Milky Way Satellite Census. III. Constraints on Dark Matter Properties from Observations of Milky Way Satellite Galaxies

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Introduction.—In the concordance model of cosmology, collisionless cold dark matter (CDM) makes up $\sim 25\%$ of the matter–energy density of the Universe [1]. While dark matter (DM) has the potential to solve a number of outstanding challenges in the Standard Model (SM) of particle physics [2–4], the only positive empirical evidence for DM comes from cosmological and astrophysical observations. Furthermore, by studying the astrophysical distribution of DM, it is possible to probe its particle nature [5, 6]. Specifically, the formation, abundance, and structure of gravitationally bound DM structures, known as “halos,” provide valuable information about viable ranges of the DM particle mass, production mechanism, and couplings to the SM. In particular, the abundance and properties of the smallest DM halos have the potential to indicate a departure from the CDM paradigm [5, 6].

The smallest known DM halos host the ultra-faint dwarf satellite galaxies of the Milky Way (MW) [7]. In these systems, star formation is highly suppressed by reionization and stellar feedback, leading to mass-to-light ratios that are hundreds of times larger than the universal average [7, 8]. Ultra-faint satellite galaxies are thus pristine laboratories for studying DM; in particular, the abundance of these systems is a sensitive probe of any DM physics that suppresses the formation or present-day abundance of small halos.

In particular, the following theoretical paradigms for DM affect the properties of the MW satellite population:

(i) Warm dark matter (WDM) is produced in the early Universe with a temperature of $O(1 \text{ keV})$, although its momentum distribution can be non-thermal. Any viable WDM candidate must be cold enough to reproduce the observed large-scale structure, but its non-negligible free-streaming length suppresses the formation of the low-mass halos that host MW satellite galaxies [9–14]. One of the most popular WDM candidates is a sterile neutrino [15, 16].

(ii) Interacting dark matter (IDM) couples strongly enough to the SM to be heated by interactions with the photon–baryon fluid before recombination. This collisional damping washes out small-scale structure, even if the DM is produced non-thermally [17–19]. DM–nucleon interactions arise in generalizations of the weakly-interacting-massive-particle (WIMP) scenario [20–22], and the impact of DM–radiation interactions on low-mass halos has also been studied [23–25]. Here, we consider a velocity- and spin-independent DM–proton coupling, $c_p$.

(iii) Fuzzy dark matter (FDM) consists of an ultra-light boson with a sufficiently small mass, $O(10^{-22} \text{ eV})$, such that its de Broglie wavelength is comparable to the sizes of dwarf galaxies, $O(1 \text{ kpc})$; this inhibits the formation
of low-mass halos due to the uncertainty principle [26–28]. Ultra-light axions constitute one popular class of FDM [29].

In this Letter, we use novel measurements and modeling of the MW satellite galaxy population to constrain each DM paradigm described above. Specifically, we combine a census of MW satellites [30] from the Dark Energy Survey (DES; [31]) and Pan-STARRS1 (PS1; [32]) with a rigorous forward-modeling framework [33] to fit the position-dependent MW satellite luminosity function in each of these DM paradigms. This procedure fully incorporates inhomogeneities in the observed MW satellite population and marginalizes over uncertainties in the mapping between MW satellite galaxies and DM halos, the efficiency of subhalo disruption due to the MW disk, and the properties of the MW system.

Our analysis yields stringent constraints on each DM paradigm based on the abundance of observed MW satellites. These limits are complementary to constraints from the Lyman-α forest [34–36], strongly-lensed systems [37, 38], and MW stellar streams [39]. Our results imply that CDM is consistent with astrophysical observations down to the smallest currently accessible scales ($k \sim 40 h \, \text{Mpc}^{-1}$) and strongly reinforce previous work demonstrating that there is no “missing satellites problem” in the MW [40]. Throughout this work, we fix cosmological parameters at $h = 0.7$, $\Omega_m = 0.286$, $\Omega_\Lambda = 0.714$, $\sigma_8 = 0.82$, $n_s = 0.96$ [41].

