
$E_T^{\text{miss}} > 650 \text{ GeV}$ $H_T > 650 \text{ GeV}$	1.13×10^6	5.87×10^5	1.72×10^6	1.55×10^6	7.67×10^4	150
$E_T^{\text{miss}} > 1300 \text{ GeV}$ $H_T > 1350 \text{ GeV}$	1.08×10^4	6.79×10^3	1.76×10^4	1.96×10^4	1.54×10^4	124
$E_T^{\text{miss}} > 2650 \text{ GeV}$ $H_T > 3350 \text{ GeV}$	51.5	16.3	67.8	50.8	26.9	22.3

Table 9: Number of expected events for $\sqrt{s} = 33 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected squark masses for the squark-neutralino model. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each squark mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

5.4 Results: 33 TeV

The results for the squark-neutralino model are shown in Fig. 31 for a 33 TeV proton collider. Discovery significance [95% CL exclusion] contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane are shown on the left [right]. As expected, the reach is significantly smaller than for the gluino-neutralino model with light flavor decays.

Using the NLO squark pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of squark mass which would yield 10 events at 3000 fb^{-1} is 5.8 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 33 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 33 TeV 3000 fb^{-1} limit with massless neutralinos is projected to be 3.4 TeV (corresponding to 3482 events). Given this huge number of events, it is possible that a different (or more sophisticated) search strategy would allow for greater sensitivity to these models — this is outside the purview of the current study. Finally, we note that the 33 TeV proton collider with 3000 fb^{-1} could discover a squark as heavy as 1.4 TeV if the neutralino is massless. As in the 14 TeV search, the squark mass discovery reach immediately begins to weaken significantly as the neutralino mass is increased from the massless limit.

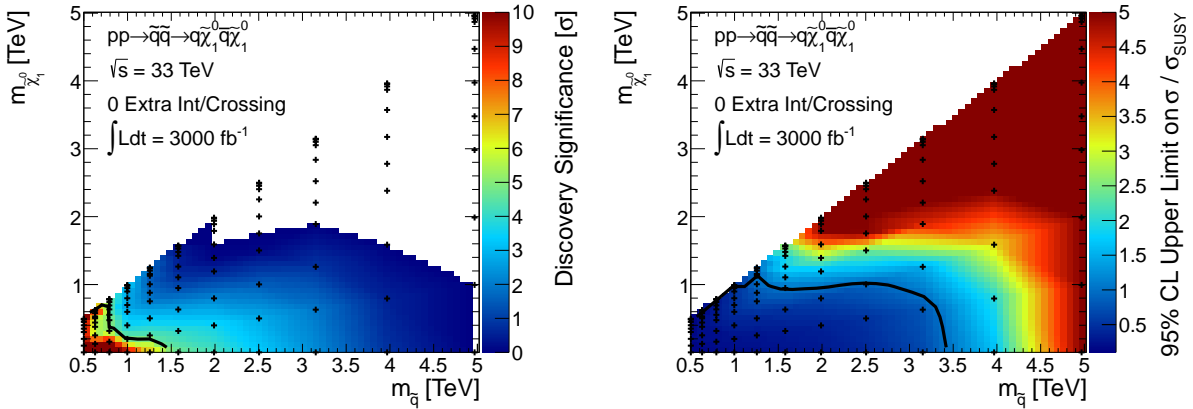


Figure 31: Results for the squark-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The left [right] panels show the expected 5σ discovery reach [95% confidence level upper limits] for squark-anti-squark production at a 33 TeV proton collider. Mass points to the left/below the contours are expected to be probed with 3000 fb^{-1} of data [right]. A 20% systematic uncertainty is assumed for the backgrounds. Pileup is not included.

5.5 Analysis: 100 TeV

Figure 32 shows the background and three signal distributions for a 100 TeV proton collider in the two kinematic variables which are scanned in this analysis: E_T^{miss} [left] and H_T [right]. In Table 10 we give the number of events after each stage of cuts for the dominant backgrounds and a two signal models. From this table, it is clear that a 100 TeV proton collider with 3000 fb^{-1} would be able to exclude (but not discover) squarks with mass of 8 TeV.

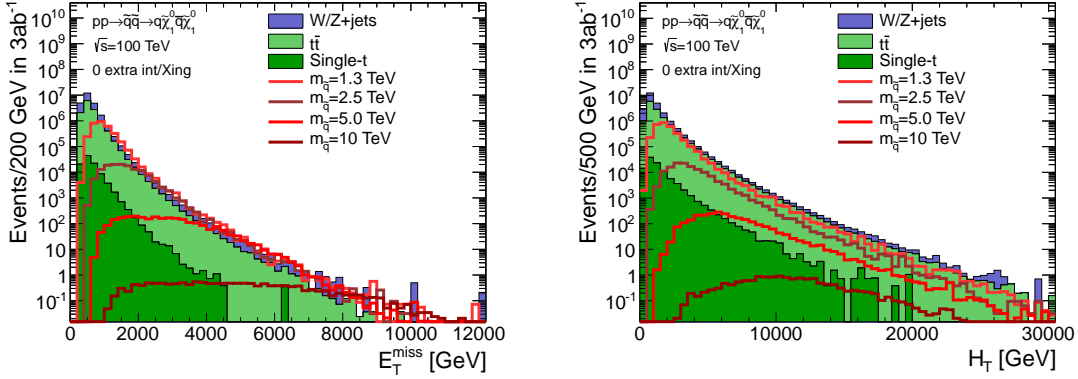


Figure 32: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of squark-neutralino models at a 100 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut	V+jets	$t\bar{t}$	Total BG	$m_{\tilde{q}}$ [GeV]		
				3162	5012	7944
Preselection	1.64×10^9	3.33×10^9	4.97×10^9	2.01×10^5	1.44×10^4	668
$E_T^{\text{miss}} / \sqrt{H_T} > 15 \text{ GeV}^{1/2}$	3.59×10^7	3.31×10^7	6.90×10^7	1.62×10^5	1.26×10^4	614
$p_T^{\text{leading}} < 0.4 \times H_T$	1.19×10^7	1.25×10^7	2.44×10^7	4.14×10^4	2.63×10^3	96.9
$E_T^{\text{miss}} > 5550 \text{ GeV}$ $H_T > 900 \text{ GeV}$	24	21.2	45.1	73.3	60.1	19.9
$E_T^{\text{miss}} > 4900 \text{ GeV}$ $H_T > 5450 \text{ GeV}$	61.2	53.3	114	119	143	29.5
$E_T^{\text{miss}} > 6150 \text{ GeV}$ $H_T > 8200 \text{ GeV}$	9.2	8.4	17.6	11.2	17	11.5

Table 10: Number of expected events for $\sqrt{s} = 100 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected squark masses for the squark-neutralino model. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each squark mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

5.6 Results: 100 TeV

The results for the squark-neutralino model are shown in Fig. 33 for a 100 TeV proton collider. Discovery significance [95% CL exclusion] contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane are shown on the left [right]. As expected, the reach is significantly smaller than for the gluino-neutralino model with light flavor decays.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of squark mass which would yield 10 events at 3000 fb^{-1} is 14.8 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 100 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 100 TeV 3000 fb^{-1} limit with massless neutralinos is projected to be 8.0 TeV (corresponding to 849 events). Given this huge number of events, it is possible that a different (or more sophisticated) search strategy would allow for greater sensitivity to these models — this is outside the purview of the current study. Finally, we note that the 100 TeV proton collider with 3000 fb^{-1} could discover a squark as heavy as 2.4 TeV if the neutralino is massless. Compared to the 14 and 33 TeV searches, the squark reach degrades less rapidly as the neutralino mass is increased from the massless limit. The next section provides a comparison of the impact that the four collider scenarios studied here can have on the parameter space of this model.

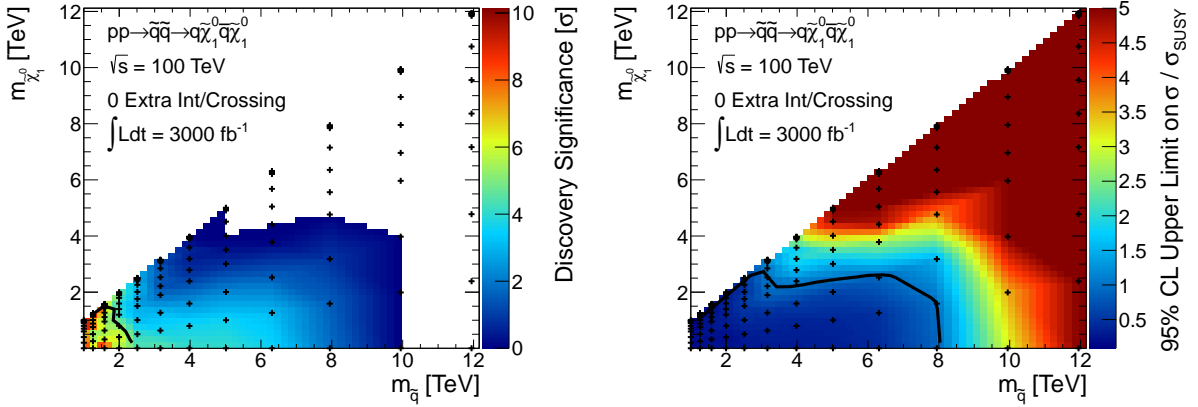


Figure 33: Results for the squark-neutralino model with light flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The left [right] panels shows the expected 5σ discovery reach [95% confidence level upper limits] for squark-anti-squark production at a 100 TeV proton collider. Mass points to the left/below the contours are expected to be probed with 3000 fb^{-1} of data [right]. A 20% systematic uncertainty is assumed for the backgrounds. Pileup is not included.

5.7 Comparing Colliders

The squark-neutralino model has a similar multi-jet plus E_T^{miss} signature to the gluino-neutralino model with light flavor decays. However, the squark-neutralino model is more difficult to probe due to the smaller number of hard jets in the final state coupled with the substantially smaller production cross section. Since this model provides a more challenging scenario, it is interesting to understand the impact that can be made on exploring the parameter space with different collider scenarios. Figure 34 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the reach using the full data set assumed for 33 and 100 TeV.

In general, we find that due to the small cross sections, it is very difficult to distinguish this model from background with discovery level significance³. Consequentially, the discovery reach does not appear to significantly improve with the 14 TeV luminosity upgrade. The discovery reach in the massless neutralino limit also scales slowly with the CM energy, increasing only by a factor of 3 from 14 TeV to 100 TeV, compared to a factor of 5 for the gluino-neutralino model.

The exclusion reach for the squark-neutralino models is much more favorable in comparison. At this level of significance the background systematics are less difficult to overcome, and the limits scale much more favorably with luminosity and CM energy, as in the gluino-neutralino model. Figure 8 makes a compelling case for investing in future proton colliders which can operate at these high energies.

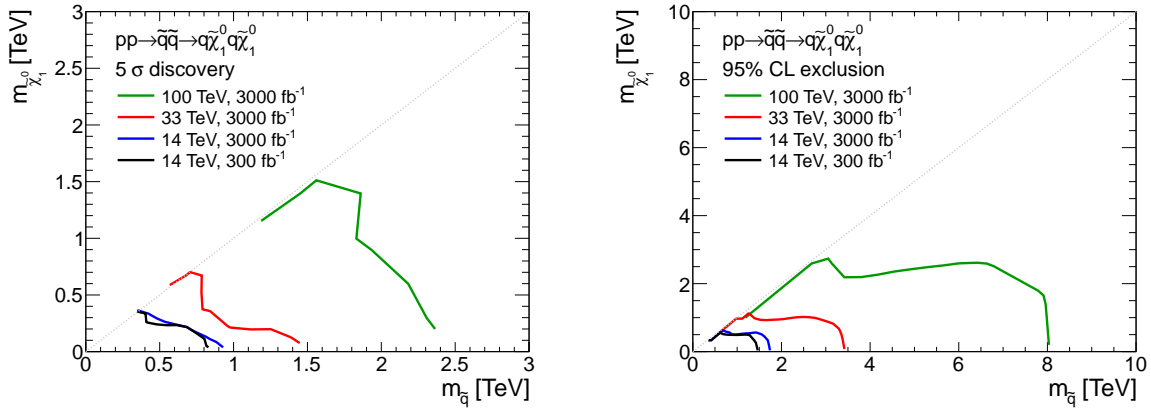


Figure 34: Results for the squark-neutralino model. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is not included.

³It is worth noting that this search, which was devised originally to target gluinos, has not been extensively optimized for the signature of squark pair production. It is possible that a search exactly tailored to this signal could improve the reach beyond what is found here.

6 The Compressed Squark-Neutralino Model

The results presented in the previous section were derived using a search which targeted the bulk of the squark-neutralino Simplified Model parameter space. In the compressed region where

$$m_{\tilde{q}} - m_{\tilde{\chi}_1^0} \equiv \Delta m \ll m_{\tilde{q}} \quad (2)$$

a different search strategy is required. For parameters in this range, the jets which result from the direct decays of the squark will be very soft and one has to rely on ISR jets to discriminate these models from background. These signatures will be very similar to those produced by the compressed gluino-neutralino model with light flavor decays, and therefore the backgrounds will be identical to those described above in Sec. 4.1. Therefore, we will use the same search strategies described above in Sec. 4.1.

6.1 Analysis: 14 TeV

As can be seen in Fig 35, for the very small squark masses excludable in the compressed region the only relevant strategy is the E_T^{miss} based search. A histogram of the discriminating variable relevant for this search is shown in Fig. 36. We also give the number of events after cuts for this strategy in Table 11. It is clear that for low mass squarks, it is possible that the signal could be distinguished over background.

