Determinations of the Matrix Element $V(ub)$ From Inclusive Semileptonic $B$ Decays With Reduced Model Dependencyingle Ion Trapping for the Enriched Xenon Observatory

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UNIVERSITY OF CALIFORNIA, SAN DIEGO

Determinations of $|V_{ub}|$ from Inclusive Semileptonic $B$ Decays
with Reduced Model Dependency

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