**Analysis Overview.**—Our procedure is based on [19] with several specific improvements for each DM paradigm under consideration. Before discussing each DM paradigm in detail, we describe the main components of our analysis used to connect non-CDM scenarios to the observed MW satellite population. For each paradigm, we assume that the non-CDM component constitutes the entirety of the DM.

**Transfer function.** The linear matter power spectrum, normalized to that of CDM, is used to generate initial conditions for simulations of structure formation. In particular, the transfer function is defined as

$$T^2(k) = \frac{P_{DM}(k)}{P_{CDM}(k)},$$

where $k$ is the cosmological wavenumber, $P_{CDM}(k)$ is the CDM linear matter power spectrum, and $P_{DM}(k)$ is the linear matter power spectrum of a non-CDM model [42]. $P_{DM}(k)$ is obtained by integrating the relevant Boltzmann equation (which may include DM–SM interactions) given the initial DM phase-space distribution. The left panel of Fig. 1 illustrates the transfer function for the three DM paradigms we consider.

It is convenient to define the **half-mode scale**, $k_{hm}$, as the wavenumber satisfying $T^2(k_{hm}) = 0.25$ [43]. The corresponding **half-mode mass**,

$$M_{hm} = \frac{4\pi}{3} \Omega_m \bar{\rho} \left(\frac{\pi}{k_{hm}}\right)^3,$$

is a characteristic mass scale below which the abundance of DM halos is significantly suppressed relative to CDM. Here, $\bar{\rho}$ is the critical density of the Universe today.

**Subhalo mass function (SHMF).** The abundance of subhalos within the virial radius of the MW is expressed as the cumulative number of subhalos as a function of subhalo mass, $M$. We follow [19] by using peak virial mass, defined according to the Bryan-Norman overdensity [44] with $\Delta_{vir} \approx 99.2$ (consistent with our cosmological parameters). We define

$$\left(\frac{dN_{sub}}{dM}\right)_{DM} = f_{DM}(M, \theta_{DM}) \left(\frac{dN_{sub}}{dM}\right)_{CDM},$$

where $f_{DM}(M, \theta_{DM})$ is the suppression of the SHMF relative to CDM and $\theta_{DM}$ are DM model parameters; both $f_{DM}$ and $\theta_{DM}$ depend on the DM model in question. The middle panel of Fig. 1 shows SHMF suppression for the three DM paradigms we consider.

**MW satellite model.** We combine the SHMF suppression in Eq. (3) with the modeling framework from [33] to predict the abundance of observed MW satellites in each DM paradigm. This modeling framework combines cosmological zoom-in simulations [45]—which are chosen to match the inferred mass, concentration, and assembly history of the MW halo and include realistic analogs of the Large Magellanic Cloud system—with a statistical model of the galaxy–halo connection in order to populate subhalos with satellite galaxies.

We implement SHMF suppression by multiplying the detection probability of each mock satellite, which includes terms that model tidal disruption due to the MW disk, the efficiency of galaxy formation, and observational detectability, by a factor of $f_{DM}(M, \theta_{DM})$, following [19, 46]. This procedure assumes that the shape of the observed radial satellite distribution (which our model predicts reasonably well; [33]) is unchanged in alternative DM scenarios, which is consistent with results from cosmological WDM simulations of MW-mass halos [47, 48]. The validity of this assumption is less certain for FDM because dynamical friction operates differently for wave-like versus particle DM, although this difference is expected to be negligible for the ~ $10^8 M_\odot$ subhalos that drive our constraints [49]. The right panel of Fig. 1 shows the predicted satellite luminosity function for each DM model under consideration.