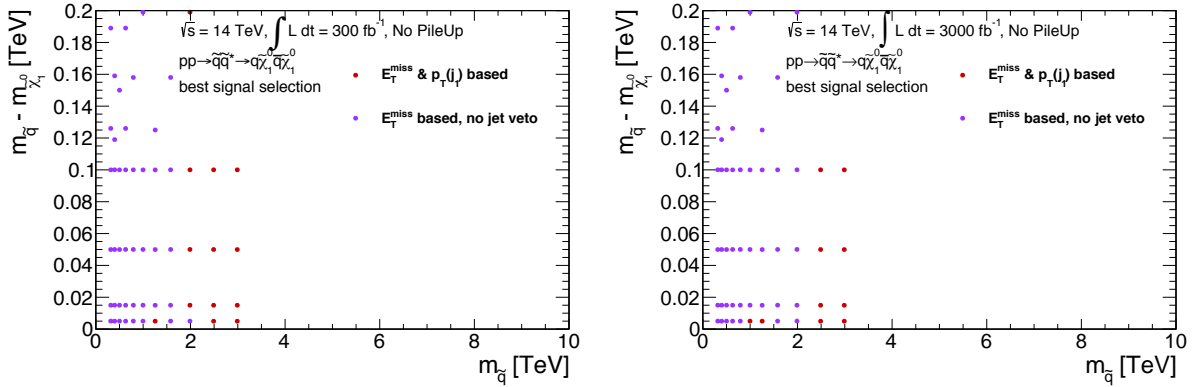


Figure 35: The choice of analysis strategy that leads to the best discovery reach for a given point in parameter space for an integrated luminosity of 300 fb^{-1} [left] and 3000 fb^{-1} [right] for the compressed region of the squark-neutralino model. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based.

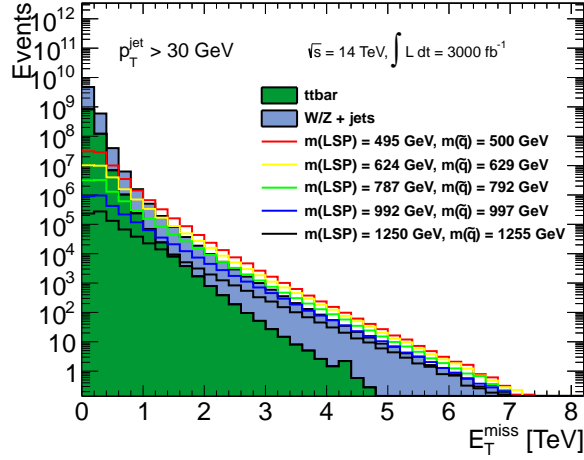


Figure 36: Histogram of E_T^{miss} for signal and background after the preselection for a range of squark and neutralino masses in the compressed region.

Cut	$V+\text{jets}$	$t\bar{t}$	Total BG	$(m_{\tilde{q}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(500, 495)	(792, 787)	(997, 992)
Preselection	1.3×10^9	1.2×10^8	1.4×10^9	5.8×10^6	4.3×10^5	9.8×10^4
$p_T^{\text{leadjet}} > 110 \text{ GeV}, \eta^{\text{leadjet}} < 2.4$	7.9×10^8	8.1×10^7	8.7×10^8	4.5×10^6	3.5×10^5	8.0×10^4
$E_T^{\text{miss}} > 500 \text{ GeV}$	2.1×10^6	1.5×10^5	2.3×10^6	4.5×10^5	5.2×10^4	1.4×10^4
$E_T^{\text{miss}} > 1 \text{ TeV}$	4.9×10^4	2.1×10^3	5.2×10^4	3.0×10^4	5.0×10^3	1.6×10^3
$E_T^{\text{miss}} > 2 \text{ TeV}$	278	3	282	237	64	24

Table 11: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ and 3000 fb^{-1} for the background processes and selected signal processes. The selection without a veto on additional jets with cuts on E_T^{miss} is applied. Three choices of cuts are provided for illustration.

6.2 Results: 14 TeV

The results for the squark neutralino model in the compressed region of parameter space are given in Fig. 37. As discussed above, only the E_T^{miss} based strategy (see Sec. 4.1) is relevant for this model at the 14 TeV LHC. It is possible to exclude (discover) squarks in the degenerate limit with mass less than $\sim 650 \text{ GeV}$ (500 GeV) with 300 fb^{-1} of data. Increasing the integrated luminosity by a factor of 10 has a minimal impact on the discovery reach for compressed squark models. This search improves the exclusion (discovery) reach near the degenerate limit by roughly 300 GeV (150 GeV) compared to the H_T -based analysis described in Sec. 5; the H_T -based searches do not begin to set stronger limits until $\Delta \gtrsim 50 \text{ GeV}$. Finally, we note that given our results for the compressed gluino-neutralino study in Sec. 4.10 above, pileup is not expected to have a significant

impact on these conclusions. The compressed region of this model will be difficult to probe at the 14 TeV LHC, but will still represent a significant improvement over current bounds.

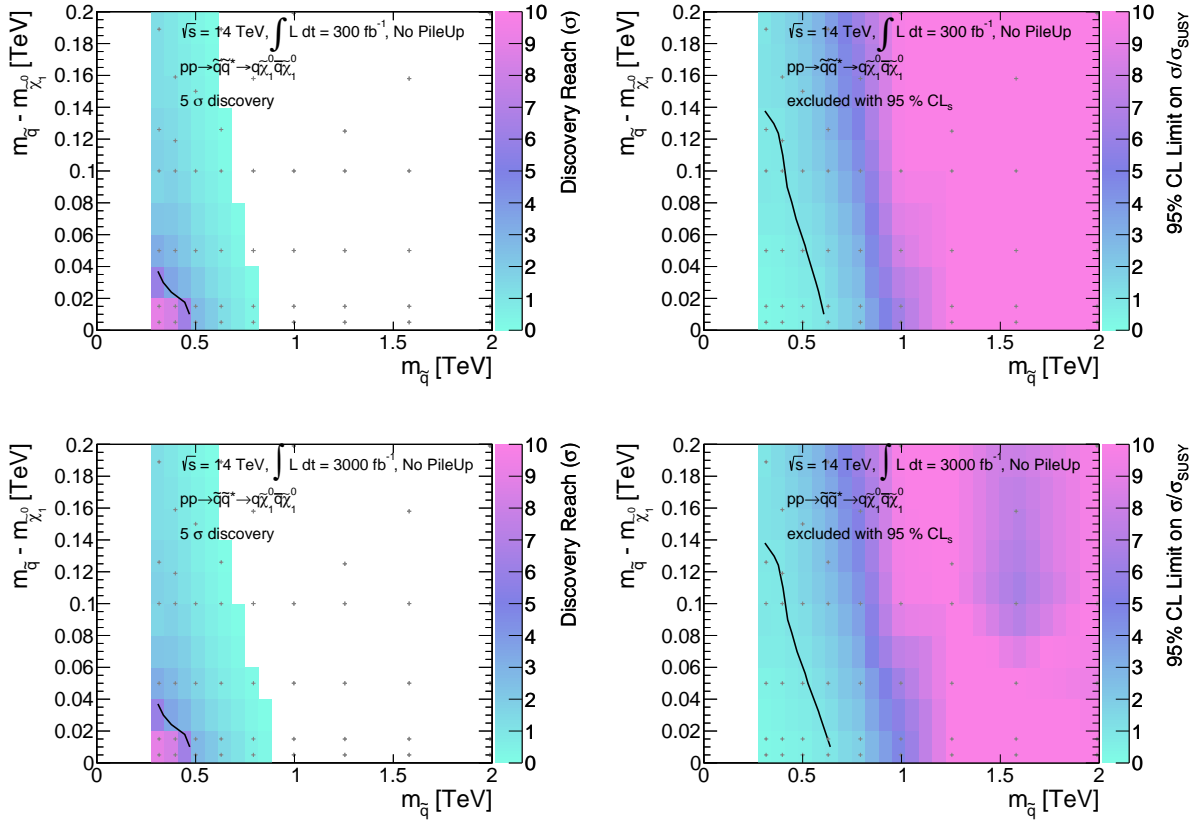


Figure 37: Results for the compressed squark-neutralino model with light flavor decays are given in the $m_{\tilde{q}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The top [bottom] row shows the expected 5 σ discovery reach [95% confidence level upper limits] for squark-anti-squark production. Mass points to the left/below the contours are expected to be probed at 300 fb⁻¹ [left] and 3000 fb⁻¹ [right]. A 20% systematic uncertainty is assumed for the background. Pileup is not included.

6.3 Analysis: 33 TeV

As discussed above in the context of the compressed region of the gluino-neutralino model, the E_T^{miss} based search tends to be more powerful at the higher energy colliders since the probability of having multiple ISR jets increases. From Fig. 38, it is clear that the relevant strategy in the region that can be probed by this machine is the E_T^{miss} based search. A histogram of the discriminating variable relevant for this search is shown in Fig. 39. We also give the number of events after cuts for this strategy in Table 12. It is clear that for low mass squarks, it is possible that the signal could be distinguished over background.

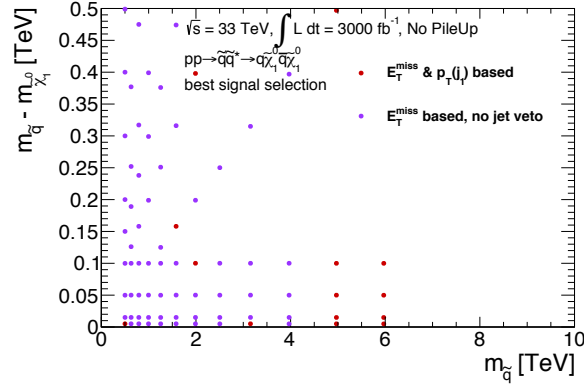


Figure 38: The choice of analysis that lead to the best discovery reach for a given point in parameter space for an integrated luminosity of 3000 fb^{-1} at a 33 TeV proton collider for the compressed region of the squark-neutralino Simplified Model with light flavor decays. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based.

Cut			Total BG	$(m_{\tilde{q}}, m_{\tilde{\chi}_1^0})$ [GeV]		
	V+jets	$t\bar{t}$		(797, 787)	(997, 992)	(1580, 1575)
Preselection	4.2×10^9	8.6×10^8	5.1×10^9	8.4×10^6	2.6×10^6	2.0×10^5
$p_T^{\text{leadjet}} > 110 \text{ GeV}, \eta^{\text{leadjet}} < 2.4$	2.6×10^9	6.5×10^8	3.3×10^9	7.2×10^6	2.3×10^6	1.8×10^5
$E_T^{\text{miss}} > 1 \text{ TeV}$	7.5×10^5	1.1×10^5	8.6×10^5	3.5×10^5	1.5×10^5	2.0×10^4
$E_T^{\text{miss}} > 3 \text{ TeV}$	1.5×10^3	62	1.5×10^3	2.1×10^3	1.3×10^3	315
$E_T^{\text{miss}} > 5 \text{ TeV}$	19	0	19	30	20	7

Table 12: Number of expected events for $\sqrt{s} = 33 \text{ TeV}$ and 3000 fb^{-1} for the background processes and selected signal processes. The selection without a veto on additional jets with cuts on E_T^{miss} is applied. Three choices of cuts are provided for illustration.

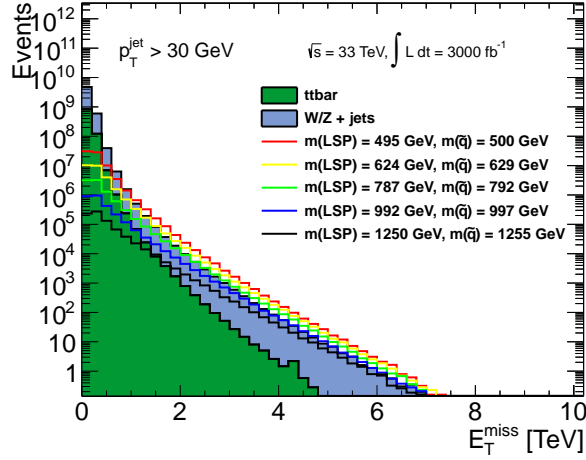


Figure 39: Histogram of E_T^{miss} for signal and background at a 33 TeV proton collider after the preselection for a range of squark and neutralino masses in the compressed region.

6.4 Results: 33 TeV

The results for the squark neutralino model in the compressed region of parameter space are given in Fig. 40. As discussed above, only the E_T^{miss} based strategy (see Sec. 4.1) is relevant for this model at a 33 TeV proton collider. It is possible to exclude (discover) squarks in the degenerate limit with mass less than $\sim 1.2(0.7)$ TeV with 3000 fb^{-1} of data. This does not substantially improve the discovery reach near the degenerate limit compared to the H_T -based analysis described in Sec. 5, but does improve the exclusion reach by roughly 200 GeV for $\Delta \lesssim 100$ GeV. Note that given our results for the compressed gluino-neutralino study in Sec. 4.10 above, pileup is not expected to have a significant impact on these conclusions. This search demonstrates that a 33 TeV machine will be relevant to our understanding of the difficult to probe compressed region of this model.

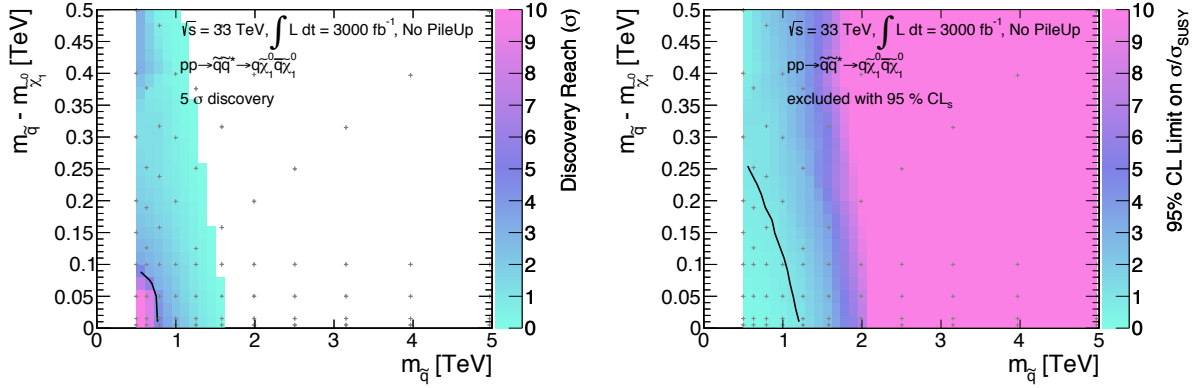


Figure 40: Results for the compressed squark-neutralino model with light flavor decays at a 33 TeV proton collider are given in the $m_{\tilde{q}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for squark-anti-squark pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed for the background and pileup is not included.

6.5 Analysis: 100 TeV

As discussed above in the context of the compressed region of the gluino-neutralino model, the E_T^{miss} based search tends to be more powerful at the higher energy colliders since the probability of having multiple ISR jets increases. From Fig. 41, it is clear that the relevant strategy in the region that can be probed by this machine is the E_T^{miss} based search. A histogram of the discriminating variable relevant for this search is shown in Fig. 42. We also give the number of events after cuts for this strategy in Table 13. It is clear that for low mass squarks, it is possible that the signal could be distinguished over background.

Cut	V+jets	$t\bar{t}$	Total BG	$(m_{\tilde{q}}, m_{\tilde{\chi}_1^0})$ [GeV]		
				(1995, 1990)	(2512, 2507)	(5012, 5007)
Preselection	1.7×10^{10}	7.0×10^9	2.4×10^{10}	2.0×10^6	6.4×10^5	1.4×10^4
$p_T^{\text{leadjet}} > 110 \text{ GeV}, \eta^{\text{leadjet}} < 2.4$	1.2×10^{10}	6.1×10^9	1.9×10^{10}	2.0×10^6	6.4×10^5	1.4×10^4
$E_T^{\text{miss}} > 3 \text{ TeV}$	1.3×10^5	2.0×10^4	1.5×10^5	4.1×10^4	1.9×10^4	935
$E_T^{\text{miss}} > 6 \text{ TeV}$	3.6×10^3	229	3.8×10^3	2.3×10^3	$1. \times 10^3$	116
$E_T^{\text{miss}} > 9 \text{ TeV}$	100	9	109	206	130	17

Table 13: Event yields for background and selected signal points for $\sqrt{s} = 100 \text{ TeV}$ and 3000 fb^{-1} in the event selection with cuts on E_T^{miss} .

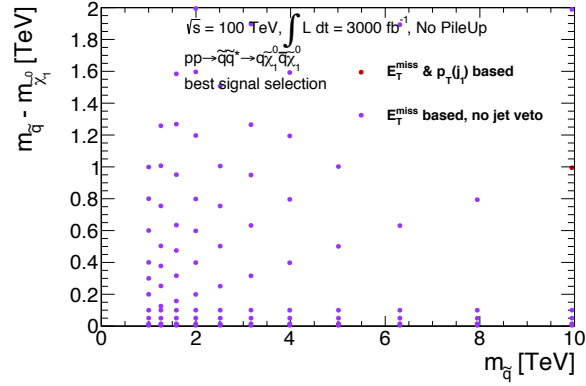


Figure 41: The choice of analysis that lead to the best discovery reach for a given point in parameter space for an integrated luminosity of 3000 fb^{-1} at a 100 TeV proton collider for the compressed region of the squark-neutralino Simplified Model with light flavor decays. The colors refer to the analyses as presented above: red circle = leading jet based, purple circle = E_T^{miss} -based.

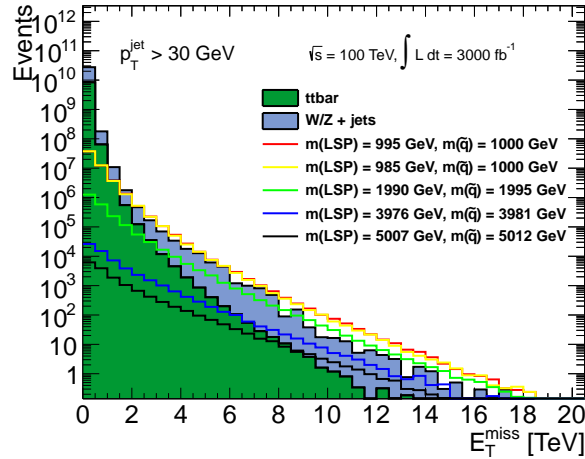


Figure 42: Histogram of E_T^{miss} for signal and background at a 100 TeV proton collider after the preselection for a range of squark and neutralino masses in the compressed region.

6.6 Results: 100 TeV

The results for the squark neutralino model in the compressed region of parameter space are given in Fig. 43. As discussed above, only the E_T^{miss} based strategy (see Sec. 4.1) is relevant for this model at a 100 TeV proton collider. It is possible to exclude (discover) squarks in the degenerate limit with mass less than $\sim 4 \text{ TeV}$ (3 TeV) with 3000 fb^{-1} of data. This improves the exclusion (discovery) reach near the degenerate limit compared to the H_T -based analysis described in Sec. 5 by roughly 1.5 TeV (1.8 TeV) for $\Delta \lesssim 200 \text{ GeV}$. Note that given our results for the compressed

gluino-neutralino study in Sec. 4.10 above, pileup is not expected to have a significant impact on these conclusions. This search demonstrates that a 100 TeV machine will be relevant to our understanding of the difficult to probe compressed region of this model.

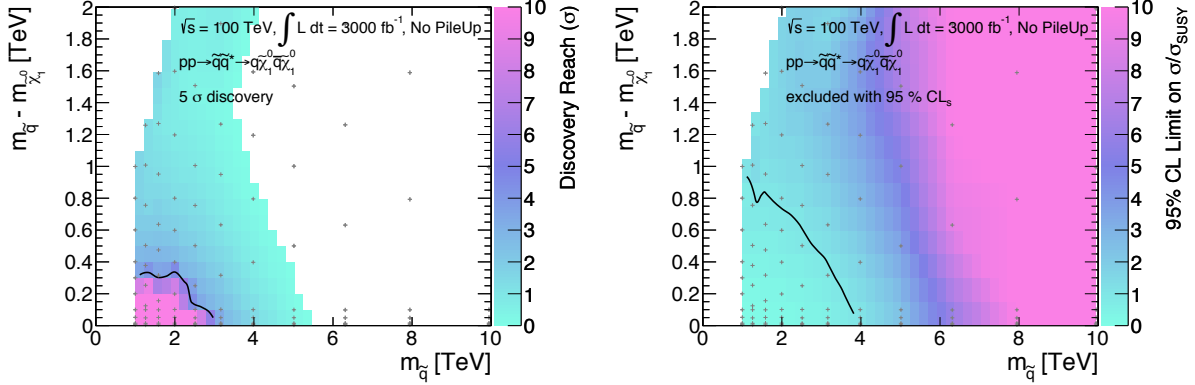


Figure 43: Results for the compressed squark-neutralino model with light flavor decays at a 100 TeV proton collider are given in the $m_{\tilde{q}} - m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{q}}$ plane. The left [right] plot shows the expected 5σ discovery reach [95% confidence level upper limits] for squark-anti-squark pair production. Mass points to the left/below the contours are expected to be probed at 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed for the background and pileup is not included.

6.7 Comparing Colliders

The compressed region of the squark-neutralino model has a similar signature to the compressed gluino-neutralino model with light flavor decays. However, the squark-neutralino model is more difficult to probe due to the substantially smaller production cross section. Since this model provides a more challenging scenario, it is interesting to understand the impact that can be made on exploring the parameter space with different collider scenarios. Figure 44 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the reach using the full data set assumed for 33 and 100 TeV.

In general, we find that due to the small cross sections, it is very difficult to distinguish this model from background with discovery level significance. Consequentially, the discovery reach does not appear to significantly improve with the 14 TeV luminosity upgrade. The discovery reach increases by a factor of ~ 6 from 14 TeV to 100 TeV, but in absolute terms remains small. The exclusion reach for the compressed squark-neutralino model is more favorable in comparison. At this level of significance the background systematics are less difficult to overcome, and the limits scale much more favorably with luminosity and CM energy. For higher center-of-mass-energy, these searches specially targeted at the compressed region also become more and more important to fill in the gap in the reach of the untargeted search described in Sec. 5. Figure 44 makes a compelling case for investing in future proton colliders which can operate at these high energies.

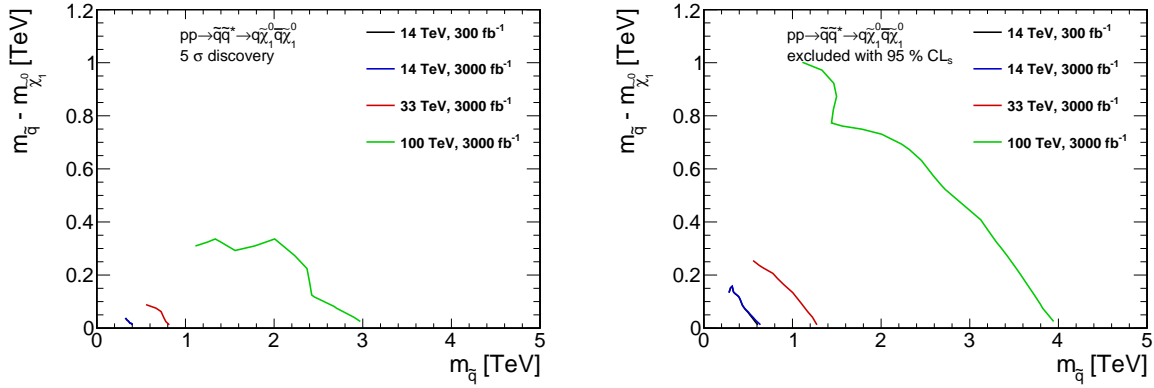


Figure 44: Results for the squark-neutralino model with light flavor decays for the analyses that target the compressed region of parameter space. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is not included.

7 The Gluino-Squark-Neutralino Model

In the “gluino-squark-neutralino model”, the gluino \tilde{g} and the first and second generation squarks \tilde{q} are all allowed to be kinematically accessible. The only relevant parameters are the squark mass $m_{\tilde{q}}$, which is taken to be universal for the first two generations, the gluino mass $m_{\tilde{g}}$, and the neutralino mass $m_{\tilde{\chi}^0}$. For this study we fix the neutralino mass $m_{\tilde{\chi}^0} = 1$ GeV, which captures the relevant kinematics for $m_{\tilde{g}}, m_{\tilde{q}} \gg m_{\tilde{\chi}^0}$. The decay mode is chosen depending on the mass hierarchy. The model is summarized as:

BSM particles	production	decay
$\tilde{g}, \tilde{q}, \tilde{\chi}_1^0$	$pp \rightarrow \tilde{g} \tilde{g}$	$\tilde{g} \rightarrow \begin{cases} \tilde{q} \bar{q} & \text{for } m_{\tilde{g}} > m_{\tilde{q}} \\ q \bar{q} \tilde{\chi}_1^0 & \text{for } m_{\tilde{g}} \simeq m_{\tilde{q}} \\ q \bar{q} \tilde{\chi}_1^0 & \text{for } m_{\tilde{g}} < m_{\tilde{q}} \end{cases}$
	$pp \rightarrow \tilde{g} \tilde{q}$	
	$pp \rightarrow \tilde{g} \tilde{q}^*$	
	$pp \rightarrow \tilde{q} \tilde{q}^*$	$\tilde{q} \rightarrow \begin{cases} q \tilde{\chi}_1^0 & \text{for } m_{\tilde{g}} > m_{\tilde{q}} \\ q \tilde{\chi}_1^0 & \text{for } m_{\tilde{g}} \simeq m_{\tilde{q}} \\ q \tilde{g} & \text{for } m_{\tilde{g}} < m_{\tilde{q}} \end{cases}$
	$pp \rightarrow \tilde{q} \tilde{q}$	

For a full MSSM model, which in particular would imply a specific neutralino composition, there will in general be a non-zero branching ratio for the squark to decay to a neutralino and a quark when kinematically allowed. If the decay directly to a gluino is kinematically allowed however it will tend to dominate, and in this study for simplicity we assume that the squark is weakly coupled to the neutralino and decays to the gluino proceed with 100% branching ratio when kinematically

allowed. Likewise for $m_{\tilde{g}} > m_{\tilde{q}}$, the branching ratio of the gluino to 3-body versus 2-body decays depends on the masses and coupling of the squarks to the neutralino, and we take the 2-body branching ratio to be 100% in this region of parameter space. To capture the transition region where $m_{\tilde{g}} \simeq m_{\tilde{q}}$, parameter choices along the line $m_{\tilde{g}} = m_{\tilde{q}}$ are included; the gluino decay is taken to be 3-body and the squarks are assumed to decay directly to the neutralino.

This model is a good proxy for comparing the power of searches which rely on the traditional jets and E_T^{miss} style hadron collider search strategy to discriminate against background. The final state ranges from two to four (or more) hard jets from the decay (depending on the production channel) and missing energy.