**Fitting procedure.** We fit predicted satellite populations to the observed satellite population from DES and PS1 using the observational selection functions derived in [30], assuming that satellite surface brightness is distributed according to a Poisson point process in each survey footprint [33, 50]. We use the Markov Chain Monte Carlo method to

To be conservative, we account for the uncertainty in halo mass from Gaia measurements of satellite kinematics, i.e. $1.0 \times 10^{12} M_\odot < M_{\text{MW}} < 1.8 \times 10^{12} M_\odot$ [52]. To be conservative, we account for the uncertainty in halo mass on our DM constraints by assuming that the mass scale describing the suppression of the SHMF in each DM paradigm is linearly related to the virial mass of the MW halo, following the scaling for minimum halo mass derived in [33]. In particular, we multiply the upper limit on the characteristic mass scale in each of our non-CDM fits by the ratio of the largest allowed MW halo mass to the average host halo mass in our simulations. We validate this procedure by fitting the observed satellite population using each MW-like simulation separately, which yields reasonable agreement with the linear scaling expectation.

In summary, our fit to the MW satellite population incorporates both intrinsic inhomogeneities in the spatial distribution of MW satellites and those introduced by the varying coverage and depth of current surveys. We assume that alternative DM physics only modifies the SHMF, via Eq. (3), and we report 95% confidence limits on DM model parameters that are marginalized over uncertainties in our MW satellite model and the properties of the MW system.

**WDM Analysis.** Thermal relic WDM with particle mass, $m_{\text{WDM}}$, has been studied extensively in the literature (e.g., [13, 53]) and serves as a benchmark model.

**Transfer function.** The transfer function for thermal relic WDM is given as a function of $m_{\text{WDM}}$ by [53]. This transfer function is commonly assumed in cosmological studies of WDM and facilitates a well-defined comparison to other small-scale structure results [34, 35, 37–39]. However, the simple thermal relic transfer function is inadequate to describe specific particle models of WDM, such as resonantly-produced sterile neutrinos [54]. Thus, constraints on specific DM candidates must be inferred using transfer functions appropriate for the particle model in question, as we discuss below.

**SHMF.** Several authors have implemented the thermal
relic WDM transfer function from [53] in cosmological zoom-in simulations to estimate the suppression of the SHMF in MW-mass host halos [13, 43, 48, 55]. These results depend on the algorithm used to remove spurious halos [55, 56], and therefore vary among studies. Following [57], SHMF suppression for thermal relic WDM can be expressed as

\[ f_{\text{WDM}}(M, m_{\text{WDM}}) = \left[ 1 + \left( \frac{\alpha M_{\text{hm}}(m_{\text{WDM}})}{M} \right)^{\beta} \right]^{\gamma}, \tag{4} \]

where \( \alpha, \beta, \) and \( \gamma \) are constants, and \( M_{\text{hm}} \) is related to \( m_{\text{WDM}} \) in our fiducial cosmology via

\[ M_{\text{hm}}(m_{\text{WDM}}) = 5 \times 10^8 \left( \frac{m_{\text{WDM}}}{3 \text{keV}} \right)^{-10/3} \text{M}_{\odot}. \tag{5} \]

To facilitate comparison with recent WDM constraints from analyses of the MW satellite population [19], strong gravitational lenses [37, 38], and stellar streams [39], we adopt the SHMF from [13], which corresponds to Eq. (4) with \( \alpha = 2.7, \beta = 1.0, \) and \( \gamma = -0.99. \) We note that the recent estimate of the SHMF from [57]—which specifically models resonantly-produced sterile neutrino WDM—is significantly less suppressed than the thermal relic SHMF from [13]. Thus, our fiducial WDM constraint only applies directly to thermal relic DM.

**Fitting procedure.** We implement Eq. (4) in our fit to the MW satellite population to obtain a marginalized posterior distribution over \( M_{\text{hm}}. \) In particular, we fit for \( \log_{10}(M_{\text{hm}}) \) using a uniform prior on this logarithmic quantity, and we translate the resulting limit to \( m_{\text{WDM}} \) using Eq. (5). We translate our thermal relic WDM limit into constraints on resonantly-produced sterile neutrinos by following [58, 59]. Specifically, we analyze sterile neutrino transfer functions over a grid of mass and mixing angle values [60], and we constrain sterile neutrino models that produce transfer functions which are strictly more suppressed than our 95% confidence ruled-out thermal relic WDM model. This procedure is described in detail in the Supplemental Material.

**IDM Analysis.** Our treatment of IDM follows the prescription of [19]. For concreteness, we focus on the case of velocity-independent DM–proton scattering.