We simulated matched MadGraph samples for $(\tilde{g}\tilde{g})$, $(\tilde{q}\tilde{q}^*)$, $(\tilde{q}\tilde{q})$, $(\tilde{g}\tilde{q})$, $(\tilde{g}\tilde{q}^*)$ production with up to 2 additional generator level jets for the following points in parameter space:

BSM particles	masses
$m_{\tilde{g}} [14 \text{ TeV}]$	(315, 397, 500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989, 3489, 3989, 4489) GeV
$m_{\tilde{g}} [33 \text{ TeV}]$	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 4981, 5981, 6981, 7981, 8981, 9981) GeV
$m_{\tilde{g}} [100 \text{ TeV}]$	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 5012, 6310, 7944, 9944, 11944, 13944, 15944, 17944, 19944, 21944, 23944) GeV
$m_{\tilde{q}} [14 \text{ TeV}]$	(315, 397, 500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989, 3489, 3989, 4489) GeV
$m_{\tilde{q}} [33 \text{ TeV}]$	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 4981, 5981, 6981, 7981, 8981, 9981) GeV
$m_{\tilde{q}} [100 \text{ TeV}]$	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 5012, 6310, 7944, 9944, 11944, 13944, 15944, 17944, 19944, 21944, 23944) GeV
$m_{\tilde{\chi}_1^0}$	1 GeV

The signatures of this model are essentially a mixture of the gluino-neutralino and squark-neutralino Simplified Models except for slight variations in the kinematics due to the presence of on-shell states in the decays. Therefore, the dominant backgrounds will be the same as described in Sec. 3.1, and we use the same search strategy described in detail in Sec. 3.2. Again, based on the results of studying the effect of pile-up on this search strategy in Sec. 3.12, we present results only for the no pile-up scenario and expect that that pileup will not have a significant impact on the results.

When both the gluino and squarks are kinematically accessible, the total cross section for this Simplified Model is significantly enhanced with respect to the limit where either particle is decoupled due to the presence of the associated production channel $\tilde{g}\tilde{q}$ and also due to t -channel diagrams which open the important $\tilde{q}\tilde{q}^*$ channel and tend to dominate the $\tilde{q}\tilde{q}^*$ cross sections. It is important to note that even when the squarks or gluinos are kinematically inaccessible these t -channel processes still can dominate the cross section. For this reason the limits we obtain within the scanned range of gluino and squark masses do not reach the asymptotic values that can be inferred from the gluino-neutralino and squark-neutralino Simplified Models.

7.1 Analysis: 14 TeV

Figure 45 gives histograms for E_T^{miss} [left] and H_T [right] for two example models at the 14 TeV LHC. Comparing with the analogous gluino-neutralino (Fig. 2) and squark-neutralino (Fig. 28) distributions, it is clear that the total BSM cross section in this model is enhanced. This will lead to a significant improvement in mass reach with respect to the previous results.

The number of events that result from the cut flow used in this search are shown in Table 14. By comparing the optimal cuts which result from this analysis to the to the cuts employed for the gluino-neutralino model in Table 1 and the squark-neutralino model in Table 8, it is clear that the optimization procedure can take advantage of the the larger cross sections by utilizing significantly harder cuts.

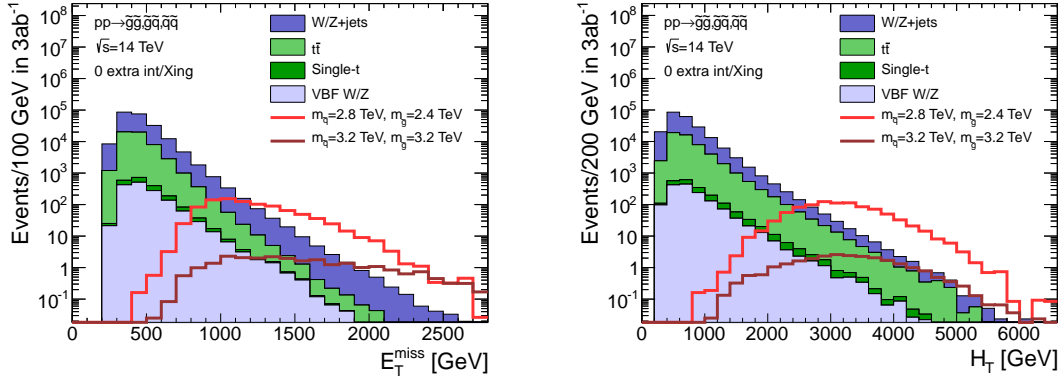


Figure 45: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of gluino-squark models at a 14 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut	V+jets	$t\bar{t}$	Total BG	$(m_{\tilde{g}}, m_{\tilde{q}})$ [TeV]	
				(2.4, 2.8)	(3.2, 3.2)
Preselection	2.07×10^7	2.47×10^7	4.54×10^7	2.75×10^3	136
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.45×10^5	1.20×10^5	5.65×10^5	1.34×10^3	109
$p_T^{\text{leading}} < 0.4 \times H_T$	1.69×10^5	5.16×10^4	2.21×10^5	937	25.4
$E_T^{\text{miss}} > 1250 \text{ GeV}$ $H_T > 3000 \text{ GeV}$	10.8	5	15.8	264	12.8
$E_T^{\text{miss}} > 1850 \text{ GeV}$ $H_T > 2850 \text{ GeV}$	1	0.2	1.2	30.5	6.1

Table 14: Number of expected events for $\sqrt{s} = 14 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected gluino and squark masses for the gluino-squark model with light flavor decays. The neutralino mass is 1 GeV. Two choices of cuts on E_T^{miss} and H_T are provided, and for each mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

7.2 Results: 14 TeV

The results for the gluino-squark-neutralino model are shown in Fig. 46. In the bulk of the parameter space, the 14 TeV LHC with 3000 fb^{-1} could discover a model with $m_{\tilde{g}} \simeq 3 \text{ TeV}$ and $m_{\tilde{q}} \simeq 3 \text{ TeV}$. When compared to the maximal reach for the gluino-neutralino model of $m_{\tilde{g}} \simeq 2.3 \text{ TeV}$ as shown in Fig. 3, the large cross section for the additional channels explains this $\sim 30\%$ improvement.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. We found the choice of gluino and squark masses which would yield a fixed number of events at 14 TeV and 300 fb^{-1} (3000 fb^{-1}) for three choices in the $m_{\tilde{q}} - m_{\tilde{g}}$ plane: there would be 10 events when $m_{\tilde{g}} = m_{\tilde{q}} = 3.5 \text{ TeV}$ (3.9 TeV); when $m_{\tilde{g}} = 2.7 \text{ TeV}$ (3.2 TeV) and the squark mass is at the edge of the region simulated; and when $m_{\tilde{q}} = 3.3 \text{ TeV}$ (3.9 TeV) and the gluino mass is at the edge of the region simulated. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 14 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 14 TeV 300 fb^{-1} limits are projected to be $m_{\tilde{g}} = m_{\tilde{q}} = 2.8$ (corresponding to 155 events); $m_{\tilde{g}} = 2.4 \text{ TeV}$ (corresponding to 43 events) and the squark mass is at the edge of the region simulated; $m_{\tilde{q}} = 2.1 \text{ TeV}$ (corresponding to 774 events) and the gluino mass is at the edge of the region simulated. The 14 TeV 3000 fb^{-1} limits are projected to be $m_{\tilde{g}} = m_{\tilde{q}} = 3.2$ (corresponding to 293 events); $m_{\tilde{g}} = 3.0 \text{ TeV}$ (corresponding to 23 events) and the squark mass is at the edge of the region simulated; $m_{\tilde{q}} = 2.7 \text{ TeV}$ (corresponding to 953 events) and the gluino mass is at the edge of the region simulated. Clearly the search does better with light gluinos. This is likely related to the four jet preselection requirement. It would be interesting to investigate to understand what additional search regions could be used to push the mass reach even further; this is beyond the scope of this work.

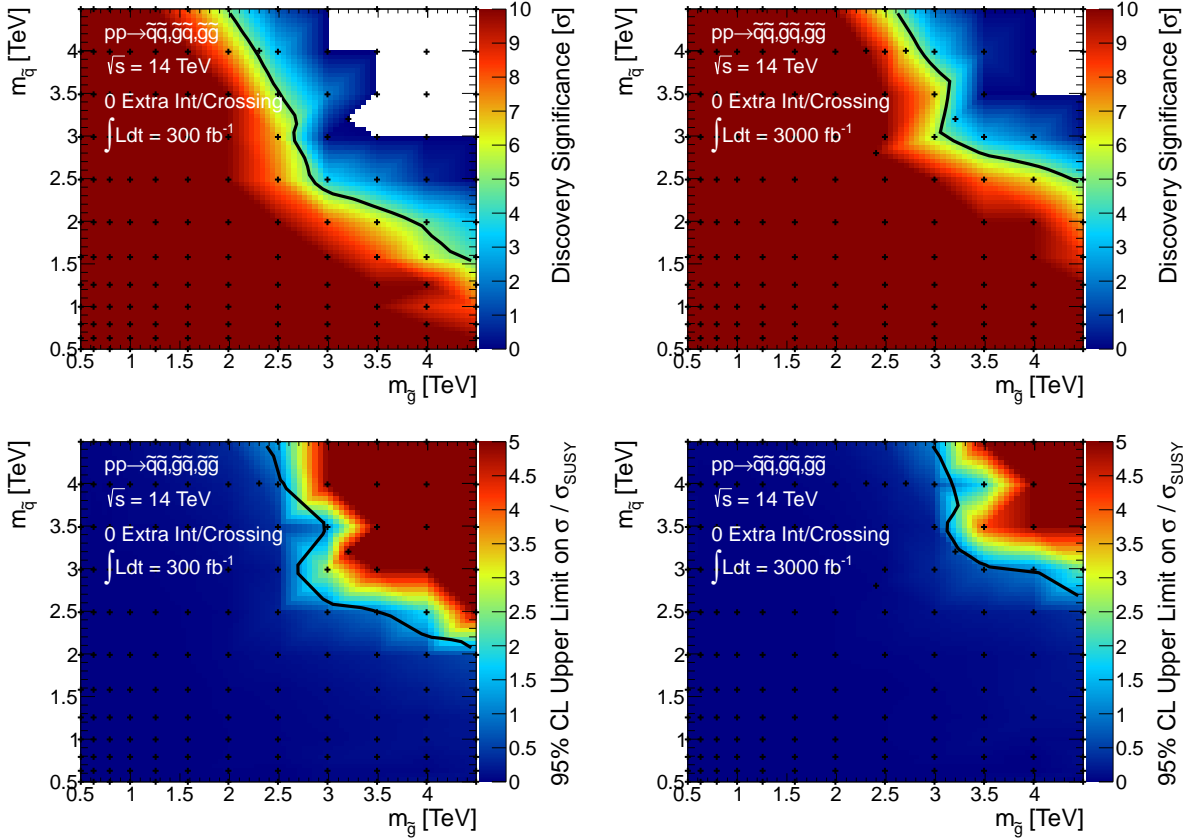


Figure 46: Results for the gluino-squark model with a massless neutralino are given in the $m_{\tilde{g}}$ versus $m_{\tilde{q}}$ plane. The top [bottom] row shows the expected 5σ discovery reach [95% confidence level upper limits] for the combined production channels at the 14 TeV LHC. Mass points to the left/below the contours are expected to be probed at 300 fb^{-1} [left] and 3000 fb^{-1} [right]. A 20% systematic uncertainty is assumed and pileup is not included.

7.3 Analysis: 33 TeV

Figure 47 gives histograms for E_T^{miss} [left] and H_T [right] for two example models at the 33 TeV LHC. Comparing with the analogous gluino-neutralino (Fig. 4) and squark-neutralino (Fig. 30) distributions, it is clear that the total BSM cross section in this model is enhanced. This will lead to a significant improvement in mass reach with respect to the previous results.

The number of events that result from the cut flow used in this search are shown in Table 15. By comparing the optimal cuts which result from this analysis to the cuts employed for the gluino-neutralino model in Table 2 and the squark-neutralino model in Table 9, it is clear that the optimization procedure can take advantage of the the larger cross sections by utilizing significantly harder cuts.

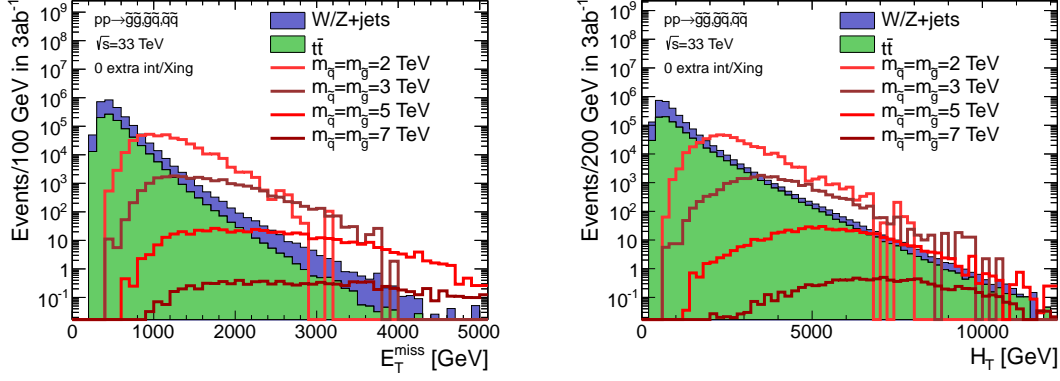


Figure 47: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of gluino-squark models at a 33 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut			Total BG	$(m_{\tilde{g}}, m_{\tilde{q}})$ [TeV]	
	V+jets	$t\bar{t}$		(3.2, 3.2)	(6.0, 6.0)
Preselection	1.55×10^8	2.86×10^8	4.42×10^8	8.64×10^4	361
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	4.50×10^6	1.93×10^6	6.44×10^6	6.55×10^4	321
$p_T^{\text{leading}} < 0.4H_T$	1.70×10^6	8.02×10^5	2.50×10^6	2.14×10^4	69.8
$E_T^{\text{miss}} > 2650 \text{ GeV}$ $H_T > 2700 \text{ GeV}$	60.4	16.4	76.8	1.79×10^3	40.1
$E_T^{\text{miss}} > 3700 \text{ GeV}$ $H_T > 5350 \text{ GeV}$	1.1	0.3	1.3	30.4	14.2

Table 15: Number of expected events for $\sqrt{s} = 33 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected gluino and squark masses for the gluino-squark model with light flavor decays. The neutralino mass is 1 GeV. Three choices of cuts on E_T^{miss} and H_T are provided, and for each mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

7.4 Results: 33 TeV

The results for the gluino-squark-neutralino model are shown in Fig. 48. In the bulk of the parameter space, a 33 TeV proton collider with 3000 fb^{-1} could discover a model with $m_{\tilde{g}} \simeq 6.5 \text{ TeV}$ and $m_{\tilde{q}} \simeq 6 \text{ TeV}$. When compared to the maximal reach for the gluino-neutralino model of $m_{\tilde{g}} \simeq 4.8 \text{ TeV}$ as shown in Fig. 5, the large cross section for the additional channels explains this $\sim 30\%$ improvement.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. We found the choice of gluino and squark masses which would yield a fixed number of events at 33 TeV and 3000 fb^{-1} for three choices in the $m_{\tilde{q}} - m_{\tilde{g}}$ plane: there would be 10 events when $m_{\tilde{g}} = m_{\tilde{q}} = 8.2 \text{ TeV}$; when $m_{\tilde{g}} = 6.1 \text{ TeV}$ and the squark mass is at the

edge of the region simulated; and when $m_{\tilde{q}} = 5.5$ TeV and the gluino mass is at the edge of the region simulated. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 33 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 33 TeV 3000 fb^{-1} limits are projected to be $m_{\tilde{g}} = m_{\tilde{q}} = 6.8$ (corresponding to 132 events); $m_{\tilde{g}} = 6.1$ TeV (corresponding to 21 events) and the squark mass is at the edge of the region simulated; $m_{\tilde{q}} = 5.5$ TeV (corresponding to 473 events) and the gluino mass is at the edge of the region simulated. Clearly the search does better with light gluinos. Furthermore, we find that we are closer to the ideal limit than in the 14 TeV case. Both of these facts are likely related to the four jet preselection requirement. While investigating the reach that could be extracted using additional search regions is beyond the scope of this work, it would be interesting to understand what it takes to push the mass reach even further.