**Transfer function.** Following [19], the transfer function in our fiducial IDM model is obtained using the modified version of the Boltzmann solver \textsc{CLASS} described in [20–22], which we use to evolve linear cosmological perturbations in the presence of velocity-independent DM–proton interactions. These interactions are described by the velocity-independent scattering cross section, \( \sigma_0, \) and the DM particle mass, \( m_\phi. \) As noted in [19], transfer functions for this model are very similar to those of thermal relic WDM, modulo dark acoustic oscillations that occur at very small scales and are significantly suppressed for our parameter space of interest.

**SHMF.** Because cosmological zoom-in simulations including DM–proton scattering have not been performed, we follow [19] by mapping the SHMF suppression of IDM to that of WDM based on the correspondence of the transfer functions. In particular, we match the half-mode scales in the transfer functions to construct a relation between \( m_{\text{WDM}} \) and \( (\sigma_0, m_\phi), \) and we assume that the IDM SHMF is identical to the corresponding thermal relic WDM SHMF from [13]. This procedure neglects late-time DM–proton scattering, which [19] estimated to have a negligible impact on subhalo abundances.

**Fitting procedure.** Following [19], we use the mapping procedure described above to translate our 95% confidence limit on thermal relic WDM into limits on \( \sigma_0, \) for several values of \( m_\chi \) in our fiducial IDM model.

**FDM Analysis.** Finally, we provide details on each step for the FDM paradigm. We focus on the case of ultra-light scalar field DM with negligible self-interactions and SM couplings.

**Transfer function.** The FDM transfer function is given as a function of the FDM mass, \( m_\phi, \) by [26]. We note that this transfer function features steeper power suppression than thermal relic WDM for a fixed half-mode scale.

**SHMF.** We assume that the FDM SHMF suppression takes the form of Eq. (3), and we fit the results of the

<table>
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<th>Parameter</th>
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**TABLE I.** Constraints on the WDM, IDM, and FDM paradigms from observations of MW satellite galaxies. Limits for each non-CDM model are derived by assuming that it constitutes the entirety of the DM. The first column lists the DM paradigm, the second column describes the particle physics parameters constrained by this analysis, the third column lists the corresponding constraints at 95% confidence, the fourth column describes the derived property constrained for each DM model, and the fifth column lists constraints on the derived parameters. Limits on the DM–proton scattering cross sections depend on the DM particle mass, \( m_\chi \) (see Fig. 2); for simplicity, we present our constraint for \( m_\chi = 100 \text{MeV}. \)
semi-analytic model in [28] with a function of the form,

\[
    f_{\text{FDM}}(M, m_\phi) = \left[ 1 + \left( \frac{M_0(m_\phi)}{M} \right)^{\tilde{\beta}(m_\phi)} \right]^{\tilde{\gamma}(m_\phi)},
\]

where \( \tilde{\beta}(m_\phi) \) and \( \tilde{\gamma}(m_\phi) \) are provided in the Supplemental Material. The characteristic subhalo mass scale \( M_0 \) is related to the FDM mass via [70]

\[
    M_0(m_\phi) = 1.6 \times 10^{10} \left( \frac{m_\phi}{10^{-22} \text{eV}} \right)^{-4/3} M_\odot.
\]

The SHMF suppression in Eq. (6) encapsulates the effects of tidal stripping on subhalos with solitonic cores, which was explicitly included by [28]. This SHMF suppression is significantly less severe than that estimated from the FDM simulations in [70]. As described in the Supplemental Material, using the SHMF from [70] in our fit yields a limit on the FDM mass that is roughly three times more stringent than our fiducial result. This confirms that the FDM SHMF is a key theoretical uncertainty that must be addressed [27].

\textit{Fitting procedure.} We implement the SHMF in Eq. (6) in our fit to the MW satellite population to obtain a marginalized posterior distribution over \( M_0 \). In particular, we fit for \( \log_{10}(M_0) \) using a uniform prior on this logarithmic quantity, and we translate the resulting limit to \( m_\phi \) using Eq. (7). We note that our procedure for constraining FDM uses the detailed shape of the SHMF suppression in this model, rather than mapping the half-mode scale of the FDM transfer function to that of thermal relic WDM as in [19] or bounding the FDM SHMF by ruled-out thermal relic WDM SHMFs as in [71]. This is necessary because both the shape of the FDM transfer function and the resulting suppression of the SHMF differ in detail from thermal relic WDM (see Fig. 1).

\textit{Results.}—Table I presents our constraints on the WDM, IDM, and FDM paradigms. We describe these results below and translate the limits into constraints on specific models corresponding to each DM paradigm.

(i) \textit{WDM}. Our fit using the thermal relic WDM SHMF suppression from [13] yields \( M_{\text{lim}} < 3.0 \times 10^7 M_\odot \), or \( m_{\text{WDM}} > 7.0 \text{keV} \), at 95% confidence. Linear scaling with MW halo mass yields our fiducial constraint of \( M_{\text{lim}} < 3.8 \times 10^7 M_\odot \), corresponding to \( m_{\text{WDM}} > 6.5 \text{keV} \). This translates to an upper limit on the free-streaming length of \( \lambda_0 \lesssim 10 h^{-1} \text{kpc} \), corresponding to the virial radii of the smallest halos that host MW satellite galaxies, and improves on previous \( m_{\text{WDM}} \) constraints from the MW satellite population by a factor of \( \sim 2 \) [19].

Our constraint on thermal relic WDM translates to a lower limit of 50 keV on the mass of a non-resonant Dodelson–Widrow sterile neutrino [53, 78]. We also translate our thermal relic WDM limit into constraints on...
Several complementary astrophysical and cosmological measurements probe the DM–proton scattering cross section. Stringent limits have been derived by reinterpreting direct detection constraints in the context of cosmic ray upscattering [80]; we do not show these results in Fig. 2 because they constrain the velocity-independent DM–proton cross sections at relativistic energies. The IDM model we consider contributes to the energy density of relativistic species at Big Bang Nucleosynthesis, which sets a lower on its mass that depends on the spin statistics of the DM particle [81–83]. Understanding the interplay of these results with our limits is an important area for future work.

(iii) FDM. We obtain \( M_0 < 1.4 \times 10^8 M_\odot \) at 95% confidence from our fiducial FDM fit. Applying linear MW-host mass scaling yields \( M_0 < 1.8 \times 10^8 M_\odot \) at 95% confidence, or \( m_\phi > 2.9 \times 10^{-21} \text{eV} \). This translates to an upper limit on the de Broglie wavelength of \( \lambda_{\text{dm}} \lesssim 0.5 \text{h}^{-1} \text{kpc} \), roughly corresponding to the sizes of the smallest MW satellite galaxies. Thus, the \( 10^{-22} \text{eV} \) FDM model invoked to solve the core–cusp and too-big-to-fail problems [27], and to fit the internal dynamics of low-surface-brightness [84, 85] and ultra-diffuse [86] galaxies, is strongly disfavored by MW satellite abundances.

To connect to particle models of FDM, we plot this limit in the well-motivated parameter space of ultra-light axion mass versus axion–photon coupling in Fig. 3. For the range of axion–photon couplings that we consider, this mixing has a negligible effect on structure formation. We reiterate that our constraint was derived assuming a light scalar field without self-interactions; this assumption may be violated in specific ultra-light axion models.

Discussion.—In this Letter, we used a state-of-the-art model of the MW satellite galaxy population to place stringent and robust limits on three fundamental DM paradigms: WDM, IDM, and FDM. Although some of these alternative DM models gained popularity by solving apparent small-scale structure “challenges” facing CDM, recent observational and theoretical advances have reversed this scenario. In particular, astrophysical and cosmological observations of the smallest DM structures now provide among the strongest constraints on the microphysical properties of DM.

This analysis improves upon previous work by using MW satellite observations over nearly the entire sky, including the population of ultra-faint dwarf galaxies discovered by DES. In addition, our modeling framework rigorously accounts for satellite detectability and uncertainties in the galaxy–halo connection. Our constraints are comparable in sensitivity to Lyman-\( \alpha \) forest, strong lensing, and stellar stream perturbation analyses. Future cosmic surveys promise to further improve these measurements [87, 88].