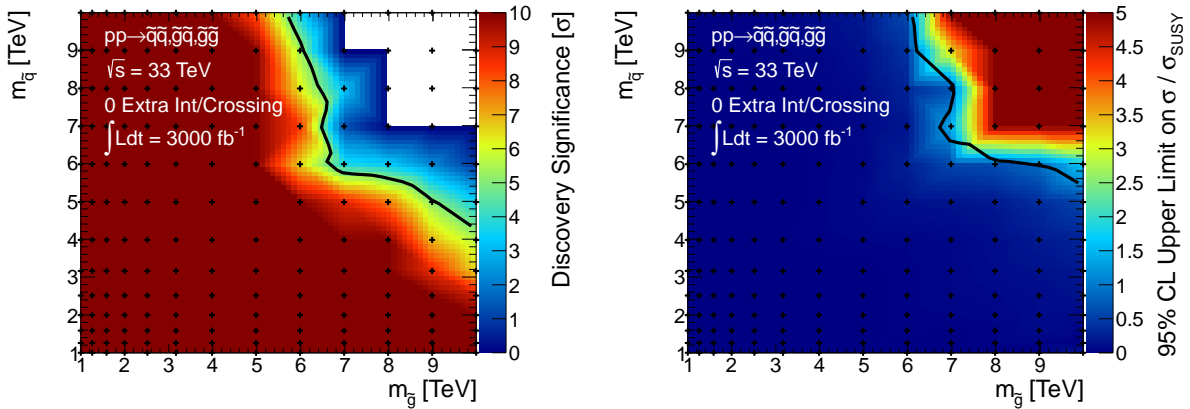


Figure 48: Results for the gluino-squark model with a massless neutralino are given in the $m_{\tilde{g}}$ versus $m_{\tilde{q}}$ plane. The left [right] panel shows the expected 5σ discovery reach [95% confidence level upper limits] for the combined production channels at a 100 TeV proton collider. Mass points to the left/below the contours are expected to be probed with 3000 fb^{-1} of data. A 20% systematic uncertainty is assumed and pileup is not included.

7.5 Analysis: 100 TeV

Figure 49 gives histograms for E_T^{miss} [left] and H_T [right] for two example models at a 100 TeV proton collider. Comparing with the analogous gluino-neutralino (Fig. 6) and squark-neutralino (Fig. 32) distributions, it is clear that the total BSM cross section in this model is enhanced. This will lead to a significant improvement in mass reach with respect to the previous results.

The number of events that result from the cut flow used in this search are shown in Table 16. Comparing the optimal cuts which result for this model to the cuts employed for the gluino-neutralino model in Table 3 and the squark-neutralino model in Table 10, it is clear that the optimization procedure can take advantage of the the larger cross sections by utilizing significantly harder cuts.

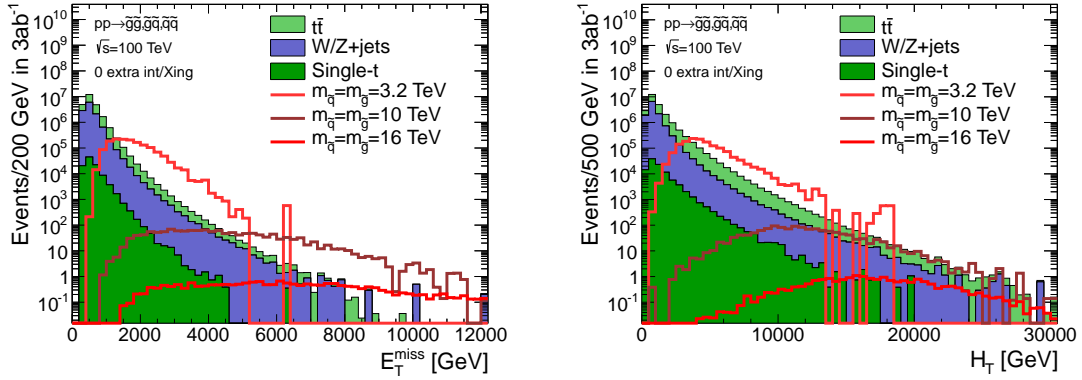


Figure 49: Histogram of E_T^{miss} [left] and H_T [right] after preselection cuts for background and a range of gluino-squark models at a 100 TeV proton collider. The neutralino mass is 1 GeV for all signal models.

Cut	Backgrounds			$(m_{\tilde{g}}, m_{\tilde{q}})$ [TeV]	
	V+jets	$t\bar{t}$	Total BG	(8, 8)	(16, 16)
Preselection	1.64×10^9	3.33×10^9	4.97×10^9	2.69×10^4	111
$E_T^{\text{miss}}/\sqrt{H_T} > 15 \text{ GeV}^{1/2}$	3.59×10^7	3.31×10^7	6.90×10^7	2.41×10^4	107
$p_T^{\text{leading}} < 0.4 \times H_T$	1.19×10^7	1.25×10^7	2.44×10^7	7.34×10^3	20.5
$E_T^{\text{miss}} > 5700 \text{ GeV}$ $H_T > 8000 \text{ GeV}$	13	14.9	27.8	771	12
$E_T^{\text{miss}} > 5800 \text{ GeV}$ $H_T > 17800 \text{ GeV}$	0.4	2.5	2.9	41.7	5.3

Table 16: Number of expected events for $\sqrt{s} = 100 \text{ TeV}$ with 3000 fb^{-1} integrated luminosity for the background processes and selected gluino and squark masses for the gluino-squark model with light flavor decays. The neutralino mass is 1 GeV. Two choices of cuts on E_T^{miss} and H_T are provided, and for each mass column the entry in the row corresponding to the “optimal” cuts is marked in red.

7.6 Results: 100 TeV

The results for the gluino-squark-neutralino model are shown in Fig. 50. In the bulk of the parameter space, a 100 TeV proton collider with 3000 fb^{-1} could discover a model with $m_{\tilde{g}} \simeq 16 \text{ TeV}$ and $m_{\tilde{q}} \simeq 14 \text{ TeV}$. When compared to the maximal reach for the gluino-neutralino model of $m_{\tilde{g}} \simeq 11 \text{ TeV}$ as shown in Fig. 7, the large cross section for the additional channels explains this $\sim 30\%$ improvement.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. The choice of gluino and squark masses which would yield a fixed number of events at 100 TeV and 3000 fb^{-1} for three choices in the $m_{\tilde{q}} - m_{\tilde{g}}$ plane: there would be 10 events when $m_{\tilde{g}} = m_{\tilde{q}} = 20.4 \text{ TeV}$; when $m_{\tilde{g}} = 16.5 \text{ TeV}$ and the squark mass is at the edge of the region simulated; and when $m_{\tilde{q}} = 19.6 \text{ TeV}$ and the gluino mass is at the edge of the region simulated. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 100 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 100 TeV 3000 fb^{-1} limits are projected to be $m_{\tilde{g}} = m_{\tilde{q}} = 16$ (corresponding to 136 events); $m_{\tilde{g}} = 16 \text{ TeV}$ (corresponding to 13 events) and the squark mass is at the edge of the region simulated; $m_{\tilde{q}} = 14 \text{ TeV}$ (corresponding to 169 events) and the gluino mass is at the edge of the region simulated. Clearly the search does better with light gluinos. Furthermore, we find that we are closer to the ideal limit than in the 14 TeV and 33 TeV cases. Both of these facts are likely related to the four jet preselection requirement. While investigating the reach that could be extracted using additional search regions is beyond the scope of this work, it would be interesting to understand what it takes to push the mass reach even further.

The next section provides a comparison of the impact that the four collider scenarios studied here can have on the parameter space of this model.

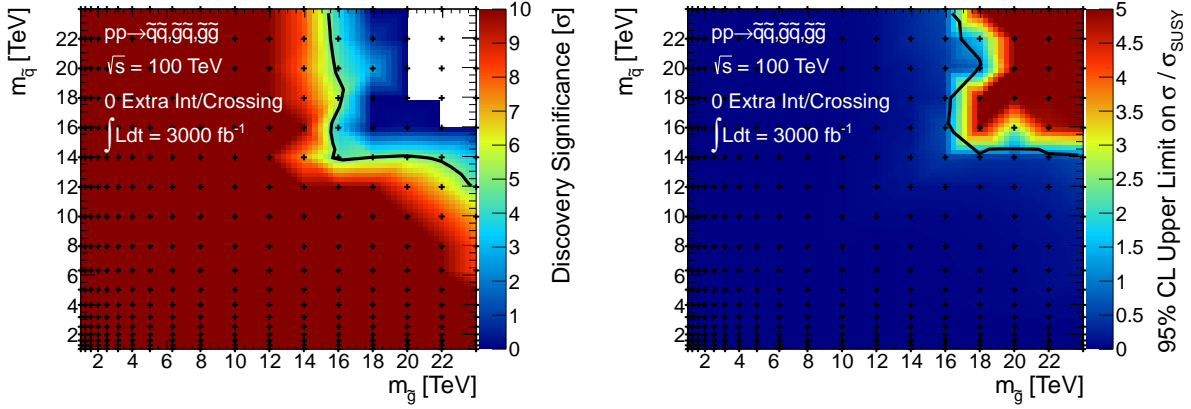


Figure 50: Results for the gluino-squark model with a massless neutralino are given in the $m_{\tilde{g}}$ versus $m_{\tilde{q}}$ plane. The left [right] panel shows the expected 5σ discovery reach [95% confidence level upper limits] for the combined production channels at a 100 TeV proton collider. Mass points to the left/below the contours are expected to be probed with 3000 fb^{-1} of data. A 20% systematic uncertainty is assumed and pileup is not included.

7.7 Comparing Colliders

The multi-jet plus E_T^{miss} signature of the gluino-squark-neutralino model with light flavor decays provides a useful case study with which to compare the potential impact of different proton colliders. Due to the large production cross sections, this model is also interesting as one of the most striking possible cases of accessible new physics. Figure 51 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the full data set assumed for 33 and 100 TeV. Because the high mass signal regions are relatively low-background for this model, a factor of 10 increase in luminosity leads to roughly a factor of 10 increase in cross-section reach at edges of the limits. In terms of mass reach, this corresponds roughly to a respectable 500 GeV improvement. Again increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space, since now much heavier gluinos can be produced without relying on the tails of parton distributions to supply the necessary energy. Figure 51 makes a compelling case for investing in future proton colliders which can operate at these high energies.

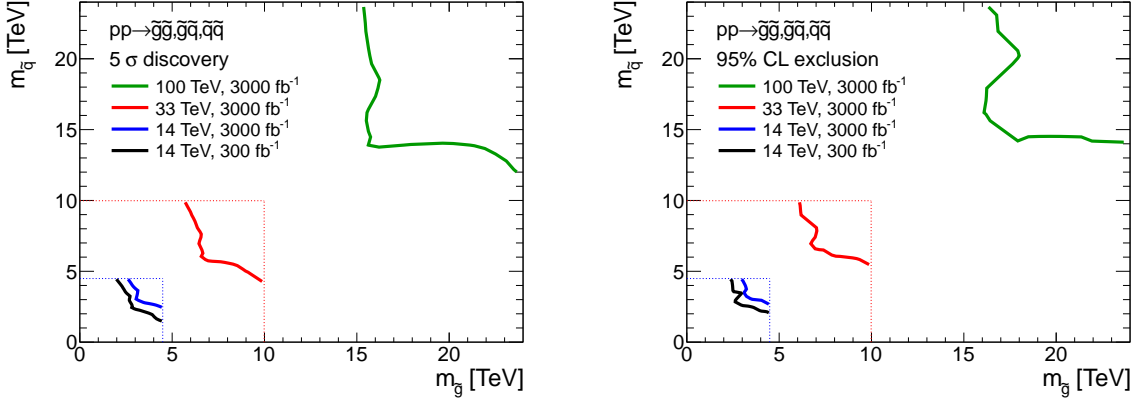


Figure 51: Results for the gluino-squark-neutralino model. The neutralino mass is taken to be 1 GeV. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is not included.