The breadth of DM models constrained by observations of MW satellites is particularly important given the mass and mixing angle of resonantly-produced sterile neutrinos assuming a Shi–Fuller production mechanism [79], following the conservative procedure described above. As shown in Fig. 2, our analysis rules out nearly the entire remaining parameter space for resonantly produced sterile neutrinos in the Neutrino Minimal Standard Model [66] at greater than 95% confidence. In addition, we robustly rule out the resonantly produced sterile neutrino interpretation of the 3.5 keV X-ray line [61].

(ii) IDM. Mapping our \( m_{\text{WDM}} > 6.5 \text{keV} \) constraint to the DM–proton scattering model following the procedure in [19] yields constraints on the velocity-independent interaction cross section of \( (7.0 \times 10^{-30}, 2.6 \times 10^{-29}, 8.8 \times 10^{-29}, 1.7 \times 10^{-27}) \text{cm}^2 \) for DM particle masses of \( (10^{-5}, 10^{-3}, 10^{-1}, 10) \text{GeV} \) at 95% confidence, as shown in Fig. 2. These constraints scale as \( m_\chi^{1/4} (m_\chi) \) for \( m_\chi \ll 1 \text{GeV} \) (\( m_\chi \gg 1 \text{GeV} \)), and are highly complementary to direction detection limits, particularly at low DM masses [19]. At a DM mass of 100 MeV, our limit translates into an upper bound on the DM–proton coupling of \( c_p \lesssim (0.3 \text{GeV})^{-2} \) [20].

Despite our conservative marginalization over MW halo mass, these results improve upon those in [19] by a factor of \( \sim 3 \) at all DM masses. This is stronger than the improvement expected from the analytic prediction for cross section constraints derived in [19] due to a more precise determination of the SHMF, resulting from the sky coverage and sensitivity of DES and PS1.
the growing interest in a wide range of theoretical possibilities following non-detections in collider, direct, and indirect searches for canonical WIMPs. In addition to the three DM paradigms considered in this work, small-scale structure measurements are also sensitive to the initial DM velocity distribution in non-thermal DM production from scalar field decay [89], the formation redshift of DM in “late–forming” DM models [90], the DM self-interaction cross section [91–94], and the lifetime of decaying DM [95, 96].

Future work could generalize our approach by measuring deviations in the small-scale linear matter power spectrum relative to a baseline CDM scenario, rather than setting constraints in the context of particular DM models. Features in the power spectrum on extremely small scales are a hallmark of many inflationary models [97, 98], and it is conceivable that DM substructure measurements can be used to infer the nature of the corresponding primordial density fluctuations.

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description of the suppression of the SHMF in this model. We therefore implemented two popular forms of the FDM
yields \( L \) and lepton asymmetry \( M \) transfer functions to the \( \text{CLASS} \) generated by [60] using sterile neutrinos, we follow the procedure in [58, 59]. In particular, we use the sterile neutrino transfer functions \( \alpha \) This SHMF suppression corresponds to Eq. (4) with appropriate for a 7 keV resonantly-produced sterile neutrino with various lepton asymmetry (or mixing angle) values. The overproduction (underproduction) boundaries correspond to sterile neutrino models with zero (maximal) lepton asymmetry in the Neutrino Minimal Standard Model [58].

Our DM limits are derived by running \( 10^5 \) iterations of the MCMC sampler \texttt{emcee} [51] to sample the eight galaxy–halo connection model parameters described in [33], plus the DM model parameter of interest (i.e., \( M_{\text{hm}} \) for our thermal relic WDM fit and \( M_0 \) for our FDM fit), using 36 walkers. The eight galaxy–halo connection model parameters are shown in Table II and described in detail by [33]. For both our thermal relic WDM and FDM fits, we discard a generous burn-in period of \( 2 \times 10^4 \) steps, corresponding to \( \sim 20 \) autocorrelation lengths. We use the Python package \texttt{ChainConsumer} [99] to visualize the posterior distributions and calculate confidence intervals.