8 The Gluino-Neutralino Model with Heavy Flavor Decays

In the “gluino-neutralino model with heavy flavor decays”, the gluino \tilde{g} is the only kinematically accessible colored particle. The squarks are completely decoupled and do not contribute to gluino production diagrams. The gluino undergoes a prompt three-body decay through off-shell stops, $\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$, where t is the top quark and $\tilde{\chi}_1^0$ is a neutralino LSP. The only two relevant parameters are the gluino mass $m_{\tilde{g}}$ and the neutralino mass $m_{\tilde{\chi}_1^0}$. This model can be summarized by:

BSM particles	production	decays
$\tilde{g}, \tilde{\chi}_1^0$	$pp \rightarrow \tilde{g}\tilde{g}$	$\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$

This model has a variety of motivations. Perhaps the most compelling are “natural” SUSY scenarios [34–38], where the stop mass is assumed to be below the (stronger) bounds on first and second generation squark masses; for some examples of explicit constructions, see [39–45]. If both the stop and gluino are kinematically accessible for a given center-of-mass energy, the gluino would be visible above background before that of the stop; this Simplified Model reproduces the first signature of this paradigm. Note that in these models, the gluino decays involving on-shell stops. However, the final state are identical and the kinematics are similar enough that the reach is qualitatively reproduced by the results presented below.

There is also a class of split-SUSY models where the inaccessible stops are somewhat lighter than the other squarks — this Simplified Model acts as an excellent proxy for the first signatures of these scenarios. There are compelling reasons to believe this is a “preferred” spectrum. Renormalization group evolution tends to reduce the stop mass with respect to the first/second generation squarks (due to the large top Yukawa coupling) [46]. Also, assuming the MSSM, avoiding flavor and/or CP violation bounds would imply that the squarks have masses $\gtrsim 1000$ [47], while for $\tan\beta \gtrsim 2$ the stops would be lighter than $\mathcal{O}(100 \text{ TeV})$ [48] in order to yield a 125 GeV Higgs boson.

Finally, we note that this model is interesting from an experimental perspective. The model produces two $t\bar{t}$ pairs along with considerable E_T^{miss} (away from the compressed region of parameter space), and therefore provides an interesting benchmark scenario for searches involving a combination of hadronic activity, leptonic signatures and b-tagging. As described in detail below, a search which requires same-sign di-leptons (SSDL) is one viable approach to eliminating the SM background since this final state is highly suppressed in the SM. We note that this was the only channel explored in this scenario; it would be interesting to investigate how an all hadronic final state would perform at the higher energy machines.

We simulated matched MadGraph samples for $\tilde{g}\tilde{g}$ with up to 2 additional generator level jets for the following points in parameter space:⁴

BSM particles	masses
$m_{\tilde{g}}$ [14 TeV]	(315, 397, 500, 629, 792, 997, 1255, 1580, 1989, 2489, 2989, 3489) GeV
$m_{\tilde{g}}$ [33 TeV]	(500, 629, 792, 997, 1255, 1580, 1989, 2504, 3152, 3968, 4968, 5968, 6968) GeV
$m_{\tilde{g}}$ [100 TeV]	(1000, 1259, 1585, 1995, 2512, 3162, 3981, 5012, 6310, 7944, 9944, 11944, 13944, 15944) GeV
$m_{\tilde{\chi}_1^0}$	1 GeV (0.5, 0.7, 0.9) \times ($m_{\tilde{g}} - 2m_t$) $m_{\tilde{g}} - 2m_t - 10$ GeV

8.1 Dominant Backgrounds

The analysis used to derive the results below requires an SSDL pair, which is very efficient at eliminating backgrounds. The dominant background is top pair production, where both tops decay leptonically (the di-leptonic channel). There are subdominant backgrounds from Wbb , which are accounted for by including the *BJ* Snowmass particle container [7]. All backgrounds simulated for Snowmass are included and their rates are found to be negligible.

8.2 Analysis Strategy

The gluino-neutralino model with heavy flavor decays can be probed with an analysis that is inspired by the CMS collaboration in [49]. A SSDL pair is required and any remaining leptons are not allowed to form a Z -boson. Since the SSDL requirement is very effective at suppressing

⁴We include 1 GeV for an example where the neutralino is effectively massless; the second line of neutralino masses is chosen to cover the bulk of the gluino-neutralino plane; the final line is chosen to ensure coverage in the “compressed” region.

backgrounds, only mild cut on E_T^{miss} is necessary to observe this model. This implies that this search will also be very effective in the compressed regions of parameter space where $m_{\tilde{g}} \simeq m_{\tilde{\chi}_1^0}$.

In detail, our analysis strategy proceeds as follows:

PRESELECTION

- At least one SSDL pair
- At least two b -tagged jets
- The invariant mass of the SSDL pair > 12 GeV
- Veto an event where a third lepton ℓ_i reconstructs a Z -boson with either of the leptons from the SSDL pair ℓ_j : $76 \text{ GeV} < m_{\ell_i \ell_j} < 106 \text{ GeV}$ is vetoed
- $(H_T)_{\text{jets}} > 80 \text{ GeV}$
- $E_T^{\text{miss}} > 50 \text{ GeV}$

SEARCH STRATEGY: Define 8 signal regions

After preselection, the following are used as discriminating variables. Eight model points, three with very low LSP mass, three with medium LSP mass, and two with high LSP mass are used to define eight signal regions, which rely on some combination of the following cuts.

- symmetric $M_{T2} > (\text{symmetric } M_{T2})_{\text{optimal}}$
- $p_T > (p_T)_{\text{optimal}}$ for the hardest lepton
- $E_T^{\text{miss}} > (E_T^{\text{miss}})_{\text{optimal}}$
- $N_{\text{jets}} > (N_{\text{jets}})_{\text{optimal}}$
- $N_{b\text{-jets}} > (N_{b\text{-jets}})_{\text{optimal}}$
- $m_{\text{eff}} > (m_{\text{eff}})_{\text{optimal}}$
- $(H_T)_{\text{jets}} > ((H_T)_{\text{jets}})_{\text{optimal}}$

Symmetric M_{T2} is defined in the canonical way [50–52], where the SSDL pair is used for the visible signal and the invisible particle test mass is assumed to be zero; m_{eff} is defined as the scalar sum of the p_T of all visible objects and E_T^{miss} .

The goal is to attempt to provide as much total coverage in the Simplified Model plane as possible. Therefore, the cuts range from very stringent (for the light gluino mass/zero neutralino mass points) to very inclusive (for the compressed and heavy spectra). Approximate signal regions will be defined for each center-of-mass energy below. These provide a sense of how the cuts scale with luminosity and energy.

8.3 Analysis: 14 TeV

In this section, the signal regions are presented. The choice of cuts depends on the assumed integrated luminosity. Table 17 [18] provides the values that are relevant for the 300 fb^{-1} [3000 fb^{-1}] results. Also shown in these tables are number of events from the two dominant contributions to the background along with the total number of background events after cuts (including all contributions). When evaluating the gluino reach, we compute the signal efficiency after cuts for each signal region and use the one with the highest significance.

signal region	BSM masses	cuts	backgrounds	
SR1	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 250 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.025
			di-boson	0.37
			total	0.40
SR2	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 641 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 250 \text{ GeV}; \quad H_T \gtrsim 700 \text{ GeV}$ $m_{\text{eff}} \gtrsim 1000 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.025
			di-boson	0.37
			total	0.40
SR3	$m_{\tilde{g}} = 1580 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 300 \text{ GeV}; \quad H_T \gtrsim 800 \text{ GeV}$ $m_{\text{eff}} \gtrsim 1500 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.020
			di-boson	0.0064
			total	0.031
SR4	$m_{\tilde{g}} = 1580 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1224 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 600 \text{ GeV}; \quad m_{\text{eff}} \gtrsim 1500 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	di-boson	0.0064
			tri-boson	0.0003
			total	0.0067
SR5	$m_{\tilde{g}} = 2489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$H_T \gtrsim 2000 \text{ TeV}; \quad m_{\text{eff}} \gtrsim 2500 \text{ GeV}$ $N_{\text{jets}} > 7$	$t\bar{t}$	0.0072
			di-boson	0.013
			total	0.022
SR6	$m_{\tilde{g}} = 2489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 2133 \text{ GeV}$	$N_{\text{jets}} > 7; \quad N_b > 2$	tW	0.96
			di-boson	0.77
			total	2.1
SR7	$m_{\tilde{g}} = 3489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	sym- $M_{T2} \gtrsim 400 \text{ GeV}$ $N_{\text{jets}} > 7$	$t\bar{t}$	0.021
			total	0.021
SR8	$m_{\tilde{g}} = 3489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 3133 \text{ GeV}$	$N_{\text{jets}} > 7$	$t\bar{t}$	0.39
			di-boson	1.1
			total	1.8

Table 17: The eight signal regions defined for the SSDL 14 TeV 300 fb^{-1} search. Also shown are the dominant two contributions to the background along with the total background after cuts, which also includes all subdominant backgrounds.

signal region	BSM masses	cuts	backgrounds	
SR1	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 250 \text{ GeV}; \quad H_T \gtrsim 500 \text{ GeV}$ $m_{\text{eff}} \gtrsim 1000 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 60 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.061
			tW	0.019
			total	0.086
SR2	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 641 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 150 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 60 \text{ GeV}$ $N_{\text{jets}} > 4; \quad N_b > 2$	$t\bar{t}$	0.87
			di-boson	0.15
			total	1.04
SR3	$m_{\tilde{g}} = 1580 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 250 \text{ GeV}; \quad H_T \gtrsim 700 \text{ GeV}$ $m_{\text{eff}} \gtrsim 1500 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 50 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.061
			tri-boson	0.0053
			total	0.069
SR4	$m_{\tilde{g}} = 1580 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1224 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 150 \text{ GeV}; \quad m_{\text{eff}} \gtrsim 500 \text{ GeV}$ $\text{sym-}M_{T2} \gtrsim 60 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.061
			tW	0.019
			total	0.088
SR5	$m_{\tilde{g}} = 2489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 250 \text{ GeV}; \quad H_T \gtrsim 1000 \text{ GeV}$ $m_{\text{eff}} \gtrsim 2000 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 180 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	tW	0.013
			total	0.013
SR6	$m_{\tilde{g}} = 2489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 2133 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 150 \text{ GeV}; \quad H_T \gtrsim 300 \text{ GeV}$ $m_{\text{eff}} \gtrsim 500 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	0.14
			tri-boson	0.15
			total	0.35
SR7	$m_{\tilde{g}} = 3489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 100 \text{ GeV}; \quad H_T \gtrsim 1000 \text{ GeV}$ $m_{\text{eff}} \gtrsim 2000 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 100 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	tri-boson	0.0027
			total	0.0027
SR8	$m_{\tilde{g}} = 3489 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 3133 \text{ GeV}$	$H_T \gtrsim 200 \text{ GeV}; \quad m_{\text{eff}} \gtrsim 400 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	1.1
			tW	4.7
			total	6.3

Table 18: The eight signal regions defined for the SSDL 14 TeV 3000 fb^{-1} search. Also shown are the dominant two contributions to the background along with the total background after cuts, which also includes all subdominant backgrounds.

8.4 Results: 14 TeV

Using the signal regions outlined in the previous section, we determine the ability of the 14 TeV LHC to probe this model in the SSDL channel. These results are presented in Fig. 52, where we show the 95% CL exclusion [solid line] and the 5σ discovery contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. A 20% systematic uncertainty has been assumed for the background. Also shown on the bottom row of this figure are the results without including pileup. The dominant effect of pileup on this analysis is that it can contaminate the lepton isolation cones, thereby reducing the signal strength. At 14 TeV this effect is significant only in the high mass compressed region, where it slightly weakens the limits.