The posterior distributions over galaxy–halo connection and DM model parameters for our thermal relic WDM and FDM fits are shown in Fig. 4 and Fig. 5, respectively. Our IDM constraints are derived using the \( M_{\text{hm}} \) limit from our thermal relic WDM fit; thus, we do not show a separate posterior for the IDM analysis.

### Resonantly-Produced Sterile Neutrino Constraints

To translate our upper bound on the mass of thermal relic WDM into constraints on resonantly-produced Shi–Fuller sterile neutrinos, we follow the procedure in [58, 59]. In particular, we use the sterile neutrino transfer functions generated by [60] using \texttt{CLASS} for a grid of sterile neutrino masses and mixing angles. We then compare these transfer functions to the \( m_{\text{WDM}} = 6.5\text{keV} \) thermal relic transfer function that is ruled out at 95% confidence by our analysis. We derive the limits in Fig. 2 by finding the combinations of sterile neutrino mass and mixing angle between the “DM Underproduction” and “DM Overproduction” lines in Fig. 2 that yield transfer functions which are strictly more suppressed than the ruled-out thermal relic transfer function. The overproduction (underproduction) boundaries correspond to sterile neutrino models with zero (maximal) lepton asymmetry in the Neutrino Minimal Standard Model [58].

We benchmark our sterile neutrino limits using the recent estimate of SHMF suppression from [57], which is appropriate for a 7 keV resonantly-produced sterile neutrino with various lepton asymmetry (or mixing angle) values. This SHMF suppression corresponds to Eq. (4) with \( \alpha = 4.2, \beta = 2.5, \gamma = -0.2 \), and the relation between \( M_{\text{hm}} \) and lepton asymmetry \( L_6 \) is given for several models in [57]. Using this SHMF in our fitting procedure, we find \( M_{\text{hm}} < 5.9 \times 10^5 \, M_\odot \) at 95% confidence. Applying linear scaling with MW halo mass to the result of the joint fit yields \( M_{\text{hm}} < 7.6 \times 10^7 \, M_\odot \), which rules out the coldest sterile neutrino model presented in [57]—corresponding to \( m_s = 7 \text{keV} \) and \( L_6 = 8 \)—at \( \gg 95\% \) confidence, consistent with our limit in Fig. 2.

### FDM Subhalo Mass Functions

Due to the difficulties of simulating non-linear structure formation in FDM, no consensus exists for a quantitative description of the suppression of the SHMF in this model. We therefore implemented two popular forms of the FDM

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Physical Interpretation</th>
<th>95% confidence interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \alpha )</td>
<td>Power-law slope of satellite luminosity function</td>
<td>(-1.46 &lt; \alpha &lt; -1.38)</td>
</tr>
<tr>
<td>( \sigma_M )</td>
<td>Scatter in satellite luminosity at fixed halo properties</td>
<td>( 0 \text{dex}^* &lt; \sigma_M &lt; 0.2 \text{dex} )</td>
</tr>
<tr>
<td>( M_{50} )</td>
<td>Peak mass at which 50% of halos host galaxies</td>
<td>( 7.5^* &lt; \log(M_{50}/M_\odot) &lt; 8.0 )</td>
</tr>
<tr>
<td>( B )</td>
<td>Subhalo disruption efficiency relative to FIRE simulations</td>
<td>( 0.2 &lt; B &lt; 1.9 )</td>
</tr>
<tr>
<td>( \sigma_{\text{gal}} )</td>
<td>Width of the galaxy occupation fraction</td>
<td>( 0 \text{dex}^* &lt; \sigma_{\text{gal}} &lt; 0.66 \text{dex} )</td>
</tr>
<tr>
<td>( \mathcal{A} )</td>
<td>Amplitude of relation between galaxy size and halo size</td>
<td>( 0 \text{pc}^* &lt; \mathcal{A} &lt; 90 \text{pc} )</td>
</tr>
<tr>
<td>( \sigma_{\log R} )</td>
<td>Scatter in galaxy size at fixed halo properties</td>
<td>( 0.1 \text{dex}^* &lt; \sigma_{\log R} &lt; 1.1 \text{dex} )</td>
</tr>
<tr>
<td>( n )</td>
<td>Power-law slope of relation between galaxy size and halo size</td>
<td>( 0^* &lt; n &lt; 1.9 )</td>
</tr>
<tr>
<td>( M_{\text{shmf}} )</td>
<td>Mass scale of thermal relic SHMF suppression (Eq. (5))</td>
<td>( 7.0^* &lt; \log(M_{\text{shmf}}/M_\odot) &lt; 7.5 )</td>
</tr>
<tr>
<td>( M_0 )</td>
<td>Mass scale of FDM SHMF suppression (Eq. (7))</td>
<td>( 7.0^* &lt; \log(M_0/M_\odot) &lt; 8.1 )</td>
</tr>
</tbody>
</table>

TABLE II. Galaxy–halo connection and DM model parameters varied in our thermal relic WDM and FDM fits to the MW satellite population. Note that \( M_0 \) is constrained in a separate fit that yields similar confidence intervals for the eight galaxy–halo connection parameters. Asterisks mark prior-driven constraints. See [33] for details on our galaxy–halo connection model.
\[ \alpha = -1.429^{+0.023}_{-0.031} \]

\[ \sigma_M = 0.007^{+0.096}_{-0.000} \]

\[ M_{50} = 7.51^{+0.22}_{-0.00} \]

\[ B = 1.01^{+0.45}_{-0.40} \]

\[ \sigma_{\text{gal}} = 0.047^{+0.304}_{-0.014} \]

\[ A = 35^{+28}_{-21} \]

\[ \sigma_{\log R} = 0.44^{+0.34}_{-0.17} \]

\[ n = 1.15^{+0.39}_{-0.50} \]

\[ M_{\text{hm}} = 7.01^{+0.23}_{-0.00} \]

SHMF to assess this uncertainty. The nominal model described in the text is the semi-analytic model derived in [28]. Our fit to this function is given by Eq. (6), with

\[ \tilde{\beta}(m_\phi) = \exp \left[ -\left( \frac{m_\phi}{13.7 \times 10^{-22} \text{eV}} \right)^{0.67} \right] + 0.77 \quad (8) \]

\[ \tilde{\gamma}(m_\phi) = 0.22 \log \left( \frac{m_\phi}{10^{-22} \text{eV}} \right)^{0.45} - 0.78. \quad (9) \]

An alternative model for the suppression of the halo mass function is derived from the “wave dark matter” simulations in [70], which corresponds to Eq. (6) with \( \tilde{\beta} = 1.1 \) and \( \tilde{\gamma} = -2.2 \). This mass function was estimated using...
high-redshift ($z > 4$) simulation outputs and is systematically more suppressed than that derived semi-analytically in [28]. Adopting this alternative SHMF in our fitting procedure and accounting for the uncertainty in MW halo mass yields $M_0 < 3.4 \times 10^7 \, M_\odot$ at 95% confidence, corresponding to $m_\phi > 9.1 \times 10^{-21} \, eV$. Thus, the current FDM SHMF uncertainty results in roughly a factor of three difference relative to our fiducial $m_\phi > 2.9 \times 10^{-21} \, eV$ constraint.

We caution that these uncertainties underlie FDM predictions from both semi-analytic models and simulations. For example, [70] simulate CDM-like particles with initial conditions appropriate for FDM, and thus do not solve the Schrödinger–Poisson system that governs FDM. This is an important caveat, because interference patterns on scales comparable to the de Broglie wavelength can potentially affect structure formation. Meanwhile, the semi-analytic treatment in [28] does not explicitly account for the “quantum pressure” term in the Madelung transformation of the Schrödinger–Poisson system, and makes several assumptions about the tidal evolution of subhalos with solitonic density profiles. The derivation of robust, quantitative predictions for the FDM SHMF represents an active area of theoretical and computational study.

FIG. 5. Same as Fig. 4, but for our FDM fit.