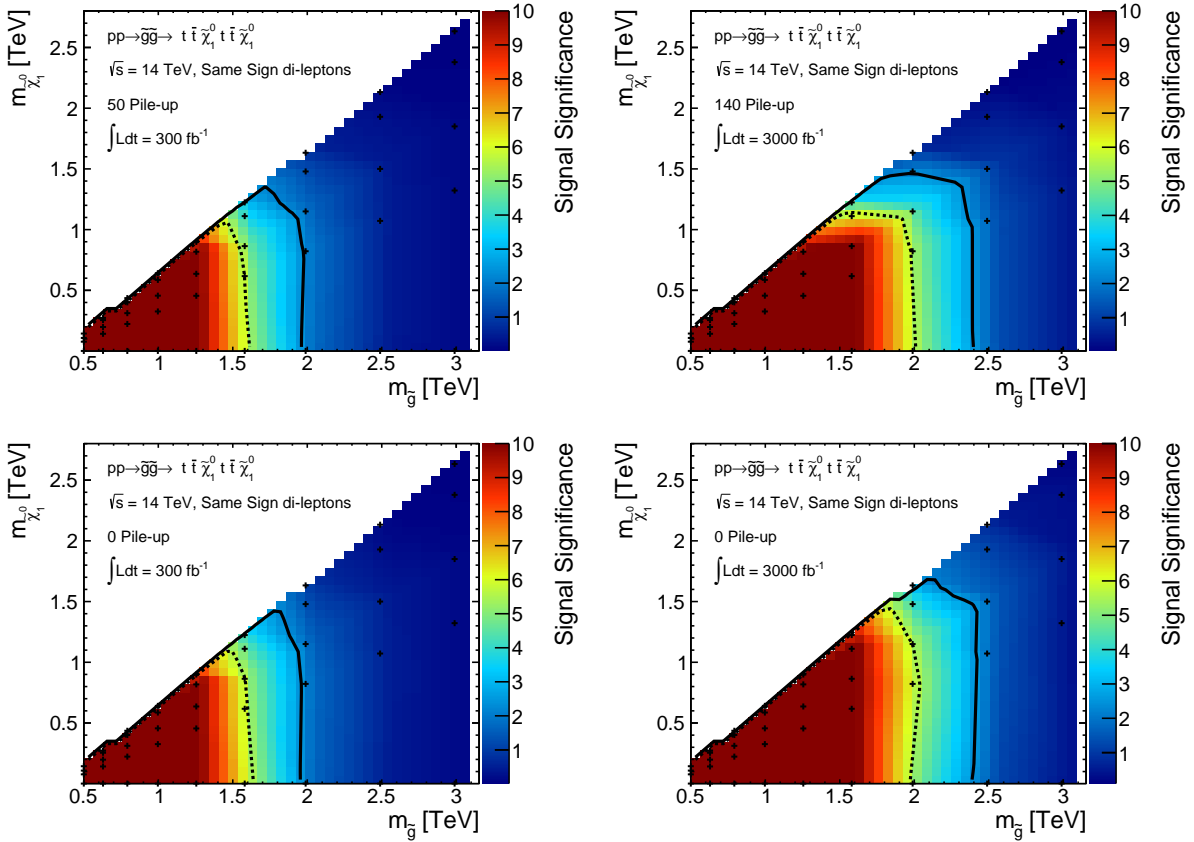


Figure 52: Results for the gluino-neutralino model with heavy flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The solid [dotted] lines shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at the 14 TeV LHC using 300 fb^{-1} [left] and 3000 fb^{-1} [right] of integrated luminosity. A 20% systematic uncertainty is assumed. The 300 fb^{-1} result on the left includes an average of 50 pileup events; the 3000 fb^{-1} result on the right includes an average of 140 pileup events. The results on the bottom do not include the effects of pileup.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of gluino mass which would yield

10 SSDL events (accounting for the leptonic branching ratios) at 300 fb^{-1} (3000 fb^{-1}) is 2.3 TeV (2.8 TeV). This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 14 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 14 TeV 300 fb^{-1} limit is projected to be 1.9 TeV (corresponding to 73 events), and the 3000 fb^{-1} limit is projected to be 2.4 TeV (corresponding to 67 events). Finally, we note that the 14 TeV LHC with 3000 fb^{-1} could discover a gluino (with $\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$) as heavy as 2.0 TeV if the neutralino is massless. Note that due to the relatively weak cuts that can be placed on E_T^{miss} , the SSDL signal is robust against models with almost degenerate gluino and neutralino.

8.5 Analysis: 33 TeV

In this section, the signal regions are presented for the SSDL search at 33 TeV assuming 3000 fb^{-1} . Table 19 provides the values from an optimization for 3000 fb^{-1} of data. Also shown in these tables are number of events from the two dominant contributions to the background along with the total number of background events after cuts (including all contributions). When evaluating the gluino reach, we compute the signal efficiency after cuts for each signal region and use the one with the highest significance.

signal region	BSM masses	cuts	backgrounds	
SR1	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 100 \text{ GeV}; \quad m_{\text{eff}} > 1000 \text{ GeV}$ $H_T \gtrsim 500 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 40 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	19
			di-boson	0.17
			total	19.2
SR2	$m_{\tilde{g}} = 997 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 641 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 50 \text{ GeV}; \quad H_T \gtrsim 400 \text{ GeV}$ $m_{\text{eff}} \gtrsim 700 \text{ GeV}$ $N_{\text{jets}} > 5; \quad N_b > 2$	$t\bar{t}$	460
			di-boson	9.2
			total	470
SR3	$m_{\tilde{g}} = 1989 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 500 \text{ GeV}; \quad H_T \gtrsim 1500 \text{ GeV}$ $m_{\text{eff}} \gtrsim 2200 \text{ GeV}; \quad \text{sym-}M_{T2} \gtrsim 200 \text{ GeV}$ $N_{\text{jets}} > 7; \quad N_b > 2$	$t\bar{t}$	0.081
			tri-boson	0.0062
			total	0.087
SR4	$m_{\tilde{g}} = 1989 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1633 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 600 \text{ GeV}; \quad m_{\text{eff}} \gtrsim 3000 \text{ GeV}$ $N_{\text{jets}} > 7; \quad N_b > 2$	$t\bar{t}$	0.20
			tj	0.035
			total	0.26
SR5	$m_{\tilde{g}} = 3152 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 1000 \text{ GeV}; \quad m_{\text{eff}} \gtrsim 2000 \text{ GeV}$ $\text{sym-}M_{T2} \gtrsim 300 \text{ GeV}$ $N_{\text{jets}} > 7; \quad N_b > 2$	tri-boson	0.0062
			total	0.0062
SR6	$m_{\tilde{g}} = 3152 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 2796 \text{ GeV}$	$N_{\text{jets}} > 7; \quad N_b > 3$	$t\bar{t}$	2.9
			tj	0.12
			total	3.0
SR7	$m_{\tilde{g}} = 4968 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 100 \text{ GeV}; \quad H_T \gtrsim 800 \text{ GeV}$ $m_{\text{eff}} \gtrsim 1500 \text{ GeV}$ $N_{\text{jets}} > 7; \quad N_b > 1$	$t\bar{t}$	390
			di-boson	0.75
			total	400
SR8	$m_{\tilde{g}} = 4968 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 4612 \text{ GeV}$	$m_{\text{eff}} \gtrsim 400 \text{ GeV}; \quad H_T \gtrsim 150 \text{ GeV}$ $\text{sym-}M_{T2} \gtrsim 100 \text{ GeV}$ $N_{\text{jets}} > 7; \quad N_b > 2$	$t\bar{t}$	1.6
			tj	0.12
			total	1.8

Table 19: The eight signal regions defined for the SSDL 33 TeV 3000 fb^{-1} search. Also shown are the dominant two contributions to the background along with the total background after cuts, which also includes all subdominant backgrounds.

8.6 Results: 33 TeV

Using the signal regions outlined in the previous section, we determine the ability of the 33 TeV LHC to probe this model in the SSDL channel. These results are presented in Fig. 53, where we show the 95% CL exclusion [solid line] and the 5σ discovery contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. A 20% systematic uncertainty has been assumed for the background. Also shown in the right panel of this figure are the results without including pileup. The dominant effect of pileup on this analysis is that it can contaminate the lepton isolation cones, thereby reducing the signal strength. As we go to higher CM energy colliders the min bias events have higher p_T and begin to affect the lepton isolation more significantly. At 33 TeV, in contrast with 14 TeV, we find a small change in the overall reach and a substantial change in the reach for the high mass compressed region.

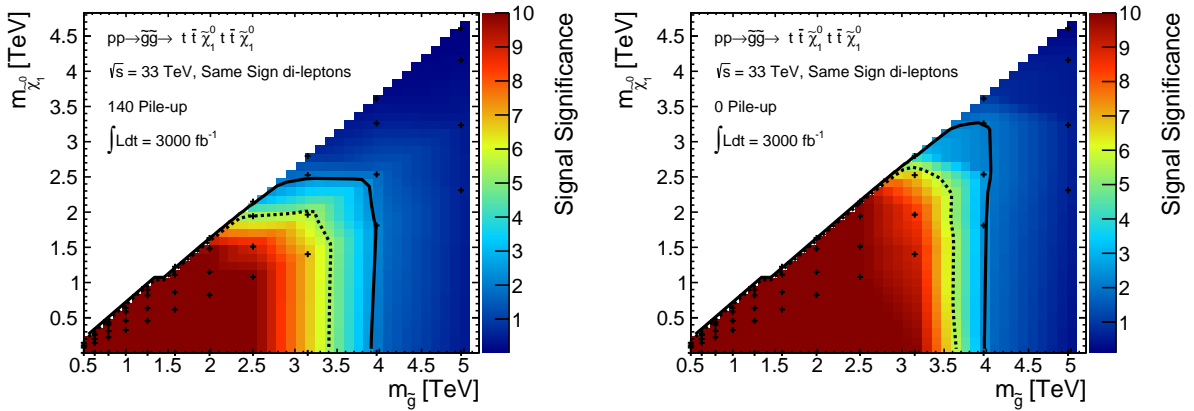


Figure 53: Results for the guino-neutralino model with heavy flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The solid [dotted] lines shows the expected 5σ discovery reach [95% CL upper limits] for guino pair production. Mass points to the left/below the contours are expected to be probed at a 33 TeV proton collider using 3000 fb^{-1} of integrated luminosity. A 20% systematic uncertainty is assumed. For the figure on the left [right], an average of 140 [0] pileup events are included.

Using the NLO squark pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of guino mass which would yield 10 SSDL events, *i.e.*, appropriately accounting for the branching ratio, at 3000 fb^{-1} is 5.5 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 33 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 33 TeV 3000 fb^{-1} limit is projected to be 4.0 TeV (corresponding to 243 events). Finally, we note that a 33 TeV proton collider with 3000 fb^{-1} could discover a guino (with $\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$) as heavy as 3.4 TeV if the neutralino is massless. Note that due to the relatively weak cuts that can be placed on E_T^{miss} , the SSDL signal is robust against models with almost degenerate guino and neutralino.

8.7 Analysis: 100 TeV

In this section, the signal regions are presented for the SSDL search at 100 TeV assuming 3000 fb^{-1} . Table 20 provides the values from an optimization for 3000 fb^{-1} of data. Also shown in these tables are number of events from the two dominant contributions to the background along with the total number of background events after cuts (including all contributions). When evaluating the gluino reach, we compute the signal efficiency after cuts for each signal region and use the one with the highest significance.

signal region	BSM masses	cuts	backgrounds	
SR1	$m_{\tilde{g}} = 1995 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 400 \text{ GeV}; H_T \gtrsim 1500 \text{ GeV}$ $m_{\text{eff}} \gtrsim 2000 \text{ GeV}; \text{sym-}M_{T2} \gtrsim 100 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 3$	$t\bar{t}$	0.53
			total	0.53
SR2	$m_{\tilde{g}} = 1995 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1639 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 400 \text{ GeV}; H_T \gtrsim 1200 \text{ GeV}$ $m_{\text{eff}} \gtrsim 2000 \text{ GeV}; \text{sym-}M_{T2} \gtrsim 100 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 3$	$t\bar{t}$	0.53
			total	0.53
SR3	$m_{\tilde{g}} = 3981 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 1200 \text{ GeV}; H_T \gtrsim 3500 \text{ GeV}$ $m_{\text{eff}} \gtrsim 4500 \text{ GeV}; \text{sym-}M_{T2} \gtrsim 350 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 2$	$t\bar{t}$	0.60
			total	0.60
SR4	$m_{\tilde{g}} = 3981 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 3625 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 1200 \text{ GeV}; H_T \gtrsim 4000 \text{ GeV}$ $m_{\text{eff}} \gtrsim 5000 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 2$	$t\bar{t}$	0.85
			tW	0.14
			total	1.0
SR5	$m_{\tilde{g}} = 7944 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 800 \text{ GeV}; H_T \gtrsim 3000 \text{ GeV}$ $m_{\text{eff}} \gtrsim 5000 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 2$	$t\bar{t}$	3.6
			tW	0.20
			total	3.8
SR6	$m_{\tilde{g}} = 7944 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 7588 \text{ GeV}$	$H_T \gtrsim 400 \text{ GeV}; m_{\text{eff}} \gtrsim 800 \text{ GeV}$ $N_{\text{jets}} > 7; N_b > 2$	$t\bar{t}$	8100
			tW	190
			total	8300
SR7	$m_{\tilde{g}} = 15944 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 1 \text{ GeV}$	$E_T^{\text{miss}} \gtrsim 500 \text{ GeV}; H_T \gtrsim 4000 \text{ GeV}$ $m_{\text{eff}} \gtrsim 6000 \text{ GeV}$ $N_{\text{jets}} > 5; N_b > 1$	$t\bar{t}$	45
			single boson	1.8
			total	50
SR8	$m_{\tilde{g}} = 15944 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 15588 \text{ GeV}$	$H_T \gtrsim 200 \text{ GeV}; m_{\text{eff}} \gtrsim 400 \text{ GeV}$ $\text{sym-}M_{T2} \gtrsim 100 \text{ GeV}$ $N_{\text{jets}} > 5; N_b > 2$	$t\bar{t}$	2200
			tW	16
			total	2200

Table 20: The eight signal regions defined for the SSDL 100 TeV 3000 fb^{-1} search. Also shown are the dominant two contributions to the background along with the total background after cuts, which also includes all subdominant backgrounds.

8.8 Results: 100 TeV

Using the signal regions outlined in the previous section, we determine the ability of the 100 TeV LHC to probe this model in the SSDL channel. These results are presented in Fig. 54, where we show the 95% CL exclusion [solid line] and the 5σ discovery contours in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. A 20% systematic uncertainty has been assumed for the background. Also shown in the right panel of this figure are the results without including pileup. The dominant effect of pileup on this analysis is that it can contaminate the lepton isolation cones, thereby reducing the signal strength. As we go to higher CM energy colliders the min bias events have higher p_T and begin to affect the lepton isolation more significantly. At 100 TeV, this effect is significant enough to decrease the limits on the gluino mass in this analysis by almost 1 TeV. Note that the lepton isolation cuts were not optimized for the higher pile-up and CM energy environments in this study; an interesting direction for future work would be to study how this issue can be ameliorated.

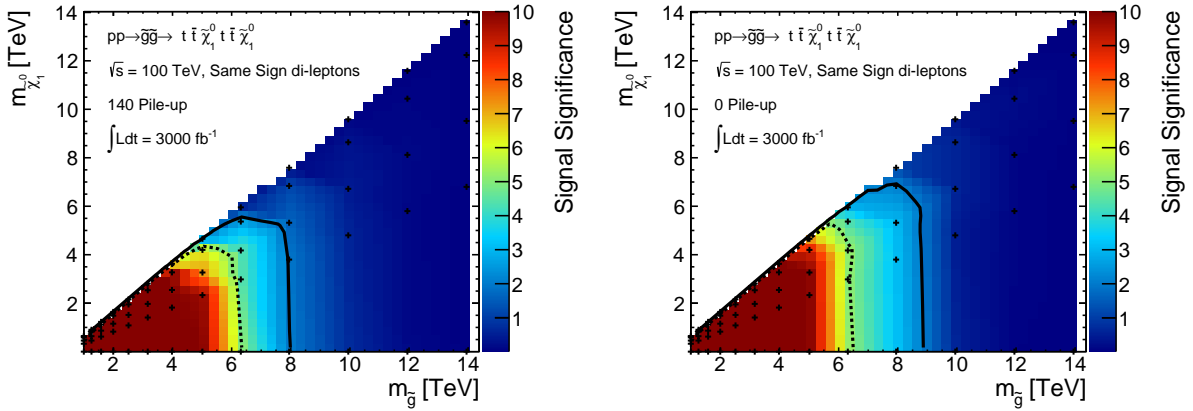


Figure 54: Results for the gluino-neutralino model with heavy flavor decays are given in the $m_{\tilde{\chi}_1^0}$ versus $m_{\tilde{g}}$ plane. The solid [dotted] lines shows the expected 5σ discovery reach [95% confidence level upper limits] for gluino pair production. Mass points to the left/below the contours are expected to be probed at a 100 TeV proton collider using 3000 fb^{-1} of integrated luminosity. A 20% systematic uncertainty is assumed. For the figure on the left [right], an average of 140 [0] pileup events are included.

Using the NLO gluino pair production cross section one can make a very naive estimate for the reach of a given collider. For example, we find that the choice of gluino mass which would yield 10 SSDL events at 3000 fb^{-1} is 12.7 TeV. This roughly corresponds to the maximal possible reach one could expect for a given luminosity using 100 TeV proton collisions.

Using a realistic simulation framework along with the search strategy employed here the 100 TeV 3000 fb^{-1} limit is projected to be 8.8 TeV (corresponding to 224 events). Finally, we note that a 100 TeV proton collider with 3000 fb^{-1} could discover a gluino (with $\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$) as heavy as 6.4 TeV if the neutralino is massless. Note that due to the relatively weak cuts that can be placed on E_T^{miss} , the SSDL signal is robust against models with almost degenerate gluino and neutralino.

8.9 Comparing Colliders

The same-sign di-lepton signature of the gluino-neutralino model with heavy flavor decays provides a useful case study with which to compare the potential impact of different proton colliders. Due to theoretical motivation in the context of both natural SUSY and split SUSY models, this final state is a very important signature of new physics to consider. Figure 55 shows the 5σ discovery reach [95% CL exclusion] for two choices of integrated luminosity at 14 TeV, along with the full data set assumed for 33 and 100 TeV. At the LHC, a factor of 10 increase in luminosity leads to an improved reach of roughly 500 GeV. Increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space, since now much heavier gluinos can be produced without relying on the tails of parton distributions to supply the necessary energy. Figure 55 makes a compelling case for investing in future proton colliders which can operate at these high energies.

Note that studying other final states for this decay channel was outside the scope of this project. In light of these results though, it would be interesting to see if an all hadronic search would lead to improvements in the projected limits, especially since lepton efficiencies are significantly affected at high CM energies by the pile-up conditions and the highly boosted top quarks, and similarly to veto τ -tagged jets to further reduce W/Z +jets. In particular, when considering searches at a 100 TeV collider, it would be interesting to investigate the fat top jet signatures of this model with very heavy gluinos.

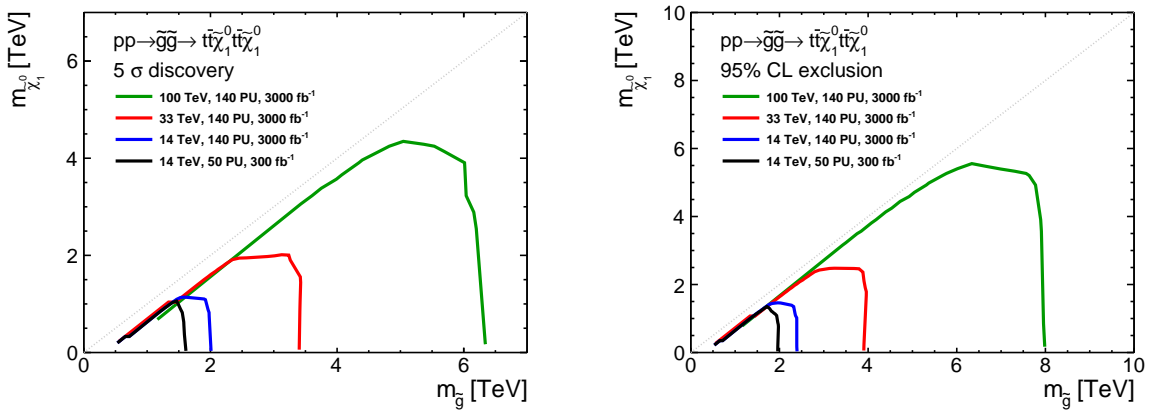


Figure 55: Results for the gluino-squark-neutralino model. The neutralino mass is taken to be 1 GeV. The left [right] panel shows the 5σ discovery reach [95% CL exclusion] for the four collider scenarios studied here. A 20% systematic uncertainty is assumed and pileup is included.

9 Outlook

Particle accelerators are one of the primary tools for experimentally investigating questions related to the microscopic properties of our Universe. Given the 20+ year time scale required to build one of these machines, it is important to think carefully about their physics capabilities. A wide variety of studies are required for making informed decisions on the machine requirements such as center-of-mass energy, instantaneous and integrated luminosity; issues related to detailed detector design specifications must also be addressed.

This paper presents some of the first comprehensive comparisons between the upcoming 14 TeV run of the CERN Large Hadron Collider and future possible experiments (for other recent studies see [12–21]). This includes a high-luminosity program at 14 TeV, and experiments that will collide protons at energies between ~ 33 and ~ 100 TeV. Our goal was to obtain the best limits possible with generic, signature-based searches that are not overly tuned to specific models.

We assessed the physics potential of these collider scenarios by performing analyses using Monte Carlo samples for signals and backgrounds with a realistic detector model. Results obtained with a fast detector simulation provide a complimentary estimate to a simple rescaling of existing limits, where the 8 TeV search strategies could be more sophisticated or involve more signal regions than the approaches taken here. Performing searches on Monte Carlo also provides insight into the impact of effects such as systematic uncertainties and pileup as a function of the center-of-mass energy.

In particular, we studied the reach for four SUSY Simplified Models whose experimental signatures are driven by the production of colored states. Three analysis strategies were employed in deriving these projections: a jets + E_T^{miss} analysis which optimized over H_T and E_T^{miss} , a mono-jet analysis with either an inclusive or exclusive jet requirement, and a same-sign di-lepton search. Table 21 shows the discovery potential [exclusion reach] for the different collider scenarios.

The results clearly demonstrate that these machines can have a substantial impact on our understanding of the parameter space of these models. They also address several big-picture questions when comparing colliders. In particular, it is possible to understand “how do analyses scale between these different machines?” by studying this work.

One example of how collider physics evolves as one moves to higher \sqrt{s} is seen in the composition of the jets + E_T^{miss} backgrounds. This was most obvious in the $\tilde{g} \rightarrow q\bar{q}\chi_1^0$ study of Sec. 3, where the dominant background was W/Z + jets at 14 TeV, but became $t\bar{t}$ at 100 TeV. Another important lesson was illustrated in using the same-sign di-lepton approach to the $\tilde{g} \rightarrow t\bar{t}\chi_1^0$ final state, where it was clear that the impact of pileup changed significantly between 14 TeV and 100 TeV. In particular, it is likely that lepton isolation requirements will need to evolve to cope with higher p_T objects and harder pileup interactions at high \sqrt{s} .

Simplified Model	14 TeV 300 fb ⁻¹	14 TeV 3000 fb ⁻¹	33 TeV	100 TeV
$\tilde{g} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	1.9 TeV [2.3 TeV]	2.2 TeV [2.7 TeV]	5.0 TeV [5.8 TeV]	11 TeV [13.5 TeV]
$\tilde{g} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{g}} \simeq m_{\tilde{\chi}_1^0}$	0.75 TeV [0.9 TeV]	0.9 TeV [1.0 TeV]	1.5 TeV [1.8 TeV]	4.6 TeV [5.5 TeV]
$\tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	0.80 TeV [1.5 TeV]	0.9 TeV [1.7 TeV]	1.4 TeV [3.4 TeV]	2.4 TeV [8.0 TeV]
$\tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{q}} \simeq m_{\tilde{\chi}_1^0}$	0.45 TeV [0.65 TeV]	0.45 TeV [0.70 TeV]	0.80 TeV [1.3 TeV]	3.0 TeV [3.9 TeV]
$\tilde{g} - \tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{g}} \simeq m_{\tilde{q}}$ and $m_{\tilde{\chi}_1^0} \simeq 0$	2.7 TeV [2.8 TeV]	3.0 TeV [3.2 TeV]	6.6 TeV [6.8 TeV]	15.5 TeV [16 TeV]
$\tilde{g} - \tilde{\chi}_1^0$ heavy flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	1.6 TeV [1.9 TeV]	2.0 TeV [2.4 TeV]	3.4 TeV [3.9 TeV]	6.3 TeV [8.8 TeV]

Table 21: This table summarizes the expected discovery reach [95% CL limits] as computed using the search strategies employed in this study.

There are many exciting opportunities for progress. This paper provides a concrete starting point for understanding the new physics potential of experiments that would collide protons at energies approaching the boundary of what humans can hope to achieve. By providing a quantitative analysis of several SUSY Simplified Models, these results help define many challenges and opportunities for future hadron colliders.

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Appendix: Simulation Framework

This appendix is devoted to the details of our simulation procedure for the signal events. The publicly available Snowmass backgrounds [7] were used for all Standard Model Monte Carlo events.

Unless otherwise specified we applied the following systematic uncertainties to all analyses:

- luminosity: 2.8%
- PDF uncertainty: 5%
- signal acceptance: 15%
- background normalization: 20%

Parton level events were generated using `Madgraph5 v1.5.10` [53]. All signals involve the pair production of SUSY particles and are matched using MLM matching up to 2 additional jets. The k_T -ordered shower scheme with a matching scale of $q_{\text{cut}}=xq_{\text{cut}}=100$ GeV was used. Note that we do not account for any possible inadequacies inherent in the current Monte Carlo technology, *e.g.* electroweak gauge bosons are not included in the shower.

The gluinos and squarks were treated as stable at the parton level. These events were subsequently decayed and showered using `Pythia6` [54] and passed through the `Delphes` detector simulation [55] using the “Snowmass” detector parameter card [9]. Total production cross sections were computed at NLO using a modified version of `Prospino v2.1` [56–58].

It proved to be advantageous to use a weighted event procedure. In particular, it was our goal to accurately model the tails of the distributions in the compressed region which is notoriously difficult to simulate. To this end we used a variation of the procedure developed for the Snowmass Standard Model background generation [7]. Since the only jets at the parton level were due to ISR,

we could use generator level H_T variable which is built into Madgraph5. We will refer to cuts on this variable as `htmin`, `htmax`. This allowed us to bin events in “recoil” due to the presence of ISR — these are exactly the types of events which contribute in the compressed region.

In detail, the process for each parameter point is:

1. *Compute the approximate differential cross section with respect to H_T .* We run Madgraph in “survey” mode (using the command `bin/madevent survey`) while incrementing the `htmin` cut to determine the cross section as a function of this cut, $\sigma_i \equiv \sigma(H_T > \text{htmin}_i)$ with

$$\text{htmin}_{i=0\dots n} = \{0 \text{ GeV}, 100 \text{ GeV}, 200 \text{ GeV}, \dots\}$$

We find that subsequent steps of 100 GeV provide an accurate enough characterization of the cross section for our purposes. We increase the cut until $\sigma_i < 1/\mathcal{L}$ where \mathcal{L} is the luminosity for which good statistics are desired. The differential cross section is calculated from the differences:

$$d\sigma_i = \sigma_{i+1} - \sigma_i.$$

2. *Determine bins of H_T for event generation.* We define $\text{bin}_{\alpha=1\dots m}$ by $\text{htmin}_\alpha \leq H_T < \text{htmax}_\alpha$. We choose bin edges based on a “weight fraction” x with $0 < x \leq 1$ as follows:

- (a) The lower edge of the first bin is $\text{htmin}_1 = 0 \text{ GeV}$.
- (b) The upper edge of the first bin htmax_1 is chosen to be the smallest value such that $\sigma_1 \geq x \times \sigma_{\text{tot}}$.
- (c) The remaining upper bin edges $\text{htmax}_{\alpha=2\dots m}$ are chosen similarly with each bin as small as possible such that

$$\sigma_\alpha \equiv \sigma(\text{htmax}_\alpha > H_T > \text{htmin}_\alpha) > x \times \sigma(H_T > \text{htmin}_\alpha), \quad (3)$$

with $\text{htmin}_\alpha = \text{htmax}_{\alpha-1}$, where $\sigma(\text{bin}_k)$ is the sum over $d\sigma_i$ for the range associated with bin_k .

- (d) The final bin is inclusive and determined by $\sigma(\text{bin}_m) \times \mathcal{L} < N/10$, where N is the total number of events to be generated in the final bin.

Note that $x = 0.9$ was used for this study.

3. *Generate weighted events.* We generate $N \simeq 5 \times 10^4$ generator-level events in each of the m bins. For each bin separately, the events are showered, decayed, and matched in Pythia and reconstructed in Delphes. After matching, each bin has $n_k \leq N$ events and an associated matched cross section $\sigma_{\text{LO-matched}}$.